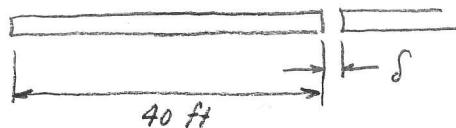


4-75



$s$  so rails just touch when  $\Delta T = 90^\circ F - (-20^\circ F) = 110^\circ F$

$$s = \alpha \Delta T L = \left(6.6 \times 10^{-6} \frac{1}{^\circ F}\right) (110^\circ F) (40 \text{ ft} \left(\frac{12 \text{ in}}{\text{ft}}\right)) = [0.348 \text{ in.}]$$

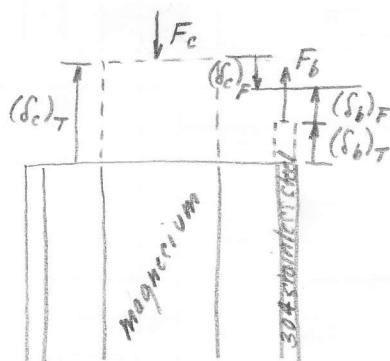
Force in rail after gap closed if  $\Delta T = 110^\circ F - 90^\circ F = 20^\circ F$

$$\delta_T = \delta_F$$

$$\left(6.6 \times 10^{-6} \frac{1}{^\circ F}\right) (20^\circ F) \left(40 \text{ ft} \left(\frac{12 \text{ in}}{\text{ft}}\right) + 0.348 \text{ in.}\right) = F \left(\frac{40 \text{ ft} (12 \text{ in}) + 0.348 \text{ in.}}{(5.10 \text{ in}^2)(29,000 \frac{\text{kip}}{\text{in}^2})}\right)$$

$F = 19.5 \text{ kip}$

4-81



equilibrium:  $\sum F_y = 0, F_b = F_c$

force in steel, both bolts

compatibility:

$$(\delta_c)_T - (\delta_c)_F = (\delta_b)_T + (\delta_b)_F$$

$$(\delta_c)_F + (\delta_b)_F = (\delta_c)_T - (\delta_b)_T$$

load displacement: subst  $F_b = F_c$

	unit	cylinder	bolt
$\alpha$	$\frac{1}{^\circ C}$	$26 \times 10^{-6}$	$17 \times 10^{-6}$
$E$	$\frac{kN}{m^2}$	$44.7 \times 10^6$	$193 \times 10^6$
$L$	m	0.100	0.150
$r$	m	0.025	0.005

$$\frac{F_c (0.100 \text{ m})}{\pi (0.025 \text{ m})^2 (44.7 \times 10^6 \frac{kN}{m^2})} + \frac{F_c (0.150 \text{ m})}{2 \pi (0.005 \text{ m})^2 (193 \times 10^6 \frac{kN}{m^2})} =$$

$$(26 \times 10^{-6} \frac{1}{^\circ C}) (110^\circ C) (0.100 \text{ m}) - (17 \times 10^{-6} \frac{1}{^\circ C}) (110^\circ C) (0.150 \text{ m})$$

$$1.1394 \times 10^{-6} \frac{m}{kN} F_c + 4.9478 \times 10^{-6} \frac{m}{kN} F_c =$$

$$6.0872 \times 10^{-6} \frac{m}{kN} F_c = 5.50 \times 10^{-6} \text{ m}$$

$$F_c = 0.9035 \text{ kN or } [904 \text{ N}]$$