## MATH 210: Who can eat both?

## NAME:

1. Consider the following problem:

Aaron, Bob, and Chad all go out to eat together every day for lunch. They each order either a ham sandwich or a pork loin. However, they always adhere to the following rules:

- i. If Aaron orders ham, Chad orders pork.
- ii. Either Aaron or Bob orders ham, but not both.
- iii. Bob and Chad do not both order pork

Let A be the statement 'Aaron orders ham'. Let B be the statement 'Bob orders ham'. And let C be the statement 'Chad orders ham'.

- (a) What does  $\sim A$  mean?
- (b) Symbolize statement i.
- (c) Symbolize statement ii.
- (d) Symbolize statement iii.
- (e) Symbolize statement i using only  $\land$ ,  $\lor$ , or  $\sim$ . (i.e. without using  $\Rightarrow$ .)
- (f) Use De Morgan's Laws to symbolize statement iii using only  $\lor$ .
- (g) Let  $E = i \wedge ii \wedge iii$ . Simplify E assuming A = T.
- (h) Simplify E assuming A = F.

- (i) What can we conclude from the previous parts in terms of the problem?
- (j) Simplify E assuming B = F (and not knowing anything about A).
- (k) Simplify E assuming B = T (and not knowing anything about A).
- (l) What can we conclude from the previous parts in terms of the problem?
- (m) Simplify E assuming C = T (and not knowing anything about A or B).
- (n) Simplify E assuming C = F (and not knowing anything about A or B).
- (o) What can we conclude from the previous parts in terms of the problem?
- (p) Write a proof of "Aaron eats pork and Bob eats ham".