## Experiments

To Accompany<br>Quantitative Chemical Analysis, $9^{\text {th }}$ Edition (2010)<br>Daniel C. Harris

0. Green Analytical Chemistry ..... 4
1. Calibration of Volumetric Glassware ..... 12
2 Gravimetric Determination of Calcium as $\mathrm{CaC}_{2} \mathrm{O}_{4} \cdot \mathrm{H}_{2} \mathrm{O}$ ..... 16
2. Gravimetric Determination of Iron as $\mathrm{Fe}_{2} \mathrm{O}_{3}$ ..... 18
3. Penny Statistics ..... 21
4. Statistical Evaluation of Acid-Base Indicators ..... 29
5. Preparing Standard Acid and Base ..... 34
6. Using a pH Electrode for an Acid-Base Titration ..... 37
7. Analysis of a Mixture of Carbonate and Bicarbonate ..... 40
8. Analysis of an Acid-Base Titration Curve: The Gran Plot ..... 42
9. Fitting a Titration Curve with Excel Solver ${ }^{\circledR}$ ..... 47
10. Kjeldahl Nitrogen Analysis ..... 55
11. EDTA Titration of $\mathrm{Ca}^{2+}$ and $\mathrm{Mg}^{2+}$ in Natural Waters ..... 58
12. Synthesis and Analysis of Ammonium Decavanadate ..... 60
13. Iodimetric Titration of Vitamin C ..... 64
14. Preparation and Iodometric Analysis of High-Temperature Superconductor ..... 66
15. Potentiometric Halide Titration with $\mathrm{Ag}^{+}$ ..... 71
16. Electrogravimetric Analysis of Copper ..... 75
17. Polarographic Measurement of an Equilibrium Constant ..... 77
18. Coulometric Titration of Cyclohexene with Bromine ..... 79
19. Spectrophotometric Determination of Iron in Vitamin Tablets ..... 83
20. Microscale Spectrophotometric Measurement of Iron in Foods by Standard Addition ..... 85
21. Spectrophotometric Measurement of an Equilibrium Constant ..... 87
22. Spectrophotometric Analysis of a Mixture: Caffeine and Benzoic Acid in Soft Drink ..... 90
23. $\mathrm{Mn}^{2+}$ Standardization by EDTA Titration ..... 93
24. Measuring Manganese in Steel by Spectrophotometry with Standard Addition ..... 95
25. Measuring Manganese in Steel by Atomic Absorption Using a Calibration Curve ..... 99
26. Properties of an Ion-Exchange Resin ..... 102
27. Analysis of Sulfur in Coal by Ion Chromatography ..... 105
28. Measuring Carbon Monoxide in Automobile Exhaust by Gas Chromatography ..... 107
29. Amino Acid Analysis by Capillary Electrophoresis ..... 109
30. DNA Composition by High-Performance Liquid Chromatography ..... 113
31. Analysis of Analgesic Tablets by High-Performance Liquid Chromatography ..... 116
32. Anion Content of Drinking Water by Capillary Electrophoresis ..... 118
33. Green Chemistry: Liquid Carbon Dioxide Extraction of Lemon Peel Oil ..... 121

## Experiments

Experiments described here illustrate major analytical techniques described in the textbook, Quantitative Chemical Analysis. Procedures are organized roughly in the same order as topics in the text. You are invited to download these instructions and reproduce them freely for use in your laboratory. References to many additional experiments published in recent years in the Journal of Chemical Education ${ }^{1}$ are listed at the web site where you found these experiments. Some of the experiments refer to the availability of standards or unknowns from Thorn Smith. ${ }^{2}$

Although these procedures are safe when carried out with reasonable care, all chemical experiments are potentially hazardous. Any solution that fumes (such as concentrated HCl ), and all nonaqueous solvents, should be handled in a fume hood. Pipetting should never be done by mouth. Spills on your body should be flooded immediately with water and washed with soap and water; your instructor should be notified for possible further action. Spills on the benchtop should be cleaned immediately. Toxic chemicals should not be flushed down the drain. Your instructor should establish a procedure for disposing of each chemical that you use.

When equipment permits, it is environmentally friendly and economical to reduce the scale of an experiment. For example, $50-\mathrm{mL}$ burets can be replaced by $10-\mathrm{mL}$ burets at some loss in analytical precision, but little educational loss. An even smaller scale is possible with microburets made from 2-mL pipets. ${ }^{3}$ Micropipets and small volumetric flasks can replace large glass pipets and large volumetric flasks (again at a sacrifice of precision). With properly chosen electrodes, potentiometric titrations can be performed on a scale of a few milliliters, instead of tens of milliliters, by using a syringe or a micropipet to deliver titrant. Instructions here were written for the commonly available, large-size lab equipment, but your modification to a smaller scale is encouraged.

1. You can search for experiments by key words in the index of the Journal of Chemical Education at http://jchemed.chem.wisc.edu/
2. Thorn Smith Inc., www.thornsmithlabs.com. The following analyzed unknowns are available: Al-Mg alloy (for $\mathrm{Al}, \mathrm{Mg}$ ), Al- Zn alloy (for $\mathrm{Al}, \mathrm{Zn}$ ), Sb ore (for Sb ), brasses (for $\mathrm{Sn}, \mathrm{Cu}, \mathrm{Pb}, \mathrm{Zn}$ ), calcium carbonate (for Ca ), cast iron (for $\mathrm{P}, \mathrm{Mn}, \mathrm{S}, \mathrm{Si}, \mathrm{C}$ ), cement (for $\mathrm{Si}, \mathrm{Fe}, \mathrm{Al}, \mathrm{Ca}, \mathrm{Mg}, \mathrm{S}$, ignition loss), Cr ore (for Cr ), Cu ore (for Cu ), copper oxide (for Cu ), ferrous ammonium sulfate (for Fe ), Fe ore (for Fe ), iron oxide (for Fe ), limestone (for $\mathrm{Ca}, \mathrm{Mg}, \mathrm{Si}$, ignition loss), magnesium sulfate (for Mg ), Mn ore (for Mn ), Monel metal (for $\mathrm{Si}, \mathrm{Cu}, \mathrm{Ni}$ ), nickel silver (for $\mathrm{Cu}, \mathrm{Ni}, \mathrm{Zn}$ ), nickel oxide (for Ni ), phosphate rock (for P ), potassium hydrogen phthalate (for $\mathrm{H}^{+}$), silver alloys (for $\mathrm{Ag}, \mathrm{Cu}, \mathrm{Zn}, \mathrm{Ni}$ ), soda ash (for $\mathrm{Na}_{2} \mathrm{CO}_{3}$ ), soluble antimony (for Sb ), soluble choride, soluble oxalate, soluble phosphate, soluble sulfate, steels (for $\mathrm{C}, \mathrm{Mn}, \mathrm{P}, \mathrm{S}, \mathrm{Si}, \mathrm{Ni}, \mathrm{Cr}, \mathrm{Mo}$ ), Zn ore (for Zn ). Primary standards are also available: potassium hydrogen phthalate (to standardize NaOH ), $\mathrm{As}_{2} \mathrm{O}_{3}$ (to standardize $\mathrm{I}_{2}$ ), $\mathrm{CaCO}_{3}$ (to standardize EDTA), $\mathrm{Fe}\left(\mathrm{NH}_{4}\right)_{2}\left(\mathrm{SO}_{4}\right)_{2}$ (to standardize dichromate or permanganate), $\mathrm{K}_{2} \mathrm{Cr}_{2} \mathrm{O}_{7}$ (to standardize thiosulfate), $\mathrm{AgNO}_{3}, \mathrm{Na}_{2} \mathrm{CO}_{3}$ (to standardize acid), NaCl (to standardize $\mathrm{AgNO}_{3}$ ), $\mathrm{Na}_{2} \mathrm{C}_{2} \mathrm{O}_{4}$ (to standardize $\mathrm{KMnO}_{4}$ ).
3. M. M. Singh, C. McGowan, Z. Szafran, and R. M. Pike, J. Chem. Ed. 1998, 75, 371; ibid. 2000, 77, 625.

## 0. Green Analytical Chemistry ${ }^{4}$

In recent years, it has become a trend to develop items as "green," with a perceived environmental friendliness. The field known as "green chemistry" can be traced back to the book Green Chemistry: Theory and Practice ${ }^{5}$ published in 1998 by Paul Anastas and John Warner. They defined green chemistry as "the use of a set of principles that reduces or eliminates the use or generation of hazardous substances in the design, manufacture, and application of chemical products." A key item to notice with this definition is that green chemistry is a set of principles, that is, a way of thinking about chemistry. It is not a separate chemical discipline like analytical, organic, or physical. In fact, it is hoped that the current generation of chemistry students taking this course will have this mode of thinking become so natural to them that we will no longer have to think about "green chemistry," but just "chemistry."

How, then, does analytical chemistry fit into this way of thinking? What is green analytical chemistry? To answer these questions, we must first reconsider what is analytical chemistry and what is green chemistry.

During this course, you will learn a series of methods to qualitatively and quantitatively characterize a sample or chemical system. Knowledge of these methods and the chemical principles behind them is an asset valued by many industries. On the other hand, analytical chemists may be viewed as a necessary evil, for example, to analyze samples in order to comply with Food and Drug Administration or other regulatory agency requirements. Analytical chemistry is something that is tolerated, but the analysis costs money, rather than adding to a company's profits. Consider the following example: You work for a detergent manufacturer and a product development chemist comes into your lab with a bottle of detergent, asking you to determine the silicone level in this product. While you could easily do what you are told, upon questioning you find out that the product development chemist really doesn't want to know the silicone concentration. What he really wants to know is why the product isn't performing the way it should (maybe it foams too much or doesn't clean effectively) and he thinks it's related to the silicone concentration. A good analytical chemist does not merely provide data, but rather supplies information and knowledge upon which educated decisions can be based.

Analytical chemists are problem solvers. We use our knowledge to become partners with our customers to answer their questions. In the detergent analysis example, one analytical

[^0]chemist might have run the silicone analysis and then several other analyses in order to eventually solve the problem. But the analytical chemist who was a true scientific partner in the process understood the problem and used his knowledge of chemistry to develop a more refined hypothesis and streamline the analyses need to answer the ultimate question more easily. This role of the analytical chemist was summarized by Prof. Herb Laitinin who editorialized, "Analysis of a sample is not the true aim of analytical chemistry...the real purpose of the analysis is to solve a problem." ${ }^{6}$ Development of problem-solving skills comes with a combination of analytical knowledge and experience. In summary, the analytical chemist is a problem solver and solving problems involves a means of thinking about chemistry.

## What is Green Chemistry?

We've defined green chemistry as something that is applied over the entire lifespan of a product. Hidden within this definition is a combination of environmental and economic concerns. That is, a product may have environmental benefits, but if it cannot compete in the marketplace, it is doomed to failure. Green chemistry is guided by the set of 12 principles developed by Anastas and Warner ${ }^{5}$ and shown in Table 1.

If green chemistry and concern for the environment are the right things to do, why haven't we been doing this all along? Think about organic chemistry. It isn't always easy to choose the right reagents to put the correct functional groups in the right places for a complex synthesis. Now consider that you are working as a product development chemist in industry. Not only must you synthesize the compound with properties desired by your company, but you must do it in a manner that can be passed on to a process engineer who can develop the process with high yield, speed, safety, and minimal cost. Now add environmental concerns on top of all of that and the lament of a certain amphibian character, "It's not easy being green," becomes more obvious. In summary, green chemistry involves a way of thinking about chemistry in an environmentally and economically sound manner.

[^1]
## Table 1. The 12 Principles of Green Chemistry ${ }^{5}$

## 1. Prevention

It is better to prevent waste than to treat or clean up waste after it has been created.

## 2. Atom Economy

Synthetic methods should be designed to maximize the incorporation of all materials used in the process into the final product.

## 3. Less Hazardous Chemical Syntheses

Wherever practicable, synthetic methods should be designed to use and generate substances that possess little or no toxicity to human health and the environment.
4. Designing Safer Chemicals

Chemical products should be designed to effect their desired function while minimizing their toxicity.
5. Safer Solvents and Auxiliaries

The use of auxiliary substances (e.g., solvents, separation agents, etc.) should be made unnecessary wherever possible and innocuous when used.
6. Design for Energy Efficiency

Energy requirements of chemical processes should be recognized for their environmental and economic impacts and should be minimized. If possible, synthetic methods should be conducted at ambient temperature and pressure.
7. Use of Renewable Feedstocks

A raw material or feedstock should be renewable rather than depleting whenever technically and economically practicable.

## 8 Reduce Derivatives

Unnecessary derivatization (use of blocking groups, protection/ deprotection, temporary modification of physical/chemical processes) should be minimized or avoided if possible, because such steps require additional reagents and can generate waste.
9. Catalysis

Catalytic reagents (as selective as possible) are superior to stoichiometric reagents.

## 10. Design for Degradation

Chemical products should be designed so that at the end of their function they break down into innocuous degradation products and do not persist in the environment.

## 11. Real-time analysis for Pollution Prevention

Analytical methodologies need to be further developed to allow for real-time, in-process monitoring and control prior to the formation of hazardous substances.

## 12. Inherently Safer Chemistry for Accident Prevention

Substances and the form of a substance used in a chemical process should be chosen to minimize the potential for chemical accidents, including releases, explosions, and fires.

## What is Green Analytical Chemistry?

Reviewing the previous summary statement, we can correctly guess that green analytical chemistry is a marriage of thought processes - a unique way of thinking about how to do chemistry. Performing chemical analyses in a green manner does not mean that we must make compromises to the requisite accuracy, precision, and other analytical demands. Inserting green values into the laboratory is about several factors related to the 12 green chemistry principles, including waste, energy, toxicity, and others. For example, the hazard associated with a given chemical is related to both our exposure to the chemical and the inherent risk possessed by the chemical. While we can wear personal protective equipment, like safety glasses, lab coats, and latex gloves, or work in a fume hood, we cannot change the inherent risk associated with a compound. So perhaps we can change the reagent. We've been doing this for years. Benzene and carbon tetrachloride were banished from the lab since the mid-1970s. But our practices must continue to evolve as our knowledge about chemicals and their inherent risk progresses.

At least half of the 12 principles of green chemistry apply to the analytical laboratory:
Principle 1: Prevent Waste. While the wastes generated in chemical production overshadow the amount of waste coming from a typical analytical laboratory, individual analytical procedures may involve as much as one liter of organic solvent to extract the analytes from the sample. When used in an analytical procedure, even water, which everyone would agree is an environmentally benign solvent, is converted to wastewater which must be treated appropriately. So the professional analyst must stay abreast of developments that can minimize waste generation.

Principle 5: Safer Solvents and Auxiliaries. The inherent risk associated with a chemical must be considered and alternatives explored. The risk may be toxicological, but may also be flammability, corrosivity, or other attributes. If alternatives do not exist, appropriate exposure controls are needed.

Principle 6: Energy Efficiency. Several common analytical procedures can be considered energy intensive. For example, not only are large amounts of solvents used in extractions, in most cases the solvent must then be evaporated to concentrate the solutes for analysis.
Instrumental procedures can require high temperatures or have high power demands. Sometimes trade-offs must be considered. Does it require less energy to keep a drying oven turned on overnight and maintain a constant temperature or to turn off the oven and require a rapid heat up just prior to use? If water is used as a nontoxic solvent, do we pay a price in the energy needed to evaporate water compared with many organic solvents? Later, we will present a set of metrics to judge these compromises.

Principle 8: Reduce Derivatives. Many times chemical derivatives are employed to enhance the solubility or detectability of sample components. For example, the determination of fats in foods requires conversion of fatty acids into methyl esters for gas chromatography. However, technological advances can provide similar analytical results while avoiding the need for derivatization. For example, modern high-performance liquid chromatography can provide results equivalent to previous generations of gas chromatography.

Principle 11: Real-time Analysis. This principle is analytical chemistry!!! The field of process analytical chemistry, involving in-line, on-line, or at-line procedures, is a valuable tool in chemical processing. By monitoring the creation of a by-product, the poisoning of a catalyst, reaction pH , or other properties, feedback is provided to allow a reaction or process to stay in control, avoiding potential process disruptions.

Principle 12: Safer Chemistry. The flammability of solvents, oxidative capability of reagents, and similar factors should be considered in developing analytical methods.

Several of the experiments in this laboratory manual illustrate green chemistry. For example, Experiment 11 (Kjeldahl Nitrogen Analysis) uses selenium-coated boiling chips, rather than a mercury compound, as a catalyst (Principle 9); Experiment 15 (Preparation and Iodometric Analysis of a High-Temperature Semiconductor) reminds us that high-temperature superconductors could help us toward energy sustainability (Principle 6); and Experiments 28 (Analysis of Sulfur in Coal by Ion Chromatography) and 29 (Measuring Carbon Monoxide in Automobile Exhaust by Gas Chromatography) illustrate the role of analytical chemistry in pollution prevention (Principles 1 and 11). A new experiment 34, Green Chemistry: Liquid Carbon Dioxide Extraction of Lemon Peel Oil, demonstrates the potential of new technology (supercritical fluid extraction) to address solvent alternatives (Principles 1 and 5). We challenge students to discuss your experiments relative to the 12 green chemistry principles as you write your reports.

Now that we've gotten some idea of what green analytical chemistry is, let's discuss some specific green analytical considerations. Some review articles ${ }^{7,8,9}$ present more detailed discussions of advances in the field of analytical chemistry that exhibit green chemistry attributes. However, general considerations for the practice of green analytical chemistry can be summarized:

Planning. Proper planning allows the maximum amount of information to be obtained from the minimal number of analyses. A branch of statistics called Design of Experiments can be used to guide planning laboratory procedures. The developing field of chemometrics allows

[^2]us to uncover relationships between sample sets that might be hidden if conventional thinking is used.

Sampling. Attention to proper sampling is an often overlooked portion of chemical analysis, but perhaps the most important step in the entire analysis. A common misconception is that an analytical method can be made green simply by being performed at the micro-scale. While this is true, one must take care to ensure that the appropriate (minimum) sample size is used. The sample must be collected to be statistically representative of the system under study and homogenized to reduce error.

Direct Analysis. Methods which do not require sample work-up prior to the measurement step have several advantages, including greenness. Techniques employing ionselective electrodes, reflectance spectroscopy, or surface analysis can often provide chemical information without using additional analytical reagents.

Sample Preparation. Organic extractions and acid digestions generate the greatest amount of waste (while using hazardous solvents or acids) in many procedures. This field has received considerable attention in modern times. Acid digestions can be made safer through the application of microwave irradiation. Alternative solvent processes using water, ionic liquids, or careful manipulation of heat and energy can greatly enhance the sample preparation process.

Chromatography. Separation of analyte from other sample components is necessary in most analytical procedures. Chromatography can involve copious amounts of solvents, sorbents, and other chemicals. Microcolumn chromatography reduces solvent consumption, minimizes the use of chromatographic sorbents, and provides superior performance.

Data Reduction. Statistical manipulations can mine information from analytical results. Many times unambiguous compound identification is not needed; rather knowledge of trends is sufficient.

Field Analysis and Process Analysis. Taking the analysis to the sample generally provides several green advantages. Near instantaneous feedback can minimize the likelihood of a process upset. Similarly, the backhoe operator at an environmental clean-up site would like instantaneous notification that the site is clean so she can quit digging, rather than waiting for results to come back from the laboratory. One contribution of analytical chemistry to the environmental movement has been the identification of hazards within the environment. Careful execution of field and process analysis may advance analytical chemistry from an identification and compliance model to a hazard prevention model.

## How Do We Decide if a Method is Green?

A good place to start is to compare an analytical method against the 12 principles of green chemistry. However, keep in mind that compromises are made along the way. One method might use less solvent, while another is less energy intensive. No procedure is truly green; rather, one method may be considered greener than another.

One set of metrics used to assess the green profile of a method is associated with the National Environmental Monitoring Index (NEMI) database (www.nemi.gov). The NEMI database was compiled by researchers from several federal agencies, the American Chemical Society Green Chemistry Institute, and others. This free, on-line database lists regulatory and nonregulatory methods and procedures for analysis of water, sediment, air, and tissues. It presents information on cost and performance of each method. Presented with each method is a green profile, developed in collaboration with 25 environmental methods experts from five regulatory agencies and private labs. An example of this profile is shown in Figure 1 for the Environmental Protection Agency method for the determination of total water hardness by EDTA titration (similar to Experiment 12).


Figure 1. Green Profile for EPA Method 130.2: Total Hardness of Water by Titrimetry

The symbol for the green profile is simple, visual, and allows an individual to make a value judgment against the profile criteria. Here's a description of the symbol criteria:

Hazardous: A method fails this criterion if it uses chemicals in either of two important databases, the Resource Conservation and Recovery Act D, F, P, or U lists ${ }^{10}$ or the Environmental Protection Agency Toxic Release Inventory. ${ }^{11}$ About half of the methods in the NEMI database fail this criterion.

Waste Amount: A method fails this criterion if the amount of waste generated is greater than 50 grams. This 50 grams includes the mass of sample, as well as all chemicals used in the procedure, but does not include calibration standards, cleaning (unless significant amounts of chemicals are stipulated in cleaning steps), and related factors. The waste criterion is perhaps the most rigorous. When applied to 560 methods on the NEMI database, approximately $2 / 3$

[^3]failed this criterion. Failures generally were due to solvent use for organic analysis and mineral acid use for inorganics.

Corrosive: A method fails this criterion if the pH during the analysis is less than 2 or greater than 12. The failure rate for this criterion was about $20 \%$ for the NEMI methods.

PBT (Persistent, Bioaccumulative, or Toxic): A method fails this criterion if it uses chemicals considered to be persistent in the environment, bioaccumulative, or toxic as defined by the EPA Toxic Release Inventory. Only about 5\% of the NEMI methods did not meet this criterion and each of the methods that failed the PBT criterion also failed for hazard. Most commonly, these methods included lead or mercury compounds.

For the EPA water hardness method (EPA Method 130.2) illustrated in Figure 1, we see that the method is considered green by hazard and PBT criteria, but not by waste and corrosion criteria. During the analysis, the pH is less than 2 and 66 grams of waste are generated.

## Summary

Both analytical chemistry and green chemistry are based on a way of thinking about how you perform experiments. Green analytical chemistry is a convergence of these thought processes. Good analytical chemistry is inherently green chemistry.

For each experiment in this laboratory manual, a green profile is displayed. A suggested component of your report should be a discussion of why a particular experiment met or failed the individual green profile criteria. Suggest ways that the experiment may be made greener. If you follow through with this exercise, these thought processes should become increasingly natural to you. If you develop this mode of thinking so that it becomes second nature, you will be poised to take on leadership responsibilities in your generation of professional chemists.

## 1. Calibration of Volumetric Glassware



Green Profile See Section 0

An important trait of a good analyst is the ability to extract the best possible data from his or her equipment. For this purpose, it is desirable to calibrate your own volumetric glassware (burets, pipets, flasks, etc.) to measure the exact volumes delivered or contained. This experiment also promotes improved technique in handling volumetric glassware.

## Calibrating a $50-\mathrm{mL}$ Buret

This procedure tells how to construct a calibration graph such as the one below to convert the measured volume delivered by a buret to the true volume delivered at $20^{\circ} \mathrm{C}$.


1. Fill the buret with distilled water and force any air bubbles out the tip. See whether the buret drains without leaving drops on its walls. If drops are left, clean the buret with soap and water or soak it with cleaning solution. ${ }^{12}$ Adjust the meniscus to be at or slightly below 0.00 mL , and touch the buret tip to a beaker to remove the suspended drop of water. Allow the buret to stand for 5 min while you weigh a $125-\mathrm{mL}$ flask fitted with a rubber stopper. (Hold the flask with a paper towel to prevent fingerprints from changing its mass.) If the
2. Prepare cleaning solution by dissolving 36 g of ammonium peroxydisulfate, $\left(\mathrm{NH}_{4}\right)_{2} \mathrm{~S}_{2} \mathrm{O}_{8}$, in a loosely stoppered 2.2-L ("one gallon") bottle of $98 \mathrm{wt} \%$ sulfuric acid. Add ammonium peroxydisulfate every few weeks to maintain the oxidizing strength. EOSULF is an alternative cleaning solution for removing proteins and other residues from glassware in a biochemistry lab. EOSULF contains the metal binder EDTA and a sulfonate detergent. It can be safely poured down the drain. [P. L. Manske, T. M. Stimpfel, and E. L. Gershey, J. Chem. Ed. 1990, 67, A280.]
level of the liquid in the buret has changed, tighten the stopcock and repeat the procedure. Record the level of the liquid.
3. Drain approximately 10 mL of water at a rate $<20 \mathrm{~mL} / \mathrm{min}$ into the weighed flask, and cap it tightly to prevent evaporation. Allow 30 s for the film of liquid on the walls to descend before you read the buret. Estimate all readings to the nearest 0.01 mL . Weigh the flask again to determine the mass of water delivered.
4. Drain the buret from 10 to 20 mL , and measure the mass of water delivered. Repeat the procedure for 30,40 , and 50 mL . Then do the entire procedure ( $10,20,30,40,50 \mathrm{~mL}$ ) a second time.
5. Use the table of water density at the end of this experiment to convert the mass of water to the volume delivered. Repeat any set of duplicate buret corrections that do not agree to within 0.04 mL . Prepare a calibration graph like the one above, showing the correction factor at each $10-\mathrm{mL}$ interval.

EXAMPLE Buret Calibration
When draining the buret at $24^{\circ} \mathrm{C}$, you observe the following values:

| Final reading | 10.01 | 10.08 mL |
| :--- | :---: | :---: |
| Initial reading | $\underline{0.03}$ | $\underline{0.04}$ |
| Difference | 9.98 | 10.04 mL |
| Mass | 9.984 | 10.056 g |
| Actual volume delivered | 10.02 | 10.09 mL |
| Correction | +0.04 | +0.05 mL |
| Average correction |  | +0.045 mL |

To calculate the actual volume delivered when 9.984 g of water is delivered at $24^{\circ} \mathrm{C}$, use the conversion factor $1.0038 \mathrm{~mL} / \mathrm{g}$ in the table of water density. We find that 9.984 g occupies $(9.984 \mathrm{~g})(1.0038 \mathrm{~mL} / \mathrm{g})=10.02 \mathrm{~mL}$. The average correction for both sets of data is +0.045 mL .

To obtain the correction for a volume greater than 10 mL , add successive masses of water collected in the flask. Suppose that the following masses were measured:

| Volume interval (mL) | Mass delivered (g) |
| :---: | :---: |
| $0.03-10.01$ | 9.984 |
| $10.01-19.90$ | 9.835 |
| $\underline{19.90-30.06}$ | $\underline{10.071}$ |
| Sum 30.03 mL | 29.890 g |

The total volume of water delivered is $(29.890 \mathrm{~g})(1.0038 \mathrm{~mL} / \mathrm{g})=30.00 \mathrm{~mL}$. Because the indicated volume is 30.03 mL , the buret correction at 30 mL is -0.03 mL .

What does this mean? Suppose that the calibration graph shown above applies to your buret. If you begin a titration at 0.04 mL and end at 29.00 mL , you would deliver 28.96 mL if the buret were perfect. The calibration graph tells you that the buret delivers 0.03 mL less than the indicated amount; so only 28.93 mL was actually delivered. To use the calibration curve, either begin all titrations near 0.00 mL or correct both the initial and the final readings. Use the calibration curve whenever you use your buret.

## Calibrating Other Glassware

Other volumetric glassware can also be calibrated by measuring the mass of water they contain or deliver. Glass transfer pipets and plastic micropipets can be calibrated by weighing the water delivered from them. A volumetric flask can be calibrated by weighing it empty and then weighing it filled to the mark with distilled water. Perform each procedure at least twice. Compare your results with the tolerances listed in tables in Chapter 2 of the textbook.

## Density of water

|  |  | Volume of $\mathbf{1} \mathbf{g}$ of water $(\mathbf{m L})$ |  |
| :--- | :--- | :--- | :--- |
| Temperature <br> $\left({ }^{\circ} \mathrm{C}\right)$ | Density <br> $(\mathrm{g} / \mathrm{mL})$ | At temperature <br> shown $^{a}$ | Corrected <br> to $\mathbf{2 0}{ }^{\circ} \mathrm{C}^{b}$ |
| 10 | 0.9997026 | 1.0014 | 1.0015 |
| 11 | 0.9996084 | 1.0015 | 1.0016 |
| 12 | 0.9995004 | 1.0016 | 1.0017 |
| 13 | 0.9993801 | 1.0017 | 1.0018 |
| 14 | 0.9992474 | 1.0018 | 1.0019 |
| 15 | 0.9991026 | 1.0020 | 1.0020 |
| 16 | 0.9989460 | 1.0021 | 1.0021 |
| 17 | 0.9987779 | 1.0023 | 1.0023 |
| 18 | 0.9985986 | 1.0025 | 1.0025 |
| 19 | 0.9984082 | 1.0027 | 1.0027 |
| 20 | 0.9982071 | 1.0029 | 1.0029 |
| 21 | 0.9979955 | 1.0031 | 1.0031 |
| 22 | 0.9977735 | 1.0033 | 1.0033 |
| 23 | 0.9975415 | 1.0035 | 1.0035 |
| 24 | 0.9972995 | 1.0038 | 1.0038 |
| 25 | 0.9970479 | 1.0040 | 1.0040 |
| 26 | 0.9967867 | 1.0043 | 1.0042 |
| 27 | 0.9965162 | 1.0046 | 1.0045 |
| 28 | 0.9962365 | 1.0048 | 1.0047 |
| 29 | 0.9959478 | 1.0051 | 1.0050 |
| 30 | 0.9956502 | 1.0054 | 1.0053 |

a. Corrected for buoyancy with Equation 2-1 in the textbook.
b. Corrected for buoyancy and expansion of borosilicate glass $\left(0.0010 \% \mathrm{~K}^{-1}\right)$

## 2. Gravimetric Determination of Calcium as $\mathrm{CaC}_{2} \mathrm{O}_{4} \cdot \mathrm{H}_{2} \mathrm{O}^{13}$



Calcium ion can be analyzed by precipitation with oxalate in basic solution to form $\mathrm{CaC}_{2} \mathrm{O}_{4} \cdot \mathrm{H}_{2} \mathrm{O}$. The precipitate is soluble in acidic solution because the oxalate anion is a weak base. Large, easily filtered, relatively pure crystals of product will be obtained if the precipitation is carried out slowly. Slow precipitation is achieved by dissolving $\mathrm{Ca}^{2+}$ and $\mathrm{C}_{2} \mathrm{O}_{4}^{2-}$ in acidic solution and gradually raising the pH by thermal decomposition of urea:


## Reagents

Ammonium oxalate solution: Make 1 L of solution containing 40 g of $\left(\mathrm{NH}_{4}\right)_{2} \mathrm{C}_{2} \mathrm{O}_{4}$ plus 25 mL of 12 M HCl . Each student will need 80 mL of this solution.
Methyl red indicator: Dissolve 20 mg of the indicator in 60 mL of ethanol and add $40 \mathrm{~mL} \mathrm{H}_{2} \mathrm{O}$. 0.1 M HCl: ( $225 \mathrm{~mL} /$ student) Dilute 8.3 mL of $37 \% \mathrm{HCl}$ up to 1 L .

Urea: $45 \mathrm{~g} /$ student.
Unknowns: Prepare 1 L of solution containing $15-18 \mathrm{~g}$ of $\mathrm{CaCO}_{3}$ plus 38 mL of 12 M HCl . Each student will need 100 mL of this solution. Alternatively, solid unknowns are available from Thorn Smith. ${ }^{2}$

## Procedure

1. Dry three medium-porosity, sintered-glass funnels for $1-2 \mathrm{~h}$ at $105^{\circ} \mathrm{C}$. Cool them in a desiccator for 30 min and weigh them. Repeat the procedure with $30-\mathrm{min}$ heating periods until successive weighings agree to within 0.3 mg . Use a paper towel or tongs, not your fingers, to handle the funnels. Alternatively, a $900-\mathrm{W}$ kitchen microwave oven dries the crucible to constant mass in two heating periods of 4 min and 2 min (with 15 min allowed for

[^4]cooldown after each cycle). ${ }^{14}$ You will need to experiment with your oven to find appropriate heating times.
2. Use a few small portions of unknown to rinse a $25-\mathrm{mL}$ transfer pipet, and discard the washings. Use a rubber bulb, not your mouth, to provide suction. Transfer exactly 25 mL of unknown to each of three 250 - to $400-\mathrm{mL}$ beakers, and dilute each with $\sim 75 \mathrm{~mL}$ of 0.1 M HCl . Add 5 drops of methyl red indicator solution to each beaker. This indicator is red below pH 4.8 and yellow above pH 6.0 .
3. Add $\sim 25 \mathrm{~mL}$ of ammonium oxalate solution to each beaker while stirring with a glass rod. Remove the rod and rinse it into the beaker with small portions of distilled water. Add $\sim 15 \mathrm{~g}$ of solid urea to each sample, cover it with a watchglass, and boil gently for $\sim 30 \mathrm{~min}$ until the indicator turns yellow.
4. Filter each hot solution through a weighed funnel, using suction (Figure 2-17 in the textbook). Add $\sim 3 \mathrm{~mL}$ of ice-cold water to the beaker, and use a rubber policeman to help transfer the remaining solid to the funnel. Repeat this procedure with small portions of icecold water until all of the precipitate has been transferred to the funnel. Finally, use two $10-\mathrm{mL}$ portions of ice-cold water to rinse each beaker, and pour the washings over the precipitate.
5. Dry the precipitate, first with aspirator suction for 1 min , then in an oven at $105^{\circ} \mathrm{C}$ for $1-2 \mathrm{~h}$. Bring each filter to constant mass. The product is somewhat hygroscopic, so only one filter at a time should be removed from the desiccator, and weighings should be done rapidly. Alternatively, the precipitate can be dried in a microwave oven once for 4 min , followed by several 2-min periods, with cooling for 15 min before weighing. This drying procedure does not remove the water of crystallization.
6. Calculate the average molarity of $\mathrm{Ca}^{2+}$ in the unknown solution or the average weight percent of Ca in the unknown solid. Report the standard deviation and relative standard deviation $(s / \bar{x}=$ standard deviation/average $)$.

[^5]
## 3. Gravimetric Determination of Iron as $\mathrm{Fe}_{2} \mathrm{O}_{3}{ }^{15}$



Green Profile See Section 0

A sample containing iron can be analyzed by precipitation of the hydrous oxide from basic solution, followed by ignition to produce $\mathrm{Fe}_{2} \mathrm{O}_{3}$ :



The gelatinous hydrous oxide can occlude impurities. Therefore, the initial precipitate is dissolved in acid and reprecipitated. Because the concentration of impurities is lower during the second precipitation, occlusion is diminished. Solid unknowns can be prepared from reagent ferrous ammonium sulfate or purchased from Thorn Smith. ${ }^{2}$

## Procedure

1. Bring three porcelain crucibles and caps to constant mass by heating to redness for 15 min over a burner (Figure 1). Cool for 30 min in a desiccator and weigh each crucible. Repeat this procedure until successive weighings agree within 0.3 mg . Be sure that all oxidizable substances on the entire surface of each crucible have burned off.


Figure 1. Positioning a crucible above a burner.

[^6]2. Accurately weigh three samples of unknown containing enough Fe to produce $\sim 0.3 \mathrm{~g}$ of $\mathrm{Fe}_{2} \mathrm{O}_{3}$. Dissolve each sample in 10 mL of 3 M HCl (with heating, if necessary). If there are insoluble impurities, filter through qualitative filter paper and wash the filter well with distilled water. Add 5 mL of $6 \mathrm{M} \mathrm{HNO}_{3}$ to the filtrate, and boil for a few minutes to ensure that all iron is oxidized to Fe (III).
3. Dilute the sample to 200 mL with distilled water and add 3 M ammonia ${ }^{16}$ with constant stirring until the solution is basic (as determined with litmus paper or pH indicator paper). Digest the precipitate by boiling for 5 min and allow the precipitate to settle.
4. Decant the supernatant liquid through coarse, ashless filter paper (Whatman 41 or Schleicher and Schuell Black Ribbon, as in Figures 2-18 and 2-19 in the textbook). Do not pour liquid higher than 1 cm from the top of the funnel. Proceed to step 5 if a reprecipitation is desired. Wash the precipitate repeatedly with hot $1 \mathrm{wt} \% \mathrm{NH}_{4} \mathrm{NO}_{3}$ until little or no $\mathrm{Cl}^{-}$is detected in the filtered supernate. (Test for $\mathrm{Cl}^{-}$by acidifying a few milliliters of filtrate with 1 mL of dilute $\mathrm{HNO}_{3}$ and adding a few drops of $0.1 \mathrm{M} \mathrm{AgNO}_{3}$. If precipitate is observed, $\mathrm{Cl}^{-}$is present.) Finally, transfer the solid to the filter with the aid of a rubber policeman and more hot liquid. Proceed to step 6 if a reprecipitation is not used.
5. Wash the gelatinous mass twice with 30 mL of boiling $1 \mathrm{wt} \%$ aqueous $\mathrm{NH}_{4} \mathrm{NO}_{3}$, decanting the supernate through the filter. Then put the filter paper back into the beaker with the precipitate, add 5 mL of 12 M HCl to dissolve the iron, and tear the filter paper into small pieces with a glass rod. Add ammonia with stirring and reprecipitate the iron. Decant through a funnel fitted with a fresh sheet of ashless filter paper. Wash the solid repeatedly with hot $1 \mathrm{wt} \% \mathrm{NH}_{4} \mathrm{NO}_{3}$ until little or no $\mathrm{Cl}^{-}$is detected in the filtered supernate. Then transfer all the solid to the filter with the aid of a rubber policeman and more hot liquid.
6. Allow the filter to drain overnight, if possible, protected from dust. Carefully lift the paper out of the funnel, fold it (Figure 2), and transfer it to a porcelain crucible that has been brought to constant mass.

[^7]

Figure 2. Folding filter paper and placing it inside a crucible for ignition. Continue folding paper so entire package fits at the bottom of the crucible. Be careful not to puncture the paper.
7. Dry the crucible cautiously with a small flame, as shown in Figure 1. The flame should be directed at the top of the container, and the lid should be off. Avoid spattering. After the filter paper and precipitate are dry, char the filter paper by increasing the flame temperature. The crucible should have free access to air to avoid reduction of iron by carbon. (The lid should be kept handy to smother the crucible if the paper inflames.) Any carbon left on the crucible or lid should be burned away by directing the burner flame at it. Use tongs to manipulate the crucible. Finally, ignite the product for 15 min with the full heat of the burner directed at the base of the crucible where the $\mathrm{Fe}_{2} \mathrm{O}_{3}$ is located.
8. Cool the crucible briefly in air and then in a desiccator for 30 min . Weigh the crucible and the lid, reignite, and bring to constant mass (within 0.3 mg ) with repeated heatings.
9. Calculate the weight percent of iron in each sample, the average, the standard deviation, and the relative standard deviation $(s / \bar{X})$.

## 4. Penny Statistics ${ }^{17}$


U.S. pennies minted after 1982 have a Zn core with a Cu overlayer. Prior to 1982, pennies were made of brass, with a uniform composition ( $95 \mathrm{wt} \% \mathrm{Cu}$ / $5 \mathrm{wt} \% \mathrm{Zn})$. In 1982, both the heavier brass coins and the lighter zinc coins were made. In this experiment, your class will weigh many coins and pool the data to answer the following questions: (1) Do pennies from different years have the same mass? (2) Do pennies from different mints have the same mass? (3) Do the masses follow a Gaussian distribution?

## Gathering Data

Each student should collect and weigh enough pennies to the nearest milligram to provide a data set for the entire class containing 300 to 500 brass coins and a similar number of zinc coins. Instructions are given for a spreadsheet, but the same operations can be carried out with a calculator. Compile all the class data in a spreadsheet. Each column should list the masses of pennies from only one calendar year. Use the spreadsheet "sort" function to sort each column so that the lightest mass is at the top of the column and the heaviest is at the bottom. (To sort a column, click on the column heading to select the entire column, go to the DATA menu, select the SORT tool, and follow the directions that come up.) There will be two columns for 1982, in which both types of coins were made. Select a year other than 1982 for which you have many coins and divide the coins into those made in Denver (with a "D" beneath the year) and those minted in Philadelphia (with no mark beneath the year).

## Discrepant Data

At the bottom of each column, compute the mean and standard deviation. Retain at least one extra digit beyond the milligram place to avoid round-off errors in your calculations.

Damaged or corroded coins may have masses different from those of the general population. Discard grossly discrepant masses lying $\geq 4$ standard deviations from the mean in any one year. (For example, if one column has an average mass of 3.000 g and a standard deviation of 0.030 g , the 4 -standard-deviation limit is $\pm(4 \times 0.030)= \pm 0.120 \mathrm{~g}$. A mass that is
17. T. H. Richardson, J. Chem. Ed. 1991, 68, 310. In a related experiment, students measure the mass of copper in the penny as a function of the year of minting: R. J. Stolzberg, J. Chem. Ed. 1998, 75, 1453.
$\leq 2.880$ or $\geq 3.120 \mathrm{~g}$ should be discarded.) After rejecting discrepant data, recompute the average and standard deviation for each column.

## Confidence Intervals and $\boldsymbol{t}$ Test

Select the two years $(\geq 1982)$ in which the zinc coins have the highest and lowest average masses. For each of the two years, compute the $95 \%$ confidence interval. Use the $t$ test to compare the two mean values at the $95 \%$ confidence level. Are the two average masses significantly different? Try the same for two years of brass coins ( $\leq 1982$ ). Try the same for the one year whose coins you segregated into those from Philadelphia and those from Denver. Do the two mints produce coins with the same mass?

## Distribution of Masses

List the masses of all pennies made in or after 1983 in a single column, sorted from lowest to highest mass. There should be at least 300 masses listed. Divide the data into $0.01-\mathrm{g}$ intervals (e.g., 2.480 to 2.489 g ) and prepare a bar graph, like that shown in Figure 1. Find the mean $(\bar{x})$, median, and standard deviation (s) for all coins in the graph. For random (Gaussian) data, only 3 out of 1000 measurements should lie outside of $\bar{x} \pm 3 s$. Indicate which bars (if any) lie beyond $\pm 3 \mathrm{~s}$. In Figure 1 two bars at the right are outside of $\bar{x} \pm 3 \mathrm{~s}$.

## Least-Squares Analysis: Do Pennies Have the Same Mass Each Year?

Prepare a graph like Figure 2 in which the ordinate ( $y$-axis) is the mass of zinc pennies minted each year since 1982 and the abscissa ( $x$-axis) is the year. For simplicity, let 1982 be year 1, 1983 be year 2, and so on. If the mass of a penny increases systematically from year to year, then the least-squares line through the data will have a positive slope. If the mass decreases, the slope will be negative. If the mass is constant, the slope will be 0 . Even if the mass is really constant, your selection of coins is random and the slope is not exactly 0 .

We want to know whether the slope is significantly different from zero. Suppose that you have data for 14 years. Enter all of the data into two columns of the least-squares spreadsheet in Figure 4-15 in the textbook. Column B $\left(x_{\mathrm{i}}\right)$ is the year (1 to 14 ) and column C $\left(y_{\mathrm{i}}\right)$ is the mass of each penny. Your table will have several hundred entries. If you are not using a


Figure 1. Distribution of penny masses from the years 1982 to 1992 measured in Dan's house by Jimmy Kusznir and Doug Harris in December 1992.
spreadsheet, just tabulate the average mass for each year. Your table will have only 14 entries. Calculate the slope ( $m$ ) and intercept (b) of the best straight line through all points and find the uncertainties in slope ( $s_{m}$ ) and intercept ( $s_{b}$ ).

Use Student's $t$ to find the $95 \%$ confidence interval for the slope:

$$
\begin{equation*}
\text { confidence interval for slope }=m \pm t s_{m} \tag{1}
\end{equation*}
$$

where Student's $t$ is for $n-2$ degrees of freedom. For example, if you have $n=300$ pennies, $n-2=298$, and it would be reasonable to use the value of $t(=1.960)$ at the bottom of the table for $n=\infty$. If the least-squares slope is $m \pm s_{m}=-2.78 \pm 0.40 \mathrm{mg} /$ year, then the $95 \%$ confidence interval is $m \pm t s_{m}=-2.78 \pm(1.960)(0.40)=-2.78 \pm 0.78 \mathrm{mg} /$ year.


Figure 2. Penny mass versus year for 612 coins. Because the slope of the least-squares line is significantly less than 0 , we conclude that the average mass of older pennies is greater than the average mass of newer pennies.

The $95 \%$ confidence interval is $-2.78 \pm 0.78=-3.56$ to $-2.00 \mathrm{mg} /$ year. We are $95 \%$ confident that the true slope is in this range and is, therefore, not 0 . We conclude that older zinc pennies are heavier than newer zinc pennies.

## Does the Distribution of Masses Follow a Gaussian Distribution?

The smooth Gaussian curve superimposed on the data in Figure 1 was calculated from the formula

$$
\begin{equation*}
y_{\text {calc }}=\frac{\text { number of coins } / 100}{s \sqrt{2 \pi}} \mathrm{e}^{-(x-\bar{x})^{2} / 2 s^{2}} \tag{2}
\end{equation*}
$$

Now we carry out a $\chi^{2}$ test (pronounced "ki squared") to see if the observed distribution (the bars in Figure 1) agrees with the Gaussian curve. The statistic $\chi^{2}$ is given by

$$
\begin{equation*}
\chi^{2}=\sum \frac{\left(y_{\mathrm{obs}}-y_{\mathrm{calc}}\right)^{2}}{y_{\mathrm{calc}}} \tag{3}
\end{equation*}
$$

where $y_{\text {obs }}$ is the height of a bar on the chart, $y_{\text {calc }}$ is the ordinate of the Gaussian curve (Equation 2), and the sum extends over all bars in the graph. Calculations for the data in Figure 1 are shown in Table 1.

Table 1. Calculation of $\chi^{2}$ for Figure 1

|  | Observed <br> number <br> of coins | Calculated <br> ordinate of <br> Gaussian curve |  |  |
| :---: | :---: | :---: | :---: | :---: |
| $(x)$ | $\left(y_{\text {obs }}\right)$ | $\left(y_{\text {calc }}\right)$ | $y_{\text {obs }}-y_{\text {calc }}$ | $\frac{\left(y_{\text {obs }}-y_{\text {calc }}\right)^{2}}{y_{\text {calc }}}$ |
| 2.415 | 3 | 1.060 | 1.940 | 3.550 |
| 2.425 | 4 | 2.566 | 1.434 | 0.801 |
| 2.435 | 1 | 5.611 | -4.611 | 3.789 |
| 2.445 | 12 | 11.083 | 0.917 | 0.076 |
| 2.455 | 18 | 19.776 | -1.776 | 0.159 |
| 2.465 | 29 | 31.875 | -2.875 | 0.259 |
| 2.475 | 31 | 46.409 | -15.409 | 5.116 |
| 2.485 | 69 | 61.039 | 7.961 | 1.038 |
| 2.495 | 75 | 72.519 | 2.481 | 0.085 |
| 2.505 | 95 | 77.829 | 17.171 | 3.788 |
| 2.515 | 83 | 75.453 | 7.547 | 0.755 |
| 2.525 | 65 | 66.077 | -1.077 | 0.176 |
| 2.535 | 48 | 52.272 | -4.272 | 0.349 |
| 2.545 | 26 | 37.354 | -11.354 | 3.451 |
| 2.555 | 24 | 24.112 | -0.112 | 0.001 |
| 2.565 | 9 | 14.060 | -5.060 | 1.821 |
| 2.575 | 10 | 7.406 | 2.594 | 0.909 |
| 2.585 | 3 | 3.524 | -0.524 | 0.078 |
| 2.595 | 4 | 1.515 | 2.485 | 4.076 |
| 2.605 | 3 | 0.588 | 2.412 | 9.894 |
| 2.615 | 1 | 0.206 | 0.794 | 3.060 |
|  |  |  | $\chi^{2}($ all 21 points $)=43.231$ |  |
|  |  | $\chi^{2}(19$ points - omitting bottom two points $)=30.277$ |  |  |

Table 2. Critical values of $\chi^{2}$ that will be exceeded in $5 \%$ of experiments*

| Degrees <br> of freedom | Critical <br> value | Degrees <br> of freedom | Critical <br> value | Degrees <br> of freedom | Critical <br> value |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 3.84 | 11 | 19.7 | 21 | 32.7 |
| 2 | 5.99 | 12 | 21.0 | 22 | 33.9 |
| 3 | 7.81 | 13 | 22.4 | 23 | 35.2 |
| 4 | 9.49 | 14 | 23.7 | 24 | 36.4 |
| 5 | 11.1 | 15 | 25.0 | 25 | 37.7 |
| 6 | 12.6 | 16 | 26.3 | 26 | 38.9 |
| 7 | 14.1 | 17 | 27.6 | 27 | 40.1 |
| 8 | 15.5 | 18 | 28.9 | 28 | 41.3 |
| 9 | 16.9 | 19 | 30.1 | 29 | 42.6 |
| 10 | 18.3 | 20 | 31.4 | 30 | 43.8 |

*Example: The value of $\chi^{2}$ from 15 observations is 17.2 . This value is less than 23.7 listed for $14(=15-1)$ degrees of freedom. Because $\chi^{2}$ does not exceed the critical value, the observed distribution is consistent with the theoretical distribution.

At the bottom of Table 1 we see that $\chi^{2}$ for all 21 bars is 43.231 . In Table 2 we find a critical value of 31.4 for 20 degrees of freedom (degrees of freedom $=$ one less than number of categories). Because $\chi^{2}$ from Equation 3 exceeds the critical value, we conclude that the distribution is not Gaussian.

It would be reasonable to omit the smallest bars at the edge of the graph from the calculation of $\chi^{2}$ because these bars contain the fewest observations but make large contributions to $\chi^{2}$. Suppose that we reject bars lying $>3$ standard deviations from the mean. This removes the two bars at the right side of Figure 1 which give the last two entries in Table 1. Omitting these two points gives $\chi^{2}=30.277$, which is still greater than the critical value of 28.9 for 18 degrees of freedom in Table 2. Our conclusion is that at the $95 \%$ confidence level the observed distribution in Figure 1 is not quite Gaussian. It is possible that exceptionally light coins are nicked and exceptionally heavy coins are dirty or corroded. You would need to inspect these coins to verify this hypothesis.

## Reporting Your Results

## Gathering data:

1. Attach a table of masses, with one column sorted by mass for each year.
2. Divide 1982 into two columns, one for light (zinc) and one for heavy (brass) pennies.
3. One year should be divided into one column from Denver and one from Philadelphia. Discrepant data:
4. List the mean $(\bar{x})$ and standard deviation (s) for each column.
5. Discard data that lie outside of $\bar{x} \pm 4 s$ and recompute $\bar{x}$ and $s$.

Confidence intervals and test:

1. For the year $\geq 1982$ with highest average mass:
$95 \%$ confidence interval $(=\bar{x} \pm t s / \sqrt{n})=$ $\qquad$
For the year $\geq 1982$ with lowest average mass:
95\% confidence interval = $\qquad$
Comparison of means with $t$-test:
$t_{\text {calculated }}=$ $\qquad$
$t_{\text {table }}=$ $\qquad$
Is the difference significant? $\qquad$
2. For the year $\leq 1982$ with highest average mass:

95\% confidence interval = $\qquad$
For the year $\leq 1982$ with lowest average mass:
95\% confidence interval = $\qquad$
Comparison of means with $t$ test:
$t_{\text {calculated }}=$ $\qquad$
$t_{\text {table }}=$ $\qquad$
Is the difference significant? $\qquad$
3. For Philadelphia versus Denver coins in one year:

Philadelphia 95\% confidence interval = $\qquad$
Denver 95\% confidence interval = $\qquad$
Comparison of means with $t$ test:
$t_{\text {calculated }}=$ $\qquad$
$t_{\text {table }}=$ $\qquad$
Is the difference significant? $\qquad$

## Gaussian distribution of masses:

Prepare a graph analogous to Figure 1 with labels showing the $\pm 3 \mathrm{~s}$ limits.
Least-squares Analysis:
Prepare a graph analogous to Figure 2 and find the least-squares slope and intercept and their standard deviations.
$m \pm s_{m}=$ $\qquad$
$t_{95} \%$ confidence $=$ $\qquad$ $t_{99} \%$ confidence $=$ $\qquad$
$95 \%$ confidence: $m \pm t s_{m}=$ $\qquad$ .

Does interval include zero? $\qquad$
$99 \%$ confidence: $m \pm t s_{m}=$ $\qquad$ .

Does interval include 0 ? $\qquad$
Is there a systematic increase or decrease of penny mass with year? $\qquad$ $\chi^{2}$ test:

Write Equation 2 for the smooth Gaussian curve that fits your bar graph.
Construct a table analogous to Table 1 to compute $\chi^{2}$ for the complete data set.
Computed value of $\chi^{2}=$ $\qquad$ Degrees of freedom $=$ $\qquad$
Critical value of $\chi^{2}=$ $\qquad$
Do the data follow a Gaussian distribution? $\qquad$
Now omit bars on the graph that are greater than 3 standard deviations away from the mean and calculate a new value of $\chi^{2}$ with the reduced data set.
Computed value of $\chi^{2}=$ $\qquad$ Degrees of freedom $=$ $\qquad$
Critical value of $\chi^{2}=$ $\qquad$
Does the reduced data set follow a Gaussian distribution? $\qquad$

## 5. Statistical Evaluation of Acid-Base Indicators ${ }^{18}$



This experiment introduces you to the use of indicators and to the statistical concepts of mean, standard deviation, $Q$ test, and $t$ test. You will compare the accuracy of different indicators in locating the end point in the titration of the base "tris" with hydrochloric acid:

```
    \(\left(\mathrm{HOCH}_{2}\right)_{3} \mathrm{CNH}_{2}+\mathrm{H}^{+} \rightarrow\left(\mathrm{HOCH}_{2}\right)_{3} \mathrm{CNH}_{3}^{+}\)
Tris(hydroxymethyl)aminomethane
    "tris"
```


## Reagents

$\sim 0.1 \mathrm{M} \mathrm{HCl}$ : Each student needs $\sim 500 \mathrm{~mL}$ of unstandardized solution, all from a single batch that will be analyzed by the whole class.

Tris: Solid, primary standard powder should be available ( $\sim 4 \mathrm{~g} /$ student).
Indicators should be available in dropper bottles:
Bromothymol blue (BB): Dissolve 0.100 g in 16.0 mL 0.0100 M NaOH and add $225 \mathrm{~mL} \mathrm{H}_{2} \mathrm{O}$
Methyl red (MR): Dissolve 20 mg in 60 mL of ethanol and add $40 \mathrm{~mL} \mathrm{H}_{2} \mathrm{O}$
Bromocresol green (BG): Dissolve 0.100 g in 14.3 mL 0.0100 M NaOH and add 225 mL
$\mathrm{H}_{2} \mathrm{O}$
Methyl orange (MO): Dissolve 10 mg in $100 \mathrm{~mL} \mathrm{H}_{2} \mathrm{O}$
Erythrosine (E): Dissolve 100 mg disodium erythrosine in $100 \mathrm{~mL} \mathrm{H}_{2} \mathrm{O}$

Color changes to use for the titration of tris with HCl are
BB: blue ( pH 7.6 ) $\rightarrow$ yellow ( pH 6.0 ) (end point is disappearance of green)
MR: yellow $(\mathrm{pH} 6.0) \rightarrow$ red $(\mathrm{pH} 4.8)$ (end point is disappearance of orange)
BG: blue ( pH 5.4 ) $\rightarrow$ yellow ( pH 3.8 ) (end point is green)
MO: yellow $(\mathrm{pH} 4.4) \rightarrow$ red $(\mathrm{pH} 3.1)$ (end point is first appearance of orange)
E: $\quad \operatorname{red}(\mathrm{pH} 3.6) \rightarrow$ orange $(\mathrm{pH} 2.2)$ (end point is first appearance of orange)

## Procedure

Each student should perform the following procedure with one indicator. Different students should be assigned different indicators so that at least four students evaluate each indicator.

[^8]1. Calculate the molecular mass of tris and the mass required to react with 35 mL of 0.10 M HCl . Weigh this much tris into a $125-\mathrm{mL}$ flask.
2. It is good practice to rinse a buret with a new solution to wash away traces of previous reagents. Wash your $50-\mathrm{mL}$ buret with three $10-\mathrm{mL}$ portions of 0.1 M HCl and discard the washings. Tilt and rotate the buret so that the liquid washes the walls, and drain the liquid through the stopcock. Then fill the buret with 0.1 M HCl to near the $0-\mathrm{mL}$ mark, allow a minute for the liquid to settle, and record the reading to the nearest 0.01 mL .
3. The first titration will be rapid, to allow you to find the approximate end point of the titration. Add $\sim 20 \mathrm{~mL}$ of HCl from the buret to the flask and swirl to dissolve the tris. Add $2-4$ drops of indicator and titrate with $\sim 1-\mathrm{mL}$ aliquots of HCl to find the end point.
4. From the first titration, calculate how much tris is required to cause each succeeding titration to require $35-40 \mathrm{~mL}$ of HCl . Weigh this much tris into a clean flask. Refill your buret to near 0 mL and record the reading. Repeat the titration in step 3, but use 1 drop at a time near the end point. When you are very near the end point, use less than a drop at a time. To do this, carefully suspend a fraction of a drop from the buret tip and touch it to the inside wall of the flask. Carefully tilt the flask so that the bulk solution overtakes the droplet and then swirl the flask to mix the solution. Record the total volume of HCl required to reach the end point to the nearest 0.01 mL . Calculate the true mass of tris with the buoyancy equation 2-1 in the textbook (density of tris $=1.327 \mathrm{~g} / \mathrm{mL}$ ). Calculate the molarity of HCl .
5. Repeat the titration to obtain at least six accurate measurements of the HCl molarity.
6. Use the Grubbs test in Section 4-6 in the textbook to decide whether any results should be discarded. Report your retained values, their mean, their standard deviation, and the relative standard deviation $(s / \bar{x})$.

## Data Analysis

Pool the data from your class to fill in Table 1, which shows two possible results. The quantity $s_{X}$ is the standard deviation of all results reported by many students. The pooled standard deviation, $s_{p}$, is derived from the standard deviations reported by each student. If two students see the end point differently, each result might be very reproducible, but the reported molarities will be different. Together, they will generate a large value of $s_{X}$ (because their results are so different), but a small value of $s_{p}$ (because each one was reproducible).

Table 1. Pooled data

|  | Number of <br> measurements <br> $(n)$ | Number of <br> students <br> $(S)$ | Mean HCl <br> molarity $(\mathrm{M})^{\mathrm{a}}$ <br> $(\bar{x})$ | $s_{X}(\mathrm{M})^{\mathrm{b}}$ |  | Relative standard <br> deviation $(\%)$ <br> $100 s_{X} / \bar{x}$ |  | $s_{p}(\mathrm{M})^{\mathrm{c}}$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Indicator | 28 | 5 | 0.09565 | 0.00225 | 2.35 | 0.00109 |  |  |
| BB | 28 |  | 0.08641 | 0.00113 | 1.31 | 0.00099 |  |  |
| MR | 29 | 4 |  |  |  |  |  |  |
| BG <br> MO <br> E |  |  |  |  |  |  |  |  |

a. Computed from all values that were not discarded with the $Q$ test.
b. $s_{X}=$ standard deviation of all $n$ measurements (degrees of freedom $=n-1$ )
c. $s_{\mathrm{p}}=$ pooled standard deviation for $S$ students (degrees of freedom $=n-S$ ). Computed with the equation

$$
s_{p}=\sqrt{\frac{s_{1}^{2}\left(n_{1}-1\right)+s_{2}^{2}\left(n_{2}-1\right)+s_{3}^{2}\left(n_{3}-1\right)+\ldots}{n-S}}
$$

where there is one term in the numerator for each student using that indicator.

Select the pair of indicators giving average HCl molarities that are farthest apart. Use the $t$ test (Equation 4-9a in the textbook) to decide whether the average molarities are significantly different from each other at the $95 \%$ confidence level. When you calculate the pooled standard deviation for Equation 4-9a, the values of $s_{1}$ and $s_{2}$ in Equation 4-10a in the textbook are the values of $s_{X}\left(\right.$ not $\left.s_{p}\right)$ in Table 1.

A condition for using Equations 4-9a and 4-10a is that the standard deviations for the two sets of measurements should not be "significantly different" from each other. The $F$ test tells us whether two standard deviations are "significantly" different from each other. $F$ is the quotient of the squares of the standard deviations:

$$
\begin{equation*}
F_{\text {calculated }}=\frac{s_{1}^{2}}{s_{2}^{2}} \tag{1}
\end{equation*}
$$

We always put the larger standard deviation in the numerator so that $F \geq 1$. If $F_{\text {calculated }}>F_{\text {table }}$ in Table 2, then the difference is significant.

Use the $F$ test in Equation 1 to decide whether or not the standard deviations for the two indicators giving the largest difference in mean HCl molarity are significantly different. If they are significantly different, use Equations 4-9b and 4-10b of the textbook for the $t$ test.

Table 2. Critical values of $F=s_{1}^{2} / s_{2}^{2}$ at $95 \%$ confidence level

| Degrees of freedom for $s_{2}$ | Degrees of freedom for $s_{1}$ |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 12 | 15 | 20 | 30 | $\infty$ |
| 2 | 19.0 | 19.2 | 19.2 | 19.3 | 19.3 | 19.4 | 19.4 | 19.4 | 19.4 | 19.4 | 19.4 | 19.4 | 19.5 | 19.5 |
| 3 | 9.55 | 9.28 | 9.12 | 9.01 | 8.94 | 8.89 | 8.84 | 8.81 | 8.79 | 8.74 | 8.70 | 8.66 | 8.62 | 8.53 |
| 4 | 6.94 | 6.59 | 6.39 | 6.26 | 6.16 | 6.09 | 6.04 | 6.00 | 5.96 | 5.91 | 5.86 | 5.80 | 5.75 | 5.63 |
| 5 | 5.79 | 5.41 | 5.19 | 5.05 | 4.95 | 4.88 | 4.82 | 4.77 | 4.74 | 4.68 | 4.62 | 4.56 | 4.50 | 4.36 |
| 6 | 5.14 | 4.76 | 4.53 | 4.39 | 4.28 | 4.21 | 4.15 | 4.10 | 4.06 | 4.00 | 3.94 | 3.87 | 3.81 | 3.67 |
| 7 | 4.74 | 4.35 | 4.12 | 3.97 | 3.87 | 3.79 | 3.73 | 3.68 | 3.64 | 3.58 | 3.51 | 3.44 | 3.38 | 3.23 |
| 8 | 4.46 | 4.07 | 3.84 | 3.69 | 3.58 | 3.50 | 3.44 | 3.39 | 3.35 | 3.28 | 3.22 | 3.15 | 3.08 | 2.93 |
| 9 | 4.26 | 3.86 | 3.63 | 3.48 | 3.37 | 3.29 | 3.23 | 3.18 | 3.14 | 3.07 | 3.01 | 2.94 | 2.86 | 2.71 |
| 10 | 4.10 | 3.71 | 3.48 | 3.33 | 3.22 | 3.14 | 3.07 | 3.02 | 2.98 | 2.91 | 2.84 | 2.77 | 2.70 | 2.54 |
| 11 | 3.98 | 3.59 | 3.36 | 3.20 | 3.10 | 3.01 | 2.95 | 2.90 | 2.85 | 2.79 | 2.72 | 2.65 | 2.57 | 2.40 |
| 12 | 3.88 | 3.49 | 3.26 | 3.11 | 3.00 | 2.91 | 2.85 | 2.80 | 2.75 | 2.69 | 2.62 | 2.54 | 2.47 | 2.30 |
| 13 | 3.81 | 3.41 | 3.18 | 3.02 | 2.92 | 2.83 | 2.77 | 2.71 | 2.67 | 2.60 | 2.53 | 2.46 | 2.38 | 2.21 |
| 14 | 3.74 | 3.34 | 3.11 | 2.96 | 2.85 | 2.76 | 2.70 | 2.65 | 2.60 | 2.53 | 2.46 | 2.39 | 2.31 | 2.13 |
| 15 | 3.68 | 3.29 | 3.06 | 2.90 | 2.79 | 2.71 | 2.64 | 2.59 | 2.54 | 2.48 | 2.40 | 2.33 | 2.25 | 2.07 |
| 16 | 3.63 | 3.24 | 3.01 | 2.85 | 2.74 | 2.66 | 2.59 | 2.54 | 2.49 | 2.42 | 2.35 | 2.28 | 2.19 | 2.01 |
| 17 | 3.59 | 3.20 | 2.96 | 2.81 | 2.70 | 2.61 | 2.55 | 2.49 | 2.45 | 2.38 | 2.31 | 2.23 | 2.15 | 1.96 |
| 18 | 3.56 | 3.16 | 2.93 | 2.77 | 2.66 | 2.58 | 2.51 | 2.46 | 2.41 | 2.34 | 2.27 | 2.19 | 2.11 | 1.92 |
| 19 | 3.52 | 3.13 | 2.90 | 2.74 | 2.63 | 2.54 | 2.48 | 2.42 | 2.38 | 2.31 | 2.23 | 2.16 | 2.07 | 1.88 |
| 20 | 3.49 | 3.10 | 2.87 | 2.71 | 2.60 | 2.51 | 2.45 | 2.39 | 2.35 | 2.28 | 2.20 | 2.12 | 2.04 | 1.84 |
| 30 | 3.32 | 2.92 | 2.69 | 2.53 | 2.42 | 2.33 | 2.27 | 2.21 | 2.16 | 2.09 | 2.01 | 1.93 | 1.84 | 1.62 |
| $\infty$ | 3.00 | 2.60 | 2.37 | 2.21 | 2.10 | 2.01 | 1.94 | 1.88 | 1.83 | 1.75 | 1.67 | 1.57 | 1.46 | 1.00 |

Select the pair of indicators giving the second most different molarities in Table 1 and use the $t$ test again to see whether or not this second pair of results is significantly different.

## Reporting Your Results

## Your Individual Data

|  | Mass of <br> tris from <br> balance $(\mathrm{g})$ | True mass <br> corrected for <br> buoyancy $(\mathrm{g})$ | HCl <br> volume <br> $(\mathrm{mL})$ | Calculated <br> HCl <br> molarity $(\mathrm{M})$ |
| :--- | :--- | :--- | :--- | :--- |
| Trial |  |  |  |  |
| 1 |  |  |  |  |
| 2 |  |  |  |  |
| 3 |  |  |  |  |
| 4 |  |  |  |  |
| 5 |  |  |  |  |
| 6 |  |  |  |  |

On the basis of the $Q$ test, should any molarity be discarded? If so, which one? $\qquad$
Mean value of retained results: $\qquad$
Standard deviation: $\qquad$
Relative standard deviation (\%): $\qquad$
Pooled Class Data

1. Attach your copy of Table 1 with all entries filled in.
2. Compare the two most different molarities in Table 1. (Show your $F$ and $t$ tests and state your conclusion.)
3. Compare the two second most different molarities in Table 1.

## 6. Preparing Standard Acid and Base



Hydrochloric acid and sodium hydroxide are the most common strong acids and bases used in the laboratory. Both reagents need to be standardized to learn their exact concentrations. Section 11-7 in the textbook provides background information for the procedures described below. Unknown samples of sodium carbonate or potassium hydrogen phthalate (available from Thorn Smith ${ }^{2}$ can be analyzed by the procedures described in this section.

## Reagents

$50 \mathrm{wt} \% \mathrm{NaOH}: \quad$ ( $3 \mathrm{~mL} /$ student) Dissolve 50 g of reagent-grade NaOH in 50 mL of distilled water and allow the suspension to settle overnight. $\mathrm{Na}_{2} \mathrm{CO}_{3}$ is insoluble in the solution and precipitates. Store the solution in a tightly sealed polyethylene bottle and handle it gently to avoid stirring the precipitate when liquid is withdrawn.

Phenolphthalein indicator: Dissolve 50 mg in 50 mL of ethanol and add 50 mL of distilled water.

Bromocresol green indicator: Dissolve 100 mg in 14.3 mL of 0.01 M NaOH and add 225 mL distilled water.

Concentrated (37 wt\%) HCl: $10 \mathrm{~mL} /$ student.
Primary standards: Potassium hydrogen phthalate ( $\sim 2.5 \mathrm{~g} /$ student) and sodium carbonate ( $\sim 1.0 \mathrm{~g} /$ student).
$0.05 \mathrm{M} \mathrm{NaCl}: 50 \mathrm{~mL} /$ student.

## Standardizing NaOH

1. Dry primary standard grade potassium hydrogen phthalate for 1 h at $105^{\circ} \mathrm{C}$ and store it in a capped bottle in a desiccator.


Potassium hydrogen phthalate FM 204.22
2. Boil 1 L of distilled water for 5 min to expel $\mathrm{CO}_{2}$. Pour the water into a polyethylene bottle, which should be tightly capped whenever possible. Calculate the volume of $50 \mathrm{wt} \% \mathrm{NaOH}$ needed to prepare 1 L of 0.1 M NaOH . (The density of $50 \mathrm{wt} \%$ NaOH is 1.50 g per milliliter of solution.) Use a graduated cylinder to transfer this much NaOH to the bottle of water. (CAUTION: $50 \mathrm{wt} \% \mathrm{NaOH}$ eats people. Flood any spills on your skin with water.) Mix well and cool the solution to room temperature (preferably overnight).
3. Weigh four samples of solid potassium hydrogen phthalate and dissolve each in $\sim 25$ mL of distilled water in a $125-\mathrm{mL}$ flask. Each sample should contain enough solid to react with $\sim 25 \mathrm{~mL}$ of 0.1 M NaOH . Add 3 drops of phenolphthalein to each flask and titrate one rapidly to find the end point. The buret should have a loosely fitted cap to minimize entry of $\mathrm{CO}_{2}$ from the air.
4. Calculate the volume of NaOH required for each of the other three samples and titrate them carefully. During each titration, periodically tilt and rotate the flask to wash all liquid from the walls into the bulk solution. Near the end, deliver less than 1 drop of titrant at a time. To do so, carefully suspend a fraction of a drop from the buret tip, touch it to the inside wall of the flask, wash it into the bulk solution by careful tilting, and swirl the solution. The end point is the first appearance of faint pink color that persists for 15 s . (The color will slowly fade as $\mathrm{CO}_{2}$ from the air dissolves in the solution.)
5. Calculate the average molarity $(\bar{x})$, the standard deviation (s), and the percent relative standard deviation $(=100 \times s / \bar{x})$. If you were careful, the relative standard deviation should be $<0.2 \%$.

## Standardizing HCl

1. Use the table inside the cover of the textbook to calculate the volume of $\sim 37 \mathrm{wt} \%$ HCl that should be added to 1 L of distilled water to produce 0.1 M HCl and prepare this solution.
2. Dry primary standard grade sodium carbonate for 1 h at $105^{\circ} \mathrm{C}$ and cool it in a desiccator.
3. Weigh four samples, each containing enough $\mathrm{Na}_{2} \mathrm{CO}_{3}$ to react with $\sim 25 \mathrm{~mL}$ of 0.1 M HCl and place each in a $125-\mathrm{mL}$ flask. When you are ready to titrate each one, dissolve it in $\sim 25 \mathrm{~mL}$ of distilled water. Add 3 drops of bromocresol green indicator and titrate one rapidly to a green color to find the approximate end point.

$$
2 \mathrm{HCl}+\underset{\text { FM } 105.99}{\mathrm{Na}_{2} \mathrm{CO}_{3}} \rightarrow \mathrm{CO}_{2}+2 \mathrm{NaCl}+\mathrm{H}_{2} \mathrm{O}
$$

4. Carefully titrate each sample until it turns from blue into green. Then boil the solution to expel $\mathrm{CO}_{2}$. The color should return to blue. Carefully add HCl from the buret until the solution turns green again and report the volume of acid at this point.
5. Perform one blank titration of 50 mL of 0.05 M NaCl containing 3 drops of indicator. Subtract the volume of HCl needed for the blank from that required to titrate $\mathrm{Na}_{2} \mathrm{CO}_{3}$.
6. Calculate the mean HCl molarity, standard deviation, and percent relative standard deviation.

## 7. Using a pH Electrode for an Acid-Base Titration



In this experiment you will use a pH electrode to follow the course of an acid-base titration. You will observe how pH changes slowly during most of the reaction and rapidly near the equivalence point. You will compute the first and second derivatives of the titration curve to locate the end point. From the mass of unknown acid or base and the moles of titrant, you can calculate the molecular mass of the unknown. Section 11-5 of the textbook provides background for this experiment. Experiment 10 teaches you how to use Excel SOLVER to fit a theoretical titration curve to the data obtained in Experiment 7.

## Reagents

Standard 0.1 M NaOH and standard 0.1 M HCl : From Experiment 6.
Bromocresol green indicator: Dissolve 0.100 g of the indicator in 14.3 mL 0.0100 M NaOH and add $225 \mathrm{~mL} \mathrm{H}_{2} \mathrm{O}$.

Phenolphthalein indicator: Dissolve 50 mg of the indicator in 50 mL of ethanol and add $50 \mathrm{~mL} \mathrm{H} \mathrm{H}_{2} \mathrm{O}$.
pH calibration buffers: pH 7 and pH 4 . Use commercial standards.
Unknowns: Unknowns should be stored in a desiccator by your instructor.
Suggested acid unknowns: potassium hydrogen phthalate (Table 10-4, FM 204.22), 2-( $N$-morpholino)ethanesulfonic acid (MES, Table 8-2, FM 195.24), imidazole hydrochloride (Table 8-2, FM 104.54, hygroscopic), potassium hydrogen iodate (Table 10-4, FM 389.91).
Suggested base unknowns: tris (Table 10-4, FM 121.14), imidazole (FM 68.08), disodium hydrogen phosphate $\left(\mathrm{Na}_{2} \mathrm{HPO}_{4}, \mathrm{FM} 141.96\right)$, sodium glycinate (may be found in chemical catalogs as glycine, sodium salt hydrate, $\mathrm{H}_{2} \mathrm{NCH}_{2} \mathrm{CO}_{2} \mathrm{Na} \cdot \mathrm{xH}_{2} \mathrm{O}$, FM $97.05+x(18.015)$ ). For sodium glycinate, one objective of the titration is to find the number of waters of hydration from the molecular mass.

## Procedure

1. Your instructor will recommend a mass of unknown (5-8 mmol) for you to weigh
accurately and dissolve in distilled water in a $250-\mathrm{mL}$ volumetric flask. Dilute to the mark and mix well.
2. Following instructions for your particular pH meter, calibrate a meter and glass electrode, using buffers with pH values near 7 and 4 . Rinse the electrode well with distilled water and blot it dry with a tissue before immersing in any new solution.
3. The first titration is intended to be rough, so that you will know the approximate end point in the next titration. For the rough titration, pipet 25.0 mL of unknown into a $125-\mathrm{mL}$ flask. If you are titrating an unknown acid, add 3 drops of phenolphthalein indicator and titrate with standard 0.1 M NaOH to the pink end point, using a $50-\mathrm{mL}$ buret. If you are titrating an unknown base, add 3 drops of bromocresol green indicator and titrate with standard 0.1 M HCl to the green end point. Add 0.5 mL of titrant at a time so that you can estimate the equivalence volume to within 0.5 mL . Near the end point, the indicator temporarily changes color as titrant is added. If you recognize this, you can slow down the rate of addition and estimate the end point to within a few drops.
4. Now comes the careful titration. Pipet 100.0 mL of unknown solution into a $250-\mathrm{mL}$ beaker containing a magnetic stirring bar. Position the electrode in the liquid so that the stirring bar will not strike the electrode. If a combination electrode is used, the small hole near the bottom on the side must be immersed in the solution. This hole is the salt bridge to the reference electrode. Allow the electrode to equilibrate for 1 min with stirring and record the pH .
5. Add 1 drop of indicator and begin the titration. The equivalence volume will be four times greater than it was in step 3. Add $\sim 1.5-\mathrm{mL}$ aliquots of titrant and record the exact volume, the pH , and the color 30 s after each addition. When you are within 2 mL of the equivalence point, add titrant in 2-drop increments. When you are within 1 mL , add titrant in 1-drop increments. Continue with 1-drop increments until you are 0.5 mL past the equivalence point. The equivalence point has the most rapid change in pH . Add five more $1.5-\mathrm{mL}$ aliquots of titrant and record the pH after each.


Figure 1. Locating the maximum position of the first derivative of a titration curve.

## Data Analysis

1. Construct a graph of pH versus titrant volume. Mark on your graph where the indicator color change(s) was observed.
2. Following the example in Figures 11-5 and 11-6 of the textbook, compute the first derivative (the slope, $\Delta \mathrm{pH} / \Delta \mathrm{V}$ ) for each data point within $\pm 1 \mathrm{~mL}$ of the equivalence volume. From your graph, estimate the equivalence volume as accurately as you can, as shown in Figure 1.
3. Following the example in Figure 11-6, compute the second derivative (the slope of the slope, $\Delta($ slope $) / \Delta V)$. Prepare a graph like Figure 11-7 in the textbook and locate the equivalence volume as accurately as you can.
4. Go back to your graph from step 1 and mark where the indicator color changes were observed. Compare the indicator end point to the end point estimated from the first and second derivatives.
5. From the equivalence volume and the mass of unknown, calculate the molecular mass of the unknown.

## 8. Analysis of a Mixture of Carbonate and Bicarbonate



This procedure involves two titrations. First, total alkalinity (= $\left.\left[\mathrm{HCO}_{3}^{-}\right)\right]+2\left[\mathrm{CO}_{3}^{2-}\right]$ ) is measured by titrating the mixture with standard HCl to a bromocresol green end point:

$$
\begin{aligned}
\mathrm{HCO}_{3}^{-}+\mathrm{H}^{+} & \rightarrow \mathrm{H}_{2} \mathrm{CO}_{3} \\
\mathrm{CO}_{3}^{2-}+2 \mathrm{H}^{+} & \rightarrow \mathrm{H}_{2} \mathrm{CO}_{3}
\end{aligned}
$$

A separate aliquot of unknown is treated with excess standard NaOH to convert $\mathrm{HCO}_{3}^{-}$to $\mathrm{CO}_{3}^{2-}$ :

$$
\mathrm{HCO}_{3}^{-}+\mathrm{OH}^{-} \rightarrow \mathrm{CO}_{3}^{2-}+\mathrm{H}_{2} \mathrm{O}
$$

Then all the carbonate is precipitated with $\mathrm{BaCl}_{2}$ :

$$
\mathrm{Ba}^{2+}+\mathrm{CO}_{3}^{2-} \rightarrow \mathrm{BaCO}_{3}(s)
$$

The excess NaOH is immediately titrated with standard HCl to determine how much $\mathrm{HCO}_{3}^{-}$was present. From the total alkalinity and bicarbonate concentration, you can calculate the original carbonate concentration.

## Reagents

Standard 0.1 M NaOH and standard 0.1 M HCl: From Experiment 6 .
$\mathrm{CO}_{2}$-free water: Boil 500 mL of distilled water to expel $\mathrm{CO}_{2}$ and pour the water into a $500-\mathrm{mL}$ plastic bottle. Screw the cap on tightly and allow the water to cool to room temperature.
Keep tightly capped when not in use.
10 wt\% aqueous $\mathrm{BaCl}_{2}$ : $35 \mathrm{~mL} /$ student.
Bromocresol green and phenolphthalein indicators: See Experiment 7 for recipes.
Unknowns: Solid unknowns ( $2.5 \mathrm{~g} /$ student) can be prepared from reagent-grade sodium carbonate or potassium carbonate and bicarbonate. Unknowns should be stored in a desiccator and should not be heated. Heating at $50^{\circ}-100^{\circ} \mathrm{C}$ converts $\mathrm{NaHCO}_{3}$ to $\mathrm{Na}_{2} \mathrm{CO}_{3}$.

## Procedure

1. Accurately weigh $2.0-2.5 \mathrm{~g}$ of unknown into a $250-\mathrm{mL}$ volumetric flask by weighing the sample in a capped weighing bottle, delivering some to a funnel in the volumetric flask, and reweighing the bottle. Continue this process until the desired mass of reagent has been transferred to the funnel. Rinse the funnel repeatedly with small portions of $\mathrm{CO}_{2}$-free water to dissolve the sample. Remove the funnel, dilute to the mark, and mix well.
2. Total alkalinity: Pipet a $25.00-\mathrm{mL}$ aliquot of unknown solution into a $250-\mathrm{mL}$ flask and titrate with standard 0.1 M HCl , using bromocresol green indicator as in Experiment 6 for standardizing HCl . Repeat this procedure with two more $25.00-\mathrm{mL}$ aliquots.
3. Bicarbonate content: Pipet 25.00 mL of unknown and 50.00 mL of standard 0.1 M NaOH into a $250-\mathrm{mL}$ flask. Swirl and add 10 mL of $10 \mathrm{wt} \% \mathrm{BaCl}_{2}$, using a graduated cylinder. Swirl again to precipitate $\mathrm{BaCO}_{3}$, add 2 drops of phenolphthalein indicator, and immediately titrate with standard 0.1 M HCl . Repeat this procedure with two more $25.00-\mathrm{mL}$ samples of unknown.
4. From the results of step 2, calculate the total alkalinity and its standard deviation. From the results of step 3, calculate the bicarbonate concentration and its standard deviation. Using the standard deviations as estimates of uncertainty, calculate the concentration (and uncertainty) of carbonate in the sample. Express the composition of the solid unknown in a form such as $63.4( \pm 0.5) \mathrm{wt} \% \mathrm{~K}_{2} \mathrm{CO}_{3}$ and $36.6( \pm 0.2) \mathrm{wt} \% \mathrm{NaHCO}_{3}$.

## 9. Analysis of an Acid-Base Titration Curve: The Gran Plot



In this experiment, you will titrate a sample of pure potassium hydrogen phthalate (Table $10-4$ ) with standard NaOH . A Gran plot will be used to find the equivalence point and $K_{\mathrm{a}}$. Activity coefficients are used in the calculations of this experiment.

## Using a Gran Plot to Find the End Point of a Titration

A problem with using derivatives to find the end point of a titration is that titration data are least accurate right near the end point because buffering is minimal and electrode response is sluggish. A Gran plot uses data from before the end point (typically from $0.8 V_{\mathrm{e}}$ or $0.9 V_{\mathrm{e}}$ up to $V_{\mathrm{e}}$ ) to locate the end point.

Consider the titration of a weak acid, HA:

$$
\begin{equation*}
\mathrm{HA} \rightleftharpoons \mathrm{H}^{+}+\mathrm{A}^{-} \quad K_{\mathrm{a}}=\frac{\left[\mathrm{H}^{+}\right] \gamma_{\mathrm{H}^{+}}\left[\mathrm{A}^{-}\right] \gamma_{\mathrm{A}^{-}}}{[\mathrm{HA}] \gamma_{\mathrm{HA}}} \tag{1}
\end{equation*}
$$

It will be necessary to include activity coefficients in this discussion because a pH electrode responds to hydrogen ion activity, not concentration.

At any point between the initial point and the end point of the titration, it is usually a good approximation to say that each mole of NaOH converts 1 mol of HA into 1 mol of $\mathrm{A}^{-}$. If we have titrated $V_{\mathrm{a}} \mathrm{mL}$ of HA (whose formal concentration is $\mathrm{F}_{\mathrm{a}}$ ) with $V_{\mathrm{b}} \mathrm{mL}$ of NaOH (whose formal concentration is $\mathrm{F}_{\mathrm{b}}$ ), we can write

$$
\begin{array}{r}
{\left[\mathrm{A}^{-}\right]=\frac{\text { moles of } \mathrm{OH}^{-} \text {delivered }}{\text { total volume }}=\frac{V_{\mathrm{b}} \mathrm{~F}_{\mathrm{b}}}{V_{\mathrm{b}}+V_{\mathrm{a}}}} \\
{[\mathrm{HA}]=\frac{\text { original moles of } \mathrm{HA}-\text { moles of } \mathrm{OH}^{-}}{\text {total volume }}=\frac{V_{\mathrm{a}} \mathrm{~F}_{\mathrm{a}}-V_{\mathrm{b}} \mathrm{~F}_{\mathrm{b}}}{V_{\mathrm{a}}+V_{\mathrm{b}}}}
\end{array}
$$

Substitution of these values of $\left[\mathrm{A}^{-}\right]$and $[\mathrm{HA}]$ into the equilibrium constant gives

$$
K_{\mathrm{a}}=\frac{\left[\mathrm{H}^{+}\right] \gamma_{\mathrm{H}}+V_{\mathrm{b}} \mathrm{~F}_{\mathrm{b}} \gamma_{\mathrm{A}^{-}}}{\left(V_{\mathrm{a}} \mathrm{~F}_{\mathrm{a}}-V_{\mathrm{b}} \mathrm{~F}_{\mathrm{b}}\right) \gamma_{\mathrm{HA}}}
$$

which can be rearranged to

$$
\begin{equation*}
V_{\mathrm{b}}[\underbrace{\left.\mathrm{H}^{+}\right] \gamma_{\mathrm{H}^{+}}}_{10-\mathrm{pH}}=\frac{\gamma_{\mathrm{HA}}}{\gamma_{\mathrm{A}^{-}}} K_{\mathrm{a}}\left(\frac{V_{\mathrm{a}} \mathrm{~F}_{\mathrm{a}}-V_{\mathrm{b}} \mathrm{~F}_{\mathrm{b}}}{\mathrm{~F}_{\mathrm{b}}}\right) \tag{2}
\end{equation*}
$$

The term on the left is $V_{\mathrm{b}} \cdot 10-\mathrm{pH}$, because $\left[\mathrm{H}^{+}\right] \gamma_{\mathrm{H}^{+}}=10-\mathrm{pH}$. The term in parentheses on the right is

$$
\frac{V_{\mathrm{a}} \mathrm{~F}_{\mathrm{a}}-V_{\mathrm{b}} \mathrm{~F}_{\mathrm{b}}}{\mathrm{~F}_{\mathrm{b}}}=\frac{V_{\mathrm{a}} \mathrm{~F}_{\mathrm{a}}}{\mathrm{~F}_{\mathrm{b}}}-V_{\mathrm{b}}=V_{\mathrm{e}}-V_{\mathrm{b}}
$$

Equation 2 can, therefore, be written in the form
Gran plot equation: $\quad V_{\mathrm{b}} \cdot 10-\mathrm{pH}=\frac{\gamma_{\mathrm{HA}}}{\gamma_{\mathrm{A}^{-}}} K_{\mathrm{a}}\left(V_{\mathrm{e}}-V_{\mathrm{b}}\right)$
A graph of $V_{\mathrm{b}} \cdot 10^{-\mathrm{pH}}$ versus $V_{\mathrm{b}}$ is called a Gran plot. If $\gamma_{\mathrm{HA}} / \gamma_{\mathrm{A}^{-}}$is constant, the graph is a straight line with a slope of $-K_{\mathrm{a}} \gamma_{\mathrm{HA}} / \gamma_{\mathrm{A}^{-}}$and an $x$-intercept of $V_{\mathrm{e}}$. Figure 1 shows a Gran plot for the titration in Figure 11-5 of the textbook. Any units can be used for $V_{b}$, but the same units should be used on both axes. In Figure 1, $V_{\mathrm{b}}$ is expressed in microliters on both axes.


The beauty of a Gran plot is that it enables us to use data taken before the end point to find the end point. The slope of the Gran plot enables us to find $K_{\mathrm{a}}$. Although we derived the Gran function for a monoprotic acid, the same plot $\left(V_{\mathrm{b}} \cdot 10-\mathrm{pH}\right.$ versus $\left.V_{\mathrm{b}}\right)$ applies to polyprotic acids (such as $\mathrm{H}_{6} \mathrm{~A}$ in Figure 11-5 of the textbook).

The Gran function, $V_{\mathrm{b}} \cdot 10-\mathrm{pH}$, does not actually go to 0 , because $10-\mathrm{pH}$ is never 0 . The curve must be extrapolated to find $V_{\mathrm{e}}$. The reason the function does not reach 0 is that we have used the approximation that every mole of $\mathrm{OH}^{-}$generates $1 \mathrm{~mol}^{-}$of $\mathrm{A}^{-}$, which is not true as $V_{\mathrm{b}}$ approaches $V_{\mathrm{e}}$. Only the linear portion of the Gran plot is used.

Another source of curvature in the Gran plot is changing ionic strength, which causes $\gamma_{\mathrm{HA}} / \gamma_{\mathrm{A}^{-}}$to vary. In Figure 11-5 of the textbook, this variation was avoided by maintaining nearly constant ionic strength with $\mathrm{NaNO}_{3}$. Even without added salt, the last $10-20 \%$ of data before $V_{\mathrm{e}}$ gives a fairly straight line because the quotient $\gamma_{\mathrm{HA}} / \gamma_{\mathrm{A}}$ - does not change very much. The Gran plot in the acidic region gives accurate results even if there is $\mathrm{CO}_{2}$ dissolved in the strong base titrant. The Gran plot in the basic region can be used to measure $\mathrm{CO}_{2}$ in the strong base.

For completeness, we note that if weak base, B , is titrated with a strong acid, the Gran function is

$$
\begin{equation*}
V_{\mathrm{a}} \cdot 10^{+\mathrm{pH}}=\left(\frac{1}{K_{\mathrm{a}}} \cdot \frac{\gamma_{\mathrm{B}}}{\gamma_{\mathrm{BH}^{+}}}\right)\left(V_{\mathrm{e}}-V_{\mathrm{a}}\right) \tag{4}
\end{equation*}
$$

where $V_{\mathrm{a}}$ is the volume of strong acid and $K_{\mathrm{a}}$ is the acid dissociation constant of $\mathrm{BH}^{+}$. A graph of $V_{\mathrm{a}} \cdot 10^{+\mathrm{pH}}$ versus $V_{\mathrm{a}}$ should be a straight line with a slope of $-\gamma_{\mathrm{B}} /\left(\gamma_{\mathrm{BH}}+K_{\mathrm{a}}\right)$ and an $x$-intercept of $V_{\mathrm{e}}$.

## Procedure (An Easy Matter)

1. Dry about 1.5 g of potassium hydrogen phthalate at $105^{\circ} \mathrm{C}$ for 1 h and cool it in a desiccator for 20 min . Accurately weigh out $\sim 1.5 \mathrm{~g}$ and dissolve it in water in a $250-\mathrm{mL}$ volumetric flask. Dilute to the mark and mix well.
2. Following the instructions for your particular pH meter, calibrate a meter and glass electrode using buffers with pH values near 7 and 4 . Rinse the electrode well with distilled water and blot it dry with a tissue before immersing in a solution.
3. Pipet 100.0 mL of phthalate solution into a $250-\mathrm{mL}$ beaker containing a magnetic stirring bar. Position the electrode in the liquid so that the stirring bar will not strike the electrode. The small hole near the bottom on the side of the combination pH electrode must be immersed in the solution. This hole is the reference electrode salt bridge. Allow the electrode to equilibrate for 1 min (with stirring) and record the pH .
4. Add 1 drop of phenolphthalein indicator (recipe in Experiment 7) and titrate the solution with standard $\sim 0.1 \mathrm{M} \mathrm{NaOH}$. Until you are within 4 mL of the theoretical equivalence point, add base in $\sim 1.5-\mathrm{mL}$ aliquots, recording the volume and pH 30 s after each addition. Thereafter, use $0.4-\mathrm{mL}$ aliquots until you are within 1 mL of the equivalence point. After that, add base 1 drop at a time until you have passed the pink end point by a few tenths of a milliliter. (Record the volume at which the pink color is observed.) Then add five more $1-\mathrm{mL}$ aliquots.
5. Construct a graph of pH versus $V_{\mathrm{b}}$ (volume of added base). Locate the equivalence volume $\left(V_{\mathrm{e}}\right)$ as the point of maximum slope or zero second derivative, as described in Section 10-5. Compare this with the theoretical and phenolphthalein end points.

## Calculations (The Work Begins!)

1. Construct a Gran plot (a graph of $V_{\mathrm{b}} 10-\mathrm{pH}$ versus $V_{\mathrm{b}}$ ) by using the data collected between $0.9 V_{\mathrm{e}}$ and $V_{\mathrm{e}}$. Draw a line through the linear portion of this curve and extrapolate it to the abscissa to find $V_{\mathrm{e}}$. Use this value of $V_{\mathrm{e}}$ in the calculations below. Compare this value with those found with phenolphthalein and estimated from the graph of pH versus $V_{\mathrm{b}}$.
2. Compute the slope of the Gran plot and use Equation 3 to find $K_{\mathrm{a}}$ for potassium hydrogen phthalate as follows: The slope of the Gran plot is $-K_{\mathrm{a}} \gamma_{\mathrm{HA}} / \gamma_{\mathrm{A}^{-}}=-K_{\mathrm{a}} \gamma_{\mathrm{HP}^{-}} / \gamma_{\mathrm{P}^{2}-.}$ In this equation, HP- is monohydrogen phthalate (the weak acid) and $\mathrm{P}^{2-}$ is phthalate anion (the weak base). Because the ionic strength changes slightly as the titration proceeds, so also do the activity coefficients. Calculate the ionic strength at $0.95 V_{\mathrm{e}}$, and use this "average" ionic strength to find the activity coefficients.

## EXAMPLE Calculating Activity Coefficients

Find $\gamma_{\mathrm{HP}^{-}}$and $\gamma_{\mathrm{P}^{2-}}$ at $0.95 V_{\mathrm{e}}$ in the titration of 100.0 mL of 0.0200 M potassium hydrogen phthalate with 0.100 M NaOH .

Solution The equivalence point is 20.0 mL , so $0.95 \mathrm{~V}_{\mathrm{e}}$, $=19.0 \mathrm{~mL}$. The concentrations of $\mathrm{H}^{+}$ and $\mathrm{OH}^{-}$are negligible compared with those of $\mathrm{K}^{+}, \mathrm{Na}^{+}, \mathrm{HP}^{-}$, and $\mathrm{P}^{2-}$, whose concentrations are

$$
\begin{aligned}
& {\left[\mathrm{K}^{+}\right]=\underbrace{\left(\frac{100 \mathrm{~mL}}{119 \mathrm{~mL}}\right)}_{\begin{array}{c}
\text { Dilution } \\
\text { factor }
\end{array}} \underbrace{0.0200 \mathrm{M})}_{\begin{array}{c}
\text { Initial } \\
\text { concentration }
\end{array}}=0.0168 \mathrm{M}} \\
& {\left[\mathrm{Na}^{+}\right]=\left(\frac{19 \mathrm{~mL}}{119 \mathrm{~mL}}\right)(0.100 \mathrm{M})=0.0160 \mathrm{M}} \\
& {\left[\mathrm{HP}^{-}\right]=\underbrace{(0.050)}_{\begin{array}{c}
\text { Fraction } \\
\text { remaining }
\end{array}} \underbrace{\left[\mathrm{P}^{2-}\right]=(0.95)\left(\frac{100 \mathrm{~mL}}{119 \mathrm{~mL}}\right)(0.0200 \mathrm{M})=0.0160 \mathrm{M}}_{\left.\begin{array}{c}
\text { Dilution } \\
\text { factor } \\
1100 \mathrm{~mL}
\end{array}\right)(\underbrace{0.0200 \mathrm{M})}_{\begin{array}{c}
\text { Inital } \\
\text { concentration }
\end{array}}=0.00084 \mathrm{M}}}
\end{aligned}
$$

The ionic strength is

$$
\begin{aligned}
\mu & =\frac{1}{2} \sum_{c_{\mathrm{i}} z_{\mathrm{i}}} \\
& =\frac{1}{2}\left[(0.0168) \cdot 1^{2}+(0.0160) \cdot 1^{2}+(0.00084) \cdot 1^{2}+(0.0160) \cdot 2^{2}\right]=0.0488 \mathrm{M}
\end{aligned}
$$

To estimate $\gamma_{\mathrm{P}^{2}}$ - and $\gamma_{\mathrm{HP}}{ }^{-}$at $\mu=0.0488 \mathrm{M}$, interpolate in Table 7-1. In this table, we find that the hydrated radius of $\mathrm{P}^{2-}$ [phthalate, $\mathrm{C}_{6} \mathrm{H}_{4}\left(\mathrm{CO}_{2}^{-}\right)_{2}$ ] is 600 pm . The size of $\mathrm{HP}^{-}$is not listed, but we will suppose that it is also 600 pm . An ion with charge $\pm 2$ and a size of 600 pm has $\gamma=0.485$ at $\mu=0.05 \mathrm{M}$ and $\gamma=0.675$ at $\mu=0.01 \mathrm{M}$. Interpolating between these values, we estimate $\gamma_{\mathrm{P}}{ }^{2-}$ $=0.49$ when $\mu=0.0488 \mathrm{M}$. Similarly, we estimate $\gamma_{\mathrm{HP}^{-}}=0.84$ at this same ionic strength.
3. From the measured slope of the Gran plot and the values of $\gamma_{\mathrm{HP}^{-}}$and $\gamma_{\mathrm{P}^{2}}$, calculate $\mathrm{p} K_{\mathrm{a}}$. Then choose an experimental point near $1 / 3 V_{\mathrm{e}}$ and one near $2 / 3 V_{\mathrm{e}}$. Use Equation 1 to find $\mathrm{p} K_{\mathrm{a}}$ with each point. (You will have to calculate $\left[\mathrm{P}^{2-}\right],\left[\mathrm{HP}^{-}\right], \gamma_{\mathrm{P}^{2-}}$, and $\gamma_{\mathrm{HP}^{-}}$at each point.) Compare the average value of $\mathrm{p} K_{\mathrm{a}}$ from your experiment with $\mathrm{p} K_{2}$ for phthalic acid listed in the Appendix of the textbook.

## 10. Fitting a Titration Curve with Excel Solver ${ }^{\circledR 19}$



Excel Solver provides tremendous power for curve fitting and solving equations. Practicing scientists and engineers make frequent use of this capability, which you will never regret making the effort to learn. Study Section 11-10 of the textbook before working on this experiment.

We will fit the theoretical titration curve to the potentiometric data ( pH versus volume of titrant) that you obtained in Experiments 7 or 9. The results of your titration can be plotted in a graph such as Figure 1.


Figure 1. pH measured during the titration of acetic acid (HA) with standard NaOH . The objective of Experiment 10 is to fit a theoretical titration curve to the measured points and extract the concentration of HA and its acid dissociation constant, $K_{\mathrm{a}}$, from the data.

For the titration of a weak acid with standard NaOH

$$
\mathrm{HA}+\mathrm{NaOH} \rightarrow \mathrm{Na}^{+}+\mathrm{A}^{-}+\mathrm{H}_{2} \mathrm{O}
$$

The theoretical titration curve is described by Equation 11-13 in the textbook:

$$
\begin{align*}
& \text { Fraction of titration for } \\
& \text { weak acid by strong base: }
\end{align*} \phi=\frac{C_{\mathrm{b}} V_{\mathrm{b}}}{C_{\mathrm{a}} V_{\mathrm{a}}}=\frac{\alpha_{\mathrm{A}^{-}}-\frac{\left[\mathrm{H}^{+}\right]-\left[\mathrm{OH}^{-}\right]}{C_{\mathrm{a}}}}{1+\frac{\left[\mathrm{H}^{+}\right]-\left[\mathrm{OH}^{-}\right]}{C_{\mathrm{b}}}}
$$

where $\phi$ is the fraction of the way to the end point, $C_{\mathrm{b}}$ is the concentration of standard base, $V_{\mathrm{b}}$ is the volume of base added at a given point in the titration, $C_{\mathrm{a}}$ is the (unknown) initial concentration of weak acid, $V_{\mathrm{a}}$ is the initial volume of acid being titrated, $\alpha_{A^{-}}$is the fraction of weak acid in the form $\mathrm{A}^{-},\left[\mathrm{H}^{+}\right]$is the concentration of $\mathrm{H}^{+}$at a point in the titration, and $\left[\mathrm{OH}^{-}\right]$is

[^9]the concentration of $\mathrm{OH}^{-}$at that same point. Equation 11-13 neglects activity coefficients. The expression for $\alpha_{A-}$ is

Fraction of weak acid
in the form $A^{-}$:

$$
\alpha_{\mathrm{A}^{-}}=\frac{K_{\mathrm{a}}}{\left[\mathrm{H}^{+}\right]+K_{\mathrm{a}}}
$$

where $K_{\mathrm{a}}$ is the acid dissociation constant for HA. By finding the curve that best fits the titration data, we will find the best values of $C_{\mathrm{a}}$ and $K_{\mathrm{a}}$. You could analyze the titration of a weak base with standard HCl by modifying Equation 11-14 in the textbook for a strong acid.

## Procedure

1. Create a spreadsheet like Figure 2. Type the constants ( $C_{\mathrm{b}}, V_{\mathrm{a}}$, etc.) in cells A3:A8. Enter the known concentration of standard base in cell B3 and the initial volume of HA in cell B4. Enter 1e-14 for $K_{\mathrm{w}}$ in cell B8. Leave cells B5:B7 blank for the moment
2. Enter experimental volumes of base ( $V_{b, o b s}$ ) and pH in columns A and B (beginning in cells A12 and B12 in Figure 2). Prepare a graph of the experimental points, as in Figure 1.
3. Estimate the equivalence volume, $V_{\mathrm{e}}$. In Figure 1, the steep part of the titration curve is near $V_{\mathrm{b}}=8 \mathrm{~mL}$. In the spreadsheet, we find the steepest rise in pH between 8.01 and 8.31 mL . So we can estimate $V_{\mathrm{e}} \approx 8.1 \mathrm{~mL}$ for this example. (The equivalence point in your titration will be at some other volume of base.) From the initial volume of acid ( $V_{\mathrm{a}}=200 \mathrm{~mL}$ ) and the concentration of standard base ( $C_{b}=0.4905 \mathrm{M}$ ), we can estimate the concentration of acid:

$$
V_{\mathrm{a}} C_{\mathrm{a}}=V_{\mathrm{e}} C_{\mathrm{b}} \Rightarrow C_{\mathrm{a}}=\frac{V_{\mathrm{e}} C_{\mathrm{b}}}{V_{\mathrm{a}}} \approx \frac{(8.1 \mathrm{~mL})(0.4905 \mathrm{M})}{(200 \mathrm{~mL})}=0.0199 \mathrm{M}
$$

In Figure 2, we enter the estimated value $C_{a}=0.0199 \mathrm{M}$ in cell B 5 . You will enter the estimated value of $C_{\mathrm{a}}$ for your titration.
4. For any titration, $\mathrm{pH}=\mathrm{pK}_{\mathrm{a}}$ when $V_{\mathrm{b}}=1 / 2 V_{\mathrm{e}}$. If $V_{\mathrm{e}} \approx 8.1 \mathrm{~mL}$, then $1 / 2 V_{\mathrm{e}} \approx 4.05 \mathrm{~mL}$. Inspecting the data in the spreadsheet, we see that $\mathrm{pH} \approx 4.85$ near $V_{\mathrm{b}} \approx 4.05 \mathrm{~mL}$. In Figure 2, the estimated value of 4.85 for $\mathrm{pK}_{\mathrm{a}}$ is entered in cell B 6 . You will enter the estimated $\mathrm{pK}_{\mathrm{a}}$ for your titration. The spreadsheet calculates $K_{\mathrm{a}}=10^{-\mathrm{p} K_{\mathrm{a}}}$ in cell B7. Eventually, we will use Excel Solver to find the best values for $C_{\mathrm{a}}$ and pK a to fit the titration data.
5. Compute $\left[\mathrm{H}^{+}\right]=10^{-\mathrm{pH}}$ obs in column C and $\left[\mathrm{OH}^{-}\right]=K_{\mathrm{w}} /\left[\mathrm{H}^{+}\right]$in column D. Compute $\alpha_{\mathrm{A}^{-}}$in column E. Compute $\phi$ in column F with the ugly expression at the right side of Equation 11-13. Spreadsheet formulas are given in the upper part of Figure 2.
6. From $\phi$ in column F , calculate the volume of base, $V_{\mathrm{b}, \mathrm{calc}}$, in column $G$.

$$
\phi=\frac{C_{\mathrm{b}} V_{\mathrm{b}, \mathrm{calc}}}{C_{\mathrm{a}} V_{\mathrm{a}}} \Rightarrow V_{\mathrm{b}, \mathrm{calc}}=\frac{\phi C_{\mathrm{a}} V_{\mathrm{a}}}{C_{\mathrm{b}}}
$$

7. The calculated titration curve is a graph of observed pH versus $V_{\mathrm{b}, \text { calc. }}$. We have not yet optimized the values of $C_{\mathrm{a}}$ and $\mathrm{pK}_{\mathrm{a}}$, but we have pretty good estimates that should give a reasonable fit to the experimental data. To superimpose the calculated titration curve on the data in Figure 1, click on the graph in your spreadsheet. In Excel 2010, in the Chart Tools ribbon go to Design and then Select Data. Click Add. Name the new data "Calc". The $x$ values are $V_{\mathrm{b}, \text { calc }}$ in column G . The $y$ values are pH in column B . Click OK and the calculated points appear on the graph. To change the calculated points to a smooth curve, click on one of the calculated points so they are all highlighted. Select Chart Tools, Format, Format Selection. For Marker Options, click None to remove the markers. For Line Color, select Solid Line and give it a color. For Line Style, select a Width of 0.75 points. Click Close and you should see the smooth calculated curve.

|  | A | B | C | D | E | F | G | H | I |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | Titration of Acetic Acid with NaOH |  |  |  |  |  |  |  |  |
| 2 |  |  |  |  | $\left[\mathrm{H}^{+}\right]: \quad \mathrm{C} 11=10^{\wedge}-\mathrm{B} 11$ |  |  |  | 0.265 |
| 3 | $\mathrm{C}_{\mathrm{b}}=$ | 0.4905 | M |  | [ $\mathrm{OH}^{-}$]: D11 = \$B\$8/C11 |  |  |  | = sum(111:I42) |
| 4 | $\mathrm{V}_{\mathrm{a}}=$ | 200 | mL |  | Alpha(A) : E11 = \$B\$7/(C11+\$B\$7) |  |  |  |  |
| 5 | $\mathrm{C}_{\mathrm{a}}=$ | 0.01990 | M |  | Phi: $\mathrm{F} 11=(\mathrm{E} 11-(\mathrm{C} 11-\mathrm{D} 11) / \$ \mathrm{~B} \$ 5) /(1+(\mathrm{C} 11-\mathrm{D} 11) / \$ \mathrm{~B} \$ 3)$ |  |  |  |  |
| 6 | $\mathrm{pK}_{\mathrm{a}}=$ | 4.850 |  |  | $\mathrm{V}_{\mathrm{b}, \text { calc }}$ : $\mathrm{G} 11=\mathrm{F} 11 * \$ \mathrm{~B} \$ 5 \times \$ \mathrm{~B} 4 / \$ \mathrm{~B} \$ 3$ |  |  |  |  |
| 7 | $\mathrm{K}_{\mathrm{a}}=$ | $1.41 \mathrm{E}-05$ | $=10^{\wedge}-\mathrm{B6}$ |  | Weight: $\mathrm{H} 11=(\mathrm{B} 12-\mathrm{B} 11) /(\mathrm{A} 12-\mathrm{A} 11)$ |  |  |  |  |
| 8 | $\mathrm{K}_{\mathrm{w}}=$ | 1.00E-14 |  |  | wt ${ }^{\star}\left(\mathrm{V}_{\mathrm{b}, \text { obs }}-\mathrm{V}_{\mathrm{b}, \text { calc }}\right)^{2}: \quad 111=\mathrm{H} 11 *(\mathrm{~A} 11-\mathrm{G} 11)^{\wedge} 2$ |  |  |  |  |
| 9 |  |  |  |  |  |  |  |  |  |
| 10 | $\mathrm{V}_{\mathrm{b}, \mathrm{obs}}$ |  |  |  |  |  |  |  | wt $^{\star}$ residual ${ }^{2}=$ |
| 11 | ( mL ) | pH obs | $\left[\mathrm{H}^{+}\right]$ | [ $\mathrm{OH}^{-}$] | Alpha(A ${ }^{-}$) | Phi | $\mathrm{V}_{\mathrm{b}, \mathrm{calc}}$ | Weight | $\mathrm{wt}{ }^{\star}\left(\mathrm{V}_{\mathrm{b}, \text { obs }}-\mathrm{V}_{\mathrm{b}, \text { calc }}\right)^{2}$ |
| 12 | 0.21 | 3.48 | 3.3E-04 | 3.0E-11 | 0.041 | 0.024 | 0.20 | 0.80 | $1.39 \mathrm{E}-04$ |
| 13 | 0.51 | 3.72 | $1.9 \mathrm{E}-04$ | 5.2E-11 | 0.069 | 0.059 | 0.48 | 0.50 | 3.89E-04 |
| 14 | 0.81 | 3.87 | $1.3 \mathrm{E}-04$ | $7.4 \mathrm{E}-11$ | 0.095 | 0.088 | 0.71 | 0.47 | $4.31 \mathrm{E}-03$ |
| 15 | 1.11 | 4.01 | 9.8E-05 | $1.0 \mathrm{E}-10$ | 0.126 | 0.121 | 0.98 | 0.47 | 7.33E-03 |
| 16 | 1.41 | 4.15 | 7.1E-05 | $1.4 \mathrm{E}-10$ | 0.166 | 0.163 | 1.32 | 0.33 | $2.66 \mathrm{E}-03$ |
| 17 | 1.71 | 4.25 | 5.6E-05 | $1.8 \mathrm{E}-10$ | 0.201 | 0.198 | 1.61 | 0.33 | 3.61E-03 |
| 18 | 2.01 | 4.35 | 4.5E-05 | 2.2E-10 | 0.240 | 0.238 | 1.93 | 0.23 | $1.45 \mathrm{E}-03$ |
| 19 | 2.31 | 4.42 | 3.8E-05 | 2.6E-10 | 0.271 | 0.269 | 2.18 | 0.27 | $4.34 \mathrm{E}-03$ |
| 20 | 2.61 | 4.50 | 3.2E-05 | 3.2E-10 | 0.309 | 0.307 | 2.49 | 0.27 | $3.69 \mathrm{E}-03$ |
| 21 | 2.91 | 4.58 | 2.6E-05 | 3.8E-10 | 0.349 | 0.348 | 2.82 | 0.30 | $2.21 \mathrm{E}-03$ |
| 22 | 3.21 | 4.67 | 2.1E-05 | 4.7E-10 | 0.398 | 0.397 | 3.22 | 0.17 | $1.44 \mathrm{E}-05$ |
| 23 | 3.51 | 4.72 | $1.9 \mathrm{E}-05$ | 5.2E-10 | 0.426 | 0.425 | 3.45 | 0.20 | 8.07E-04 |
| 24 | 3.81 | 4.78 | 1.7E-05 | 6.0E-10 | 0.460 | 0.459 | 3.72 | 0.23 | $1.73 \mathrm{E}-03$ |
| 25 | 4.11 | 4.85 | $1.4 \mathrm{E}-05$ | 7.1E-10 | 0.500 | 0.499 | 4.05 | 0.23 | 8.06E-04 |
| 26 | 4.41 | 4.92 | $1.2 \mathrm{E}-05$ | 8.3E-10 | 0.540 | 0.540 | 4.38 | 0.20 | $2.01 \mathrm{E}-04$ |
| 27 | 4.71 | 4.98 | $1.0 \mathrm{E}-05$ | 9.5E-10 | 0.574 | 0.574 | 4.66 | 0.23 | $6.95 \mathrm{E}-04$ |
| 28 | 5.01 | 5.05 | 8.9E-06 | 1.1E-09 | 0.613 | 0.613 | 4.97 | 0.23 | $3.48 \mathrm{E}-04$ |
| 29 | 5.31 | 5.12 | 7.6E-06 | 1.3E-09 | 0.651 | 0.650 | 5.28 | 0.30 | $3.48 \mathrm{E}-04$ |
| 30 | 5.61 | 5.21 | 6.2E-06 | 1.6E-09 | 0.696 | 0.696 | 5.65 | 0.27 | $3.44 \mathrm{E}-04$ |
| 31 | 5.91 | 5.29 | 5.1E-06 | 1.9E-09 | 0.734 | 0.733 | 5.95 | 0.30 | $4.96 \mathrm{E}-04$ |
| 32 | 6.21 | 5.38 | 4.2E-06 | 2.4E-09 | 0.772 | 0.772 | 6.26 | 0.37 | $1.05 \mathrm{E}-03$ |
| 33 | 6.51 | 5.49 | 3.2E-06 | 3.1E-09 | 0.814 | 0.813 | 6.60 | 0.40 | $3.27 \mathrm{E}-03$ |
| 34 | 6.81 | 5.61 | 2.5E-06 | 4.1E-09 | 0.852 | 0.852 | 6.91 | 0.50 | $5.18 \mathrm{E}-03$ |
| 35 | 7.11 | 5.76 | $1.7 \mathrm{E}-06$ | 5.8E-09 | 0.890 | 0.890 | 7.22 | 0.70 | $9.18 \mathrm{E}-03$ |
| 36 | 7.41 | 5.97 | 1.1E-06 | 9.3E-09 | 0.929 | 0.929 | 7.54 | 1.03 | $1.79 \mathrm{E}-02$ |
| 37 | 7.71 | 6.28 | 5.2E-07 | 1.9E-08 | 0.964 | 0.964 | 7.82 | 3.17 | $4.06 \mathrm{E}-02$ |
| 38 | 8.01 | 7.23 | 5.9E-08 | 1.7E-07 | 0.996 | 0.996 | 8.08 | 9.70 | $4.83 \mathrm{E}-02$ |
| 39 | 8.31 | 10.14 | 7.2E-11 | 1.4E-04 | 1.000 | 1.007 | 8.17 | 2.37 | $4.46 \mathrm{E}-02$ |
| 40 | 8.61 | 10.85 | $1.4 \mathrm{E}-11$ | 7.1E-04 | 1.000 | 1.037 | 8.41 | 1.17 | $4.44 \mathrm{E}-02$ |
| 41 | 8.91 | 11.20 | 6.3E-12 | 1.6E-03 | 1.000 | 1.083 | 8.79 | 0.63 | $9.30 \mathrm{E}-03$ |
| 42 | 9.21 | 11.39 | 4.1E-12 | 2.5E-03 | 1.000 | 1.129 | 9.16 | 0.50 | $1.20 \mathrm{E}-03$ |
| 43 | 9.51 | 11.54 | 2.9E-12 | 3.5E-03 | 1.000 | 1.183 | 9.60 | 0.50 | $3.68 \mathrm{E}-03$ |

Figure 2. Initial spreadsheet for fitting Equation 11-13 to experimental points for titration of HA with standard NaOH .

|  | A | B | C | D | E | F | G | H | I |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | Titration of Acetic Acid with NaOH |  |  |  |  |  |  |  | $\Sigma\left(w^{*}\right.$ residual $\left.{ }^{2}\right)=$ |
| 2 |  |  |  |  | $\left[\mathrm{H}^{+}\right]: \quad \mathrm{C} 11=10^{\wedge}$-B11 |  |  |  | 0.240 |
| 3 | $\mathrm{C}_{\mathrm{b}}=$ | 0.4905 | M |  | [ $\mathrm{OH}^{-}$]: $\mathrm{D} 11=\$ \mathrm{~B} \$ 8 / \mathrm{C} 11$ |  |  |  | = sum(111:I42) |
| 4 | $\mathrm{V}_{\mathrm{a}}=$ | 200 | mL |  | Alpha(A): $\mathrm{E} 11=\$ \mathrm{~B} 7 /(\mathrm{C} 11+\$ \mathrm{~B} 7$ ) |  |  |  |  |
| 5 | $\mathrm{C}_{\mathrm{a}}=$ | 0.01981 | M |  | Phi: F11 = (E11-(C11-D11)/\$B\$5)/(1+(C11-D11)/\$B\$3) |  |  |  |  |
| 6 | $\mathrm{pK}_{\mathrm{a}}=$ | 4.840 |  |  | $\mathrm{V}_{\mathrm{b}, \mathrm{calc}}$ : G11 $=\mathrm{F} 11 * \$ \mathrm{~B} \$ 5 \times \$ \mathrm{~B} 4 / \$ \mathrm{~B} \$ 3$ |  |  |  |  |
| 7 | $\mathrm{K}_{\mathrm{a}}=$ | $1.44 \mathrm{E}-05$ | $=10^{\wedge}-\mathrm{B6}$ |  | Weight: $\mathrm{H} 11=(\mathrm{B} 12-\mathrm{B} 11) /(\mathrm{A} 12-\mathrm{A} 11)$ |  |  |  |  |
| 8 | $\mathrm{K}_{\mathrm{w}}=$ | $1.00 \mathrm{E}-14$ |  |  | $\mathrm{wt}^{\star}\left(\mathrm{V}_{\mathrm{b}, \text { obs }}-\mathrm{V}_{\mathrm{b}, \text { calc }}\right)^{2}: \quad 111=\mathrm{H} 11 *(\mathrm{~A} 11-\mathrm{G} 11)^{\wedge} 2$ |  |  |  |  |
| 9 |  |  |  |  |  |  |  |  |  |
| 10 | $\mathrm{V}_{\mathrm{b}, \mathrm{obs}}$ |  |  |  |  |  |  |  | wt $^{\star}$ residual ${ }^{2}=$ |
| 11 | (mL) | pH ${ }_{\text {obs }}$ | $\left[\mathrm{H}^{+}\right]$ | [ $\mathrm{OH}^{-}$] | Alpha(A ${ }^{-}$) | Phi | $\mathrm{V}_{\mathrm{b}, \mathrm{calc}}$ | Weight | $w t^{\star}\left(V_{b, o b s}-V_{b, \text { calc }}\right)^{2}$ |
| 12 | 0.21 | 3.48 | 3.3E-04 | 3.0E-11 | 0.042 | 0.025 | 0.20 | 0.80 | 4.57E-05 |
| 13 | 0.51 | 3.72 | 1.9E-04 | 5.2E-11 | 0.070 | 0.061 | 0.49 | 0.50 | $1.76 \mathrm{E}-04$ |
| 14 | 0.81 | 3.87 | 1.3E-04 | 7.4E-11 | 0.097 | 0.090 | 0.73 | 0.47 | $3.29 \mathrm{E}-03$ |
| 15 | 1.11 | 4.01 | 9.8E-05 | 1.0E-10 | 0.129 | 0.124 | 1.00 | 0.47 | 5.64E-03 |
| 16 | 1.41 | 4.15 | 7.1E-05 | 1.4E-10 | 0.169 | 0.166 | 1.34 | 0.33 | $1.65 \mathrm{E}-03$ |
| 17 | 1.71 | 4.25 | 5.6E-05 | 1.8E-10 | 0.204 | 0.201 | 1.63 | 0.33 | $2.27 \mathrm{E}-03$ |
| 18 | 2.01 | 4.35 | 4.5E-05 | 2.2E-10 | 0.244 | 0.242 | 1.96 | 0.23 | $6.99 \mathrm{E}-04$ |
| 19 | 2.31 | 4.42 | 3.8E-05 | 2.6E-10 | 0.275 | 0.273 | 2.21 | 0.27 | $2.77 \mathrm{E}-03$ |
| 20 | 2.61 | 4.50 | 3.2E-05 | 3.2E-10 | 0.314 | 0.312 | 2.52 | 0.27 | $2.18 \mathrm{E}-03$ |
| 21 | 2.91 | 4.58 | 2.6E-05 | 3.8E-10 | 0.354 | 0.353 | 2.85 | 0.30 | 9.96E-04 |
| 22 | 3.21 | 4.67 | 2.1E-05 | 4.7E-10 | 0.403 | 0.402 | 3.25 | 0.17 | $2.39 \mathrm{E}-04$ |
| 23 | 3.51 | 4.72 | $1.9 \mathrm{E}-05$ | 5.2E-10 | 0.431 | 0.430 | 3.47 | 0.20 | $2.47 \mathrm{E}-04$ |
| 24 | 3.81 | 4.78 | $1.7 \mathrm{E}-05$ | 6.0E-10 | 0.465 | 0.464 | 3.75 | 0.23 | 7.91E-04 |
| 25 | 4.11 | 4.85 | $1.4 \mathrm{E}-05$ | 7.1E-10 | 0.506 | 0.505 | 4.08 | 0.23 | $2.41 \mathrm{E}-04$ |
| 26 | 4.41 | 4.92 | 1.2E-05 | 8.3E-10 | 0.546 | 0.545 | 4.40 | 0.20 | $9.31 \mathrm{E}-06$ |
| 27 | 4.71 | 4.98 | $1.0 \mathrm{E}-05$ | 9.5E-10 | 0.580 | 0.579 | 4.68 | 0.23 | $2.34 \mathrm{E}-04$ |
| 28 | 5.01 | 5.05 | 8.9E-06 | 1.1E-09 | 0.618 | 0.618 | 4.99 | 0.23 | $8.00 \mathrm{E}-05$ |
| 29 | 5.31 | 5.12 | 7.6E-06 | 1.3E-09 | 0.656 | 0.655 | 5.29 | 0.30 | $8.78 \mathrm{E}-05$ |
| 30 | 5.61 | 5.21 | 6.2E-06 | 1.6E-09 | 0.701 | 0.700 | 5.66 | 0.27 | 6.23E-04 |
| 31 | 5.91 | 5.29 | 5.1E-06 | 1.9E-09 | 0.738 | 0.738 | 5.96 | 0.30 | 7.15E-04 |
| 32 | 6.21 | 5.38 | 4.2E-06 | 2.4E-09 | 0.776 | 0.776 | 6.27 | 0.37 | $1.18 \mathrm{E}-03$ |
| 33 | 6.51 | 5.49 | 3.2E-06 | 3.1E-09 | 0.817 | 0.817 | 6.60 | 0.40 | $3.08 \mathrm{E}-03$ |
| 34 | 6.81 | 5.61 | 2.5E-06 | 4.1E-09 | 0.855 | 0.855 | 6.90 | 0.50 | $4.35 \mathrm{E}-03$ |
| 35 | 7.11 | 5.76 | 1.7E-06 | 5.8E-09 | 0.893 | 0.893 | 7.21 | 0.70 | 6.92E-03 |
| 36 | 7.41 | 5.97 | 1.1E-06 | 9.3E-09 | 0.931 | 0.931 | 7.52 | 1.03 | $1.24 \mathrm{E}-02$ |
| 37 | 7.71 | 6.28 | 5.2E-07 | 1.9E-08 | 0.965 | 0.965 | 7.79 | 3.17 | 2.25E-02 |
| 38 | 8.01 | 7.23 | 5.9E-08 | 1.7E-07 | 0.996 | 0.996 | 8.04 | 9.70 | $1.19 \mathrm{E}-02$ |
| 39 | 8.31 | 10.14 | 7.2E-11 | 1.4E-04 | 1.000 | 1.007 | 8.14 | 2.37 | 7.14E-02 |
| 40 | 8.61 | 10.85 | $1.4 \mathrm{E}-11$ | 7.1E-04 | 1.000 | 1.037 | 8.38 | 1.17 | $6.25 \mathrm{E}-02$ |
| 41 | 8.91 | 11.20 | 6.3E-12 | 1.6E-03 | 1.000 | 1.084 | 8.75 | 0.63 | $1.58 \mathrm{E}-02$ |
| 42 | 9.21 | 11.39 | 4.1E-12 | 2.5E-03 | 1.000 | 1.130 | 9.12 | 0.50 | $3.67 \mathrm{E}-03$ |
| 43 | 9.51 | 11.54 | 2.9E-12 | 3.5E-03 | 1.000 | 1.183 | 9.56 | 0.50 | $1.21 \mathrm{E}-03$ |

Figure 3. Spreadsheet after executing Solver to optimize the values of $C_{\mathrm{a}}$ and $\mathrm{p} K_{\mathrm{a}}$ to minimize the weighted sum of the squares of the residuals in cell I2.
8. Before finding the best values of $C_{\mathrm{a}}$ and $\mathrm{p} K_{\mathrm{a}}$ to fit the data, we are going to give each experimental point a weight in column $H$. The greater the weight, the more importance we attach to an experimental point in the least-squares fitting procedure. We could have weighted all points equally with a weight of 1 . An empirical weight that attaches more significance to points near $V_{\mathrm{e}}$ is the derivative $\Delta \mathrm{pH} / \Delta V_{\mathrm{b}, \mathrm{obs}}{ }^{20}$ For the first weight in cell H 12 , the formula is

$$
\text { weight }=\frac{\Delta \mathrm{pH}}{\Delta V_{\mathrm{b}}}=\frac{\mathrm{B} 13-\mathrm{B} 12}{\mathrm{~A} 13-\mathrm{A} 12}=\frac{3.72-3.48}{0.51-0.21}=0.80
$$

This procedure finds a weight for every point except the last one in cell H 43 , because there is no data in cells A44 and B44 with which to compute a derivative. For simplicity, assign the last weight in cell H 43 equal to the weight computed in cell H 42 .
9. In least squares curve fitting, we seek to minimize the sum of squares of the difference between an observed and a calculated quantity. In your experiment, you measured $V_{\mathrm{b}, \mathrm{obs}}$ and calculated $V_{\mathrm{b}, \mathrm{calc}}$. We want to minimize the $\operatorname{sum}\left(V_{\mathrm{b}, \mathrm{obs}}-V_{\mathrm{b}, \mathrm{calc}}\right)^{2}$. To find $V_{\mathrm{e}}$ (and, therefore $C_{\mathrm{a}}$ ) more accurately, we attach higher weights to points near $V_{\mathrm{e}}$. Therefore, we will minimize the sum $\Sigma\left[\right.$ weight $\left.*\left(V_{\mathrm{b}, \mathrm{obs}}-V_{\mathrm{b}, \mathrm{calc}}\right)^{2}\right]$. In column I of the spreadsheet compute the product weight $*\left(V_{\mathrm{b}, \mathrm{obs}}-V_{\mathrm{b}, \mathrm{calc}}\right)^{2}$ for each row. In cell I2, compute the sum of weighted squares of the residuals:

$$
\text { sum }=\Sigma\left[\text { weight } *\left(V_{\mathrm{b}, \mathrm{obs}}-V_{\mathrm{b}, \mathrm{calc}}\right)^{2}\right] \quad \Rightarrow \quad \mathrm{I} 2=\mathrm{SUM}(\mathrm{I} 12: \mathrm{I} 43)
$$

10. Now we are ready for a least-squares optimization of $C_{\mathrm{a}}$ and $\mathrm{p} K_{\mathrm{a}}$ to find the theoretical titration curve that best fits the experimental points. In Excel 2010, in the Data ribbon, select Solver. (If you don't see Solver in the Analysis section of the ribbon, click the Microsoft Office button at the top left of the spreadsheet. Click Excel Options and select Add-Ins. Highlight Solver Add-In, click OK, and Solver is loaded.) In the Data ribbon, click on Solver. In the Solver window, Set Objective \$I\$2 Equal To Min By Changing Variable Cells \$B\$5,\$B\$6.
11. The weighting function $\Delta \mathrm{pH} / \Delta V_{\mathrm{b}}$,obs is recommended by Burnett and Burns ${ }^{19}$ to improve the accuracy of finding $V_{\mathrm{e}}$ and, hence, $C_{\mathrm{a}}$. In general, the accuracy of measuring pH is poorest near $V_{\mathrm{e}}$, so it could be argued that these points should be given the least weight, not the most weight. However, points near $V_{\mathrm{e}}$ are most important for finding $V_{\mathrm{e}}$ accurately, so we weight them the highest. The Gran plot in the preceding experiment is the best way to find $V_{\mathrm{e}}$ without having to rely on less accurate data near $V_{\mathrm{e}}$.


Click the Solve button. Solver takes a few seconds to vary the quantities $C_{\mathrm{a}}$ and $\mathrm{p} K_{\mathrm{a}}$ in cells B5 and B6 to minimize the sum in cell I2. The result is shown in Figure 3. The sum in cell I2 is reduced from 0.428 in Figure 2 to 0.240 . The optimum values $C_{a}=0.01981 \mathrm{M}$ and $\mathrm{p} K_{\mathrm{a}}$ $=4.840$ appear in cells B5 and B6 in Figure 3.
11. Superimpose the optimum computed curve on your experimental points to obtain a graph like Figure 4.


Figure 4. Calculated titration curve (smooth line) superimposed on measured points after optimizing the fit with Solver.

Try different starting values of $C_{\mathrm{a}}$ and $\mathrm{p} K_{\mathrm{a}}$ in cells B 5 and B 6 to see how well Solver can optimize two parameters at once. You will find that if the initial values of $C_{\mathrm{a}}$ and $\mathrm{p} K_{\mathrm{a}}$ are not close to the correct values, Solver might not be able to find an answer. In this experiment, it was easy to find values of $C_{\mathrm{a}}$ and $\mathrm{p} K_{\mathrm{a}}$ that are close to the true values by inspection of the experimental titration data.

In case you could not find good starting estimates for $C_{\mathrm{a}}$ and $\mathrm{p} K_{\mathrm{a}}$, try to optimize one variable at a time. In the Solver window, Set Objective \$I\$2 Equal To Min By Changing Variable Cells \$B\$5. Once Solver has found the best value in cell B5, Set Objective \$I\$2 Equal To Min By Changing Variable Cells \$B\$6. With these two individually optimized values in cells B5 and B6, you can optimize them together by Set Objective \$I\$2 Equal To Min By Changing Variable Cells $\$ \mathrm{~B} \$ 5, \$ \mathrm{~B} \$ 6$.

From this exercise, turn in a graph such as Figure 4 and a spreadsheet such as Figure 3. Report the optimum values of $C_{\mathrm{a}}$ and $\mathrm{p} K_{\mathrm{a}}$ that fit your experimental data.

## 11. Kjeldahl Nitrogen Analysis



The Kjeldahl nitrogen analysis is widely used to measure the nitrogen content of pure organic compounds and complex substances such as milk, cereal, and flour. Digestion in boiling $\mathrm{H}_{2} \mathrm{SO}_{4}$ with a catalyst converts organic nitrogen into $\mathrm{NH}_{4}^{+}$. The solution is then made basic, and the liberated $\mathrm{NH}_{3}$ is distilled into a known amount of HCl (Reactions 11-9 to 11-11 in the textbook). Unreacted HCl is titrated with NaOH to determine how much HCl was consumed by $\mathrm{NH}_{3}$. Because the solution to be titrated contains both HCl and $\mathrm{NH}_{4}^{+}$, we choose an indicator that permits titration of HCl without beginning to titrate $\mathrm{NH}_{4}^{+}$. Bromocresol green, with a transition range of pH 3.8 to 5.4 , fulfills this purpose.

The Kjeldahl digestion captures amine $\left(-\mathrm{NR}_{2}\right)$ or amide $\left(-\mathrm{C}[=\mathrm{O}] \mathrm{NR}_{2}\right)$ nitrogens (where R can be H or an organic group), but not oxidized nitrogen such as nitro $\left(-\mathrm{NO}_{2}\right)$ or azo $(-\mathrm{N}=\mathrm{N}-)$ groups, which must be reduced first to amines or amides.

## Reagents

Standard NaOH and standard HCl: From Experiment 6.
Bromocresol green and phenolphthalein indicators: Recipes in Experiment 7.
Potassium sulfate: $10 \mathrm{~g} /$ student.
Selenium-coated boiling chips: Hengar selenium-coated granules are convenient. Alternative catalysts are 0.1 g of $\mathrm{Se}, 0.2 \mathrm{~g}$ of $\mathrm{CuSeO}_{3}$, or a crystal of CuSO 4 .

Concentrated (98 wt\%) $\mathrm{H}_{2} \mathrm{SO}_{4}: 25 \mathrm{~mL} /$ student.
Unknowns: Unknowns are pure acetanilide, $N$-2-hydroxyethylpiperazine- $N$ '-2-ethanesulfonic acid (HEPES buffer, Table 8-2 in the textbook), tris(hydroxymethyl)aminomethane (tris buffer, Table 8-2), or the $p$-toluenesulfonic acid salts of ammonia, glycine, or nicotinic acid. Each student needs enough unknown to produce $2-3 \mathrm{mmol}$ of $\mathrm{NH}_{3}$.

## Digestion

1. Dry your unknown at $105^{\circ} \mathrm{C}$ for 45 min and accurately weigh an amount that will produce $2-3 \mathrm{mmol}$ of $\mathrm{NH}_{3}$. Place the sample in a dry $500-\mathrm{mL}$ Kjeldahl flask (Figure 11-10 in the
textbook), so that as little as possible sticks to the walls. Add 10 g of $\mathrm{K}_{2} \mathrm{SO}_{4}$ (to raise the boiling temperature) and three selenium-coated boiling chips. Pour in 25 mL of $98 \mathrm{wt} \%$ $\mathrm{H}_{2} \mathrm{SO}_{4}$, washing down any solid from the walls. (CAUTION: Concentrated $\mathrm{H}_{2} \mathrm{SO}_{4}$ eats people. If you get any on your skin, flood it immediately with water, followed by soap and water.)
2. In a fume hood, clamp the flask at a $30^{\circ}$ angle away from you. Heat gently with a burner until foaming ceases and the solution becomes homogeneous. Continue boiling gently for an additional 30 min .
3. Cool the flask for 30 min in the air, and then in an ice bath for 15 min . Slowly, and with constant stirring, add 50 mL of ice-cold, distilled water. Dissolve any solids that crystallize. Transfer the liquid to the $500-\mathrm{mL}$ 3-neck distillation flask in Figure 1. Wash the Kjeldahl flask five times with $10-\mathrm{mL}$ portions of distilled water, and pour the washings into the distillation flask.

## Distillation

1. Set up the apparatus in Figure 1 and tighten the connections well. Pipet 50.00 mL of standard 0.1 M HCl into the receiving beaker and clamp the funnel in place below the liquid level.
2. Add 5-10 drops of phenolphthalein indicator to the three-neck flask in Figure 1 and secure the stoppers. Pour 60 mL of $50 \mathrm{wt} \% \mathrm{NaOH}$ into the adding funnel and drip this into the distillation flask over a period of 1 min until the indicator turns pink. (CAUTION: $50 \mathrm{wt} \%$ NaOH eats people. Flood any spills on your skin with water.) Do not let the last 1 mL through the stopcock, so that gas cannot escape from the flask. Close the stopcock and heat the flask gently until two-thirds of the liquid has distilled.
3. Remove the funnel from the receiving beaker before removing the burner from the flask (to avoid sucking distillate back into the condenser). Rinse the funnel well with distilled water and catch the rinses in the beaker. Add 6 drops of bromocresol green indicator solution to the beaker and carefully titrate to the blue end point with standard 0.1 M NaOH . You are looking for the first appearance of light blue color. (Practice titrations with HCl and NaOH beforehand to familiarize yourself with the end point.)
4. Calculate the $w t \%$ of nitrogen in the unknown.


## 12. EDTA Titration of $\mathrm{Ca}^{2+}$ and $\mathbf{M g}^{2+}$ in Natural Waters



The most common multivalent metal ions in natural waters are $\mathrm{Ca}^{2+}$ and $\mathrm{Mg}^{2+}$. In this experiment, we will find the total concentration of metal ions that can react with EDTA, and we will assume that this equals the concentration of $\mathrm{Ca}^{2+}$ and $\mathrm{Mg}^{2+}$. In a second experiment, $\mathrm{Ca}^{2+}$ is analyzed separately after precipitating $\mathrm{Mg}(\mathrm{OH})_{2}$ with strong base.

## Reagents

EDTA: $\mathrm{Na}_{2} \mathrm{H}_{2} \mathrm{EDTA} \cdot 2 \mathrm{H}_{2} \mathrm{O}$ (FM 374.24), $0.6 \mathrm{~g} /$ student.
Buffer ( pH 10 ): Add 142 mL of $28 \mathrm{wt} \%$ aqueous $\mathrm{NH}_{3}$ to 17.5 g of $\mathrm{NH}_{4} \mathrm{Cl}$ and dilute to 250 mL with distilled water.

Eriochrome black T indicator: Dissolve 0.2 g of the solid indicator in 15 mL of triethanolamine plus 5 mL of absolute ethanol. (Alternatively, Calmagite could be used by dissolving 0.05 g in 100 mL of water. The color changes are the same for both indicators.)
Hydroxynaphthol blue indicator: This indicator may be sold as a neat solid or as a solid mixture with $\sim 99 \mathrm{wt} \% \mathrm{NaCl}$ and $1 \mathrm{wt} \%$ indicator. If you have the neat solid, dissolve 0.4 g in 100 mL of water. The $1 \%$ mixture with NaCl can be used as a solid. Hydroxynaphthol blue is hazardous in case of skin or eye contact, ingestion, or inhalation. In case of skin contact, flush with cool running water immediately. Cover the irritated skin with an emollient. If irritation persists, seek medical attention. Wash contaminated clothing well.
Unknowns: Collect water from streams or lakes or from the ocean. To minimize bacterial growth, plastic jugs should be filled to the top and tightly sealed. Refrigeration is recommended.
$50 \mathrm{wt} \% \mathrm{NaOH}$ : Dissolve 100 g of NaOH in 100 g of $\mathrm{H}_{2} \mathrm{O}$ in a $250-\mathrm{mL}$ plastic bottle. Store tightly capped. When you remove solution with a pipet, try not to disturb the solid $\mathrm{Na}_{2} \mathrm{CO}_{3}$ precipitate. The solution is extremely corrosive to human tissue and clothing. In case of contact, flush with cool running water immediately. Seek medical attention for serious burns.

## Procedure

1. Dry $\mathrm{Na}_{2} \mathrm{H}_{2}$ EDTA $\cdot 2 \mathrm{H}_{2} \mathrm{O}$ (FM 372.24) at $80^{\circ} \mathrm{C}$ for 1 h and cool in the desiccator. Accurately weigh out $\sim 0.6 \mathrm{~g}$ and dissolve it with heating in 400 mL of water in a $500-\mathrm{mL}$ volumetric flask. Cool to room temperature, dilute to the mark, and mix well.
2. Pipet a sample of unknown into a $250-\mathrm{mL}$ flask. A $1.000-\mathrm{mL}$ sample of seawater or a $50.00-$ mL sample of tap water is usually reasonable. If you use 1.000 mL of seawater, add 50 mL of distilled water. To each sample, add 3 mL of pH 10 buffer and 6 drops of Eriochrome black T indicator. Titrate with EDTA from a $50-\mathrm{mL}$ buret and note when the color changes from wine red to blue. Practice finding the end point several times by adding a little tap water and titrating with more EDTA. Save a solution at the end point to use as a color comparison for other titrations.
3. Repeat the titration with three samples to find an accurate value of the total $\mathrm{Ca}^{2+}+\mathrm{Mg}^{2+}$ concentration. Perform a blank titration with 50 mL of distilled water and subtract the value of the blank from each result.
4. For the determination of $\mathrm{Ca}^{2+}$, pipet four samples of unknown into clean flasks (adding 50 mL of distilled water if you use 1.000 mL of seawater). Add 30 drops of $50 \mathrm{wt} \% \mathrm{NaOH}$ to each solution and swirl for 2 min to precipitate $\mathrm{Mg}(\mathrm{OH})_{2}$ (which may not be visible). Add 6 drops of hydroxynaphthol blue indicator solution or $\sim 0.1 \mathrm{~g}$ of solid $1 \mathrm{wt} \%$ hydroxynaphthol blue to each flask. (This indicator is used because it remains blue at higher pH than does Eriochrome black T.) Titrate one sample rapidly to find the end point and practice finding it several times, if necessary. Remember that the titration of $\mathrm{Ca}^{2+}$ cannot require more EDTA than you needed for $\mathrm{Ca}^{2+}+\mathrm{Mg}^{2+}$. Save a solution at the end point to use as a color comparison for other titrations.
5. Titrate the other three samples carefully. After reaching the blue end point, allow each sample to sit for 5 min with occasional swirling so that any $\mathrm{Ca}(\mathrm{OH})_{2}$ precipitate may redissolve. Then titrate back to the blue end point. (Repeat this procedure if the blue color turns to red upon standing.) Perform a blank titration with 50 mL of distilled water.
6. Calculate the total concentration of $\mathrm{Ca}^{2+}$ and $\mathrm{Mg}^{2+}$, as well as the individual concentrations of each ion. Calculate the relative standard deviation of replicate titrations.

## 13. Synthesis and Analysis of Ammonium Decavanadate ${ }^{21}$



The species of aqueous $\mathrm{V}^{5+}$ depend on both pH and concentration (Figure 1).
$\mathrm{VO}_{4}^{3-} \rightleftharpoons \mathrm{V}_{2} \mathrm{O}_{7}^{4-} \rightleftharpoons \mathrm{V}_{4} \mathrm{O}_{12}^{4-} \rightleftharpoons \mathrm{HV}_{10} \mathrm{O}_{28}^{5-} \rightleftharpoons \mathrm{VO}_{2}^{+}$
In strong
base

$$
\begin{aligned}
& \begin{array}{l}
\mathrm{NH}_{4}^{+}, \\
\text {acetic acid, } \\
\text { alcohol }
\end{array} \\
& \begin{array}{l}
\text { In strong } \\
\text { acid }
\end{array} \\
& \left(\mathrm{NH}_{4}\right)_{6} \mathrm{~V}_{10} \mathrm{O}_{28} \cdot 6 \mathrm{H}_{2} \mathrm{O} \\
& \text { FM } 1173.7
\end{aligned}
$$

The decavanadate ion $\left(\mathrm{V}_{10} \mathrm{O}_{28}^{6-}\right)$, which we will isolate in this experiment as the ammonium salt, consists of $10 \mathrm{VO}_{6}$ octahedra sharing edges with one another (Figure 2).


Figure 1. Phase diagram for aqueous vanadium(V) as a function of total vanadium concentration and pH. [From J. W. Larson, J. Chem. Eng. Data 1995, 40, 1276.] The region marked "precipitate" probably refers to a vanadium hydroxide.
21. G. G. Long, R. L. Stanfield, and F. C. Hentz, Jr., J. Chem. Ed. 1979, 56, 195.


Figure 2. Structure of $\mathrm{V}_{10} \mathrm{O}_{28}^{6-}$ anion, consisting of $\mathrm{VO}_{6}$ octahedra sharing edges with one another. There is a vanadium atom at the center of each octahedron.

After preparing this salt, we will determine the vanadium content by a redox titration and $\mathrm{NH}_{4}^{+}$by the Kjeldahl method. In the redox titration, $\mathrm{V}^{5+}$ will first be reduced to $\mathrm{V}^{4+}$ with sulfurous acid and then titrated with standard permanganate.

$$
\begin{aligned}
& \mathrm{V}_{10} \mathrm{O}_{28}^{6-}+\mathrm{H}_{2} \mathrm{SO}_{3} \rightarrow \mathrm{VO}^{2+}+\mathrm{SO}_{2} \\
& \mathrm{VO}^{2+}+\underset{\text { purple }}{\mathrm{MnO}_{4}^{-}} \rightarrow \underset{\text { yellow }}{\mathrm{VO}_{2}^{+}}+\underset{\text { colorless }}{\mathrm{Mn}^{2+}}
\end{aligned}
$$

## Reagents

Ammonium metavanadate $\left(\mathrm{NH}_{4} \mathrm{VO}_{3}\right): 3 \mathrm{~g} /$ student.
50 vol\% aqueous acetic acid: $4 \mathrm{~mL} /$ student.
$95 \%$ ethanol: $200 \mathrm{~mL} /$ student.
$\mathrm{KMnO}_{4}$ : $\quad 1.6 \mathrm{~g} /$ student or prepare $0.02 \mathrm{M} \mathrm{KMnO}_{4}(\sim 300 \mathrm{~mL} / \mathrm{student})$ for use by the class.
Sodium Oxalate $\left(\mathrm{Na}_{2} \mathrm{C}_{2} \mathrm{O}_{4}\right): 1 \mathrm{~g} /$ student.
$0.9 \mathrm{M} \mathrm{H}_{2} \mathrm{SO}_{4}$ : ( $1 \mathrm{~L} /$ student) Slowly add 50 mL of concentrated ( $96-98 \mathrm{wt} \%$ ) $\mathrm{H}_{2} \mathrm{SO}_{4}$ to 900 mL of $\mathrm{H}_{2} \mathrm{O}$ and dilute to $\sim 1 \mathrm{~L}$.
$1.5 \mathrm{M} \mathrm{H}_{2} \mathrm{SO}_{4}$ : ( $100 \mathrm{~mL} /$ student) Slowly add 83 mL of concentrated $(96-98 \mathrm{wt} \%) \mathrm{H}_{2} \mathrm{SO}_{4}$ to 900 mL of $\mathrm{H}_{2} \mathrm{O}$ and dilute to $\sim 1 \mathrm{~L}$.
Sodium hydrogen sulfite ( $\mathrm{NaHSO}_{3}$, also called sodium bisulfite): $2 \mathrm{~g} /$ student.
Standard 0.1 M HCl: ( $75 \mathrm{~mL} /$ student) From Experiment 6.
Standard $0.1 \mathrm{M} \mathrm{NaOH:} \mathrm{( } 75 \mathrm{~mL} / \mathrm{student}$ ) From Experiment 6.
Phenolphthalein indicator and bromocresol green indicators: Recipes in Experiment 7.
$50 \mathrm{wt} \% \mathrm{NaOH}: \quad 60 \mathrm{~mL} /$ student. Mix 100 g NaOH with $100 \mathrm{~mL} \mathrm{H}_{2} \mathrm{O}$ and dissolve.

## Synthesis

1. Heat 3.0 g of ammonium metavanadate $\left(\mathrm{NH}_{4} \mathrm{VO}_{3}\right)$ in 100 mL of water with constant stirring (but not boiling) until most or all of the solid has dissolved. Filter the solution and add 4 mL of $50 \mathrm{vol} \%$ aqueous acetic acid with stirring.
2. Add 150 mL of $95 \%$ ethanol with stirring and then cool the solution in a refrigerator or ice bath.
3. After maintaining a temperature of $0^{\circ}-10^{\circ} \mathrm{C}$ for 15 min , filter the orange product with suction and wash with two $15-\mathrm{mL}$ portions of ice-cold $95 \%$ ethanol.
4. Dry the product in the air (protected from dust) for 2 days. Typical yield is $2.0-2.5 \mathrm{~g}$.

## Analysis of Vanadium with $\mathbf{K M n O}_{4}$

Preparation and Standardization of $\mathbf{K M n O}_{4}{ }^{22}$ (See Section 16-4 in the textbook)

1. Prepare a 0.02 M permanganate solution by dissolving 1.6 g of $\mathrm{KMnO}_{4}$ in 500 mL of distilled water. Boil gently for 1 h , cover, and allow the solution to cool overnight. Filter through a clean, fine sintered-glass funnel, discarding the first 20 mL of filtrate. Store the solution in a clean glass amber bottle. Do not let the solution touch the cap.
2. Dry sodium oxalate $\left(\mathrm{Na}_{2} \mathrm{C}_{2} \mathrm{O}_{4}\right)$ at $105^{\circ} \mathrm{C}$ for 1 h , cool in a desiccator, and weigh three $\sim 0.25-\mathrm{g}$ samples into $500-\mathrm{mL}$ flasks or $400-\mathrm{mL}$ beakers. To each, add 250 mL of 0.9 M $\mathrm{H}_{2} \mathrm{SO}_{4}$ that has been recently boiled and cooled to room temperature. Stir with a thermometer to dissolve the sample, and add $90-95 \%$ of the theoretical amount of $\mathrm{KMnO}_{4}$ solution needed for the titration. (This can be calculated from the mass of $\mathrm{KMnO}_{4}$ used to prepare the permanganate solution. The chemical reaction is given by Equation 7-1 in the textbook.)
3. Leave the solution at room temperature until it is colorless. Then heat it to $55^{\circ}-60^{\circ} \mathrm{C}$ and complete the titration by adding $\mathrm{KMnO}_{4}$ until the first pale pink color persists. Proceed slowly near the end, allowing 30 s for each drop to lose its color.
4. As a blank, titrate 250 mL of $0.9 \mathrm{M} \mathrm{H}_{2} \mathrm{SO}_{4}$ to the same pale pink color. Subtract the blank volume from each titration volume. Compute the average molarity of $\mathrm{KMnO}_{4}$.
[^10]
## Vanadium Analysis

1. Accurately weigh two $0.3-\mathrm{g}$ samples of ammonium decavanadate into $250-\mathrm{mL}$ flasks and dissolve each in 40 mL of $1.5 \mathrm{M} \mathrm{H}_{2} \mathrm{SO}_{4}$ (with warming, if necessary).
2. In a fume hood, add 50 mL of water and 1 g of $\mathrm{NaHSO}_{3}$ to each and dissolve with swirling. After 5 min , boil the solution gently for 15 min to remove $\mathrm{SO}_{2}$.
3. Titrate the warm solution with standard $0.02 \mathrm{M} \mathrm{KMnO}_{4}$ from a $50-\mathrm{mL}$ buret. The end point is taken when the yellow color of $\mathrm{VO}_{2}^{+}$takes on a dark shade (from excess $\mathrm{MnO}_{4}^{-}$) that persists for 15 s .
4. Calculate the average $\mathrm{wt} \%$ of vanadium in the ammonium decavanadate and compare your result to the theoretical value.

## Analysis of Ammonium Ion by Kjeldahl Distillation

1. Set up the apparatus in Figure 1 of Experiment 11 and press the stoppers to make airtight connections. Pipet 50.00 mL of standard 0.1 M HCl into the receiving beaker and clamp the funnel in place below the liquid level.
2. Transfer 0.6 g of accurately weighed ammonium decavanadate to the three-neck flask and add 200 mL of water. Add 5-10 drops of phenolphthalein indicator and secure the stoppers. Pour 60 mL of $50 \mathrm{wt} \% \mathrm{NaOH}$ into the adding funnel and drip this into the distillation flask over a period of 1 min until the indicator turns pink. (Caution: $50 \mathrm{wt} \% \mathrm{NaOH}$ eats people. Flood any spills on your skin with water.) Do not let the last 1 mL through the stopcock, so that gas cannot escape from the flask. Close the stopcock and heat the flask gently until two-thirds of the liquid has distilled.
3. Remove the funnel from the receiving beaker before removing the burner from the flask (to avoid sucking distillate back into the condenser). Rinse the funnel well with distilled water and catch the rinses in the beaker. Add 6 drops of bromocresol green indicator solution to the beaker and carefully titrate to the blue end point with standard 0.1 M NaOH . You are looking for the first appearance of light blue color. (Several practice titrations with HCl and NaOH will familiarize you with the end point.)
4. Calculate the weight percent of nitrogen in the ammonium decavanadate.

## 14. Iodimetric Titration of Vitamin $\mathbf{C}^{23}$



Ascorbic acid (vitamin C) is a mild reducing agent that reacts rapidly with triiodide (See Section 16-7). In this experiment, we will generate a known excess of $I_{3} \overline{3}$ by the reaction of iodate with iodide (Reaction 16-18), allow the reaction with ascorbic acid to proceed, and then back titrate the excess $I_{3}$ with thiosulfate (Reaction 16-19 and Color Plate 11).

## Reagents

Starch indicator: Make a paste of 5 g of soluble starch and 5 mg of $\mathrm{Hg}_{2} \mathrm{I}_{2}$ in 50 mL of distilled water. Pour the paste into 500 mL of boiling distilled water and boil until it is clear.

Sodium thiosulfate: $9 \mathrm{~g} \mathrm{Na} 2 \mathrm{~S}_{2} \mathrm{O}_{3} \cdot 5 \mathrm{H}_{2} \mathrm{O} /$ student.
Sodium carbonate: $50 \mathrm{mg} \mathrm{Na}_{2} \mathrm{CO}_{3} /$ student.
Potassium iodate: $1 \mathrm{~g} \mathrm{KIO}_{3} /$ student.
Potassium iodide: $12 \mathrm{~g} \mathrm{KI} /$ student.
$0.5 \mathrm{M} \mathrm{H}_{2} \mathrm{SO}_{4}$ : $30 \mathrm{~mL} /$ student.
Vitamin C: Dietary supplement containing 100 mg of vitamin $C$ per tablet is suitable. Each student needs six tablets.
$0.3 \mathrm{M} \mathrm{H}_{2} \mathrm{SO}_{4}$ : $180 \mathrm{~mL} /$ student.

## Preparation and Standardization of Thiosulfate Solution

1. Prepare starch indicator by making a paste of 5 g of soluble starch and 5 mg of $\mathrm{HgI}_{2}$ in 50 mL of water. Pour the paste into 500 mL of boiling water and boil until it is clear.
2. Prepare $0.07 \mathrm{M} \mathrm{Na}_{2} \mathrm{~S}_{2} \mathrm{O}_{3}{ }^{24}$ by dissolving $\sim 8.7 \mathrm{~g}$ of $\mathrm{Na}_{2} \mathrm{~S}_{2} \mathrm{O}_{3} \cdot 5 \mathrm{H}_{2} \mathrm{O}$ in 500 mL of freshly boiled water containing 0.05 g of $\mathrm{Na}_{2} \mathrm{CO}_{3}$. Store this solution in a tightly capped amber bottle. Prepare $\sim 0.01 \mathrm{M} \mathrm{KIO}_{3}$ by accurately weighing $\sim 1 \mathrm{~g}$ of solid reagent and dissolving it in a $500-\mathrm{mL}$ volumetric flask. From the mass of $\mathrm{KIO}_{3}$ (FM 214.00), compute the molarity of the solution.
3. D. N. Bailey, J. Chem. Ed. 1974, 51, 488.
4. An alternative to standardizing $\mathrm{Na}_{2} \mathrm{~S}_{2} \mathrm{O}_{3}$ solution is to prepare anhydrous primary standard $\mathrm{Na}_{2} \mathrm{~S}_{2} \mathrm{O}_{3}$ by refluxing 21 g of $\mathrm{Na}_{2} \mathrm{~S}_{2} \mathrm{O}_{3} \cdot 5 \mathrm{H}_{2} \mathrm{O}$ with 100 mL of methanol for 20 min . Then filter the anhydrous salt, wash with 20 mL of methanol, and dry at $70^{\circ} \mathrm{C}$ for 30 min . [A. A. Woolf, Anal. Chem. 1982, 54, 2134.]
5. Standardize the thiosulfate solution as follows: Pipet 50.00 mL of $\mathrm{KIO}_{3}$ solution into a flask. Add 2 g of solid KI and 10 mL of $0.5 \mathrm{M} \mathrm{H}_{2} \mathrm{SO}_{4}$. Immediately titrate with thiosulfate until the solution has lost almost all its color (pale yellow). Then add 2 mL of starch indicator and complete the titration. Repeat the titration with two additional $50.00-\mathrm{mL}$ volumes of $\mathrm{KIO}_{3}$ solution. From the stoichiometries of Reactions 16-18 and 16-19, compute the average molarity of thiosulfate and the relative standard deviation.

## Analysis of Vitamin C

Commercial vitamin C containing 100 mg per tablet can be used. Perform the following analysis three times, and find the mean value (and relative standard deviation) for the number of milligrams of vitamin $C$ per tablet.

1. Dissolve two tablets in 60 mL of $0.3 \mathrm{M} \mathrm{H}_{2} \mathrm{SO}_{4}$, using a glass rod to help break the solid. (Some solid binding material will not dissolve.)
2. Add 2 g of solid KI and 50.00 mL of standard $\mathrm{KIO}_{3}$. Then titrate with standard thiosulfate as above. Add 2 mL of starch indicator just before the end point.

## 15. Preparation and Iodometric Analysis of a High-Temperature Superconductor ${ }^{25}$



In this experiment you will determine the oxygen content of yttrium barium copper oxide $\left(\mathrm{YBa}_{2} \mathrm{Cu}_{3} \mathrm{O}_{\chi}\right)$. This material is an example of a nonstoichiometric solid, in which the value of $x$ is variable, but near 7. Some of the copper in the formula $\mathrm{YBa}_{2} \mathrm{Cu}_{3} \mathrm{O}_{7}$ is in the unusual high-oxidation state, $\mathrm{Cu}^{3+}$. This experiment describes the synthesis of $\mathrm{YBa}_{2} \mathrm{Cu}_{3} \mathrm{O}_{x}$, (which can also be purchased) and then gives two alternative procedures to measure the $\mathrm{Cu}^{3+}$ content. The iodometric method is based on the reactions in Box 16-3 in the textbook. The more elegant citrate-complexed copper titration ${ }^{26}$ eliminates many experimental errors associated with the simpler iodometric method and gives more accurate and precise results.

## Preparation of $\mathbf{Y B a}_{2} \mathbf{C u}_{3} \mathbf{O}_{X}$

1. Place in a mortar 0.750 g of $\mathrm{Y}_{2} \mathrm{O}_{3}, 2.622 \mathrm{~g}$ of $\mathrm{BaCO}_{3}$, and 1.581 g of CuO (atomic ratio $\mathrm{Y}: \mathrm{Ba}: \mathrm{Cu}=1: 2: 3)$. Grind the mixture well with a pestle for 20 min and transfer the powder to a porcelain crucible or boat. Heat in the air in a furnace at $920^{\circ}-930^{\circ} \mathrm{C}$ for 12 h or longer. Turn off the furnace and allow the sample to cool slowly in the furnace. This slow cooling step is critical for achieving an oxygen content in the range $x=6.5-7$ in the formula $\mathrm{YBa}_{2} \mathrm{Cu}_{3} \mathrm{O}_{x}$. The crucible may be removed when the temperature is below $100^{\circ} \mathrm{C}$.
2. Dislodge the black solid mass gently from the crucible and grind it to a fine powder with a mortar and pestle. It can now be used for this experiment, but better quality material is produced if the powder is heated again to $920^{\circ}-930^{\circ} \mathrm{C}$ and cooled slowly as in step 1 . If the powder from step 1 is green instead of black, raise the temperature of the furnace by $20^{\circ} \mathrm{C}$ and repeat step 1. The final product must be black, or it is not the correct compound.
3. D. C. Harris, M. E. Hills, and T. A. Hewston, J. Chem. Ed. 1987, 64, 847. Alternative syntheses of $\mathrm{YBa}_{2} \mathrm{Cu}_{3} \mathrm{O}_{x}$ are described by C. D. Cogdell, D. G. Wayment, D. J. Casadonte, Jr., and K. A. Kubat-Martin, J. Chem. Ed. 1995, 72, 840 and P. I. Djurovich and R. J. Watts, J. Chem. Ed. 1993, 70, 497.
4. E. H. Appelman, L. R. Morss, A. M. Kini, U. Geiser, A. Umezawa, G. W. Crabtree, and K. D. Carlson, Inorg. Chem. 1987, 26, 3237.

## lodometric Analysis

1. Sodium Thiosulfate and Starch Indicator. Prepare $0.03 \mathrm{M} \mathrm{Na}_{2} \mathrm{~S}_{2} \mathrm{O}_{3}$ as described in Experiment 14 , using 3.7 g of $\mathrm{Na}_{2} \mathrm{~S}_{2} \mathrm{O}_{3} \cdot 5 \mathrm{H}_{2} \mathrm{O}$ instead of 8.7 g . The starch indicator solution is the same one used in Experiment 14.
2. Standard $\mathrm{Cu}^{2+}$. Weigh accurately $0.5-0.6 \mathrm{~g}$ of reagent Cu wire into a $100-\mathrm{mL}$ volumetric flask. In a fume hood, add 6 mL of distilled water and 3 mL of $70 \mathrm{wt} \%$ nitric acid, and boil gently on a hot plate until the solid has dissolved. Add 10 mL of distilled water and boil gently. Add 1.0 g of urea or 0.5 g of sulfamic acid and boil for 1 min to destroy $\mathrm{HNO}_{2}$ and oxides of nitrogen that would interfere with the iodometric titration. Cool to room temperature and dilute to the mark with 1.0 M HCl .
3. Standardization of $\mathrm{Na}_{2} \mathrm{~S}_{2} \mathrm{O}_{3}$ With $\mathrm{Cu}^{2+}$. The titration should be carried out as rapidly as possible under a brisk flow of $\mathrm{N}_{2}$, because $\mathrm{I}^{-}$is oxidized to $\mathrm{I}_{2}$ in acid solution by atmospheric oxygen. Use a $180-\mathrm{mL}$ tall-form beaker (or a $150-\mathrm{mL}$ standard beaker) with a loosely fitting two-hole cork at the top. One hole serves as the inert gas inlet and the other is for the buret. Pipet 10.00 mL of standard $\mathrm{Cu}^{2+}$ into the beaker and flush with $\mathrm{N}_{2}$. Remove the cork just long enough to pour in 10 mL of distilled water containing $1.0-1.5 \mathrm{~g}$ of KI (freshly dissolved) and begin magnetic stirring. In addition to the dark color of iodine in the solution, suspended solid CuI will be present. Titrate with $\mathrm{Na}_{2} \mathrm{~S}_{2} \mathrm{O}_{3}$ solution from a $50-\mathrm{mL}$ buret, adding 2 drops of starch solution just before the last trace of $\mathrm{I}_{2}$ color disappears. If starch is added too soon, there can be irreversible attachment of $I_{2}$ to the starch and the end point is harder to detect. You may want to practice this titration several times to learn to distinguish the colors of $\mathrm{I}_{2}$ and $\mathrm{I}_{2} /$ starch from the color of suspended $\mathrm{CuI}(s)$. (Alternatively, Pt and calomel electrodes can be used instead of starch to eliminate subjective judgment of color in finding the end point. ${ }^{27}$ ) Repeat this standardization two more times and use the average $\mathrm{Na}_{2} \mathrm{~S}_{2} \mathrm{O}_{3}$ molarity from the three determinations.
4. Superconductor Experiment A. Dissolve an accurately weighed 150 - to $200-\mathrm{mg}$ sample of powdered $\mathrm{YBa}_{2} \mathrm{Cu}_{3} \mathrm{O}_{x}$ in 10 mL of $1.0 \mathrm{M} \mathrm{HClO}_{4}$ in a titration beaker in a fume hood. (Perchloric acid is recommended because it is inert to reaction with superconductor, which might oxidize HCl to $\mathrm{Cl}_{2}$. We have used HCl instead of $\mathrm{HClO}_{4}$ with no significant interference in the analysis. Solutions of $\mathrm{HClO}_{4}$ should not be boiled to dryness because of

[^11]their explosion hazard.) Boil gently for 10 min , so that Reaction 1 in Box 16-3 goes to completion. Cool to room temperature, cap with the two-hole-stopper-buret assembly, and begin $\mathrm{N}_{2}$ flow. Dissolve $1.0-1.5 \mathrm{~g}$ of KI in 10 mL of distilled water and immediately add the solution to the beaker. Titrate rapidly with magnetic stirring as described in step 3. Repeat this procedure two more times.
5. Superconductor Experiment B. Place an accurately weighed $150-$ to $200-\mathrm{mg}$ sample of powdered $\mathrm{YBa}_{2} \mathrm{Cu}_{3} \mathrm{O}_{x}$ in the titration beaker and begin $\mathrm{N}_{2}$ flow. Dissolve $1.0-1.5 \mathrm{~g}$ of KI in 10 mL of $1.0 \mathrm{M} \mathrm{HClO}_{4}$ and immediately add the solution to the titration beaker. Stir magnetically for 1 min , so that the Reactions 2 and 3 of Box $16-3$ occur. Add 10 mL of water and rapidly complete the titration. Repeat this procedure two more times.

## Calculations

1. Suppose that mass, $m_{\mathrm{A}}$, is analyzed in Experiment A and the volume, $V_{\mathrm{A}}$, of standard thiosulfate is required for titration. Let the corresponding quantities in Experiment B be $m_{\mathrm{B}}$ and $V_{\mathrm{B}}$. Let the average oxidation state of Cu in the superconductor be $2+p$. Show that $p$ is given by

$$
\begin{equation*}
p=\frac{V_{\mathrm{B}} / m_{\mathrm{B}}-V_{\mathrm{A}} / m_{\mathrm{A}}}{V_{\mathrm{A}} / m_{\mathrm{A}}} \tag{1}
\end{equation*}
$$

and $x$ in the formula $\mathrm{YBa}_{2} \mathrm{Cu}_{3} \mathrm{O}_{x}$, is related to $p$ as follows:

$$
\begin{equation*}
x=\frac{7}{2}+\frac{3}{2}(2+p) \tag{2}
\end{equation*}
$$

For example, if the superconductor contains one $\mathrm{Cu}^{3+}$ and two $\mathrm{Cu}^{2+}$, the average oxidation state of copper is $7 / 3$ and the value of $p$ is $1 / 3$. Setting $p=1 / 3$ in Equation 2 gives $x=7$. Equation 1 does not depend on the metal stoichiometry being exactly $\mathrm{Y}: \mathrm{Ba}: \mathrm{Cu} 1: 2: 3$, but Equation 2 does require this exact stoichiometry.
2. Use the average results of Experiments A and B to calculate the values of $p$ and $x$ in Equations 1 and 2.
3. Suppose that the uncertainty in mass of superconductor analyzed is 1 in the last decimal place. Calculate the standard deviations for steps 3,4 , and 5 of the iodometric analysis.

Using these standard deviations as uncertainties in volume, calculate the uncertainties in the values of $p$ and $x$ in Equations 1 and 2 .

## Citrate-Complexed Copper Titration ${ }^{26}$

This procedure directly measures $\mathrm{Cu}^{3+}$. The sample is first dissolved in a closed container with 4.4 $\mathrm{M} \mathrm{HBr}^{\text {, in }}$ which $\mathrm{Cu}^{3+}$ oxidizes $\mathrm{Br}^{-}$to $\mathrm{Br}_{3}^{-}$:

$$
\begin{equation*}
\mathrm{Cu}^{3+}+\frac{11}{2} \mathrm{Br}^{-} \rightarrow \mathrm{CuBr}_{4}^{2-}+\frac{1}{2} \mathrm{Br}_{3}^{-} \tag{3}
\end{equation*}
$$

The solution is transferred to a vessel containing excess $\mathrm{I}^{-}$, excess citrate, and enough $\mathrm{NH}_{3}$ to neutralize most of the acid. $\mathrm{Cu}^{2+}$ is complexed by citrate and is not further reduced to $\mathrm{CuI}(\mathrm{s})$. (This eliminates the problem in the iodometric titration of performing a titration in the presence of colored solid.) $\mathrm{Br}_{3}^{-}$from Reaction 3 oxidizes $\mathrm{I}^{-}$to $\mathrm{I}_{3}^{-}$:

$$
\begin{equation*}
\mathrm{Br}_{3}^{-}+3 \mathrm{I}^{-} \rightarrow 3 \mathrm{Br}^{-}+\mathrm{I}_{3}^{-} \tag{4}
\end{equation*}
$$

and the $\mathrm{I}_{3}^{-}$produced in Reaction 4 is titrated with thiosulfate.
Our experience with the iodometric procedure is that the precision in oxygen content of $\mathrm{YBa}_{2} \mathrm{Cu}_{3} \mathrm{O}_{x}$, is $\pm 0.04$ in the value of $x$. The uncertainty is reduced to $\pm 0.01$ by the citratecomplexed copper procedure.

## Procedure

1. Prepare and standardize sodium thiosulfate solution as described in steps $1-3$ of the iodometric analysis in the previous section.
2. Place an accurately weighed 20 - to $50-\mathrm{mg}$ sample of superconductor in a $4-\mathrm{mL}$ screw-cap vial with a Teflon cap liner and add 2.00 mL of ice-cold 4.4 M HBr by pipet. (The HBr is prepared by diluting 50 mL of $48 \mathrm{wt} \% \mathrm{HBr}$ to 100 mL .) Cap tightly and gently agitate the vial for 15 min as it warms to room temperature. (We use a motor to rotate the sample slowly for 15 min .)
3. Cool the solution back to $0^{\circ} \mathrm{C}$ and carefully transfer it to the titration beaker (used in the thiosulfate standardization) containing an ice-cold, freshly prepared solution made from 0.7 g of KI, 20 mL of water, 5 mL of 1.0 M trisodium citrate, and approximately 0.5 mL of 28
$\mathrm{wt} \% \mathrm{NH}_{3}$. The exact amount of $\mathrm{NH}_{3}$ should be enough to neutralize all but 1 mmol of acid present in the sample. When calculating the acid content, remember that each mole of $\mathrm{YBa}_{2} \mathrm{Cu}_{3} \mathrm{O}_{x}$ consumes $2 x$ moles of HBr . (You can estimate that $x$ is close to 7.) Wash the vial with three $1-\mathrm{mL}$ aliquots of 2 M HBr to complete the quantitative transfer to the beaker.
4. Add 0.1 mL of $1 \mathrm{wt} \%$ starch solution and titrate with 0.1 M standard $\mathrm{Na}_{2} \mathrm{~S}_{2} \mathrm{O}_{3}$ under a brisk flow of $\mathrm{N}_{2}$, using a $250-\mathrm{mL}$ Hamilton syringe to deliver titrant. The end point is marked by a change from dark blue ( $\mathrm{I}_{2}$-starch) to the light blue-green of the $\mathrm{Cu}^{2+}$-citrate complex.
5. Run a blank reaction with $\mathrm{CuSO}_{4}$ in place of superconductor. The moles of Cu in the blank should be the same as the moles of Cu in the superconductor. In a typical experiment, 30 mg of $\mathrm{YBa}_{2} \mathrm{Cu}_{3} \mathrm{O}_{6.88}$ required approximately $350 \mu \mathrm{~L}$ of $\mathrm{Na}_{2} \mathrm{~S}_{2} \mathrm{O}_{3}$ and the blank required $10 \mu \mathrm{~L}$ of $\mathrm{Na}_{2} \mathrm{~S}_{2} \mathrm{O}_{3}$ If time permits, run two more blanks. Subtract the average blank from the titrant in step 4.
6. Repeat the analysis with two more samples of superconductor.

## Calculations

1. From the thiosulfate required to titrate $\mathrm{I}_{3}^{-}$released in Reaction 4, find the average moles of $\mathrm{Cu}^{3+}$ per gram of superconductor $\left(1 \mathrm{~mol} \mathrm{~S}_{2} \mathrm{O}_{3}^{2-}=1 \mathrm{~mol} \mathrm{Cu}^{3+}\right)$ and the standard deviation for your three samples.
2. Defining $R$ as (mol Cu $\left.{ }^{3+}\right) /\left(\mathrm{g}\right.$ superconductor), show that $z$ in the formula $\mathrm{YBa}_{2} \mathrm{Cu}_{3} \mathrm{O}_{7-z}$ is

$$
\begin{equation*}
z=\frac{1-666.20 R}{2-15.999 R} \tag{5}
\end{equation*}
$$

where 666.20 is the formula mass of $\mathrm{YBa}_{2} \mathrm{Cu}_{3} \mathrm{O}_{7}$ and 15.9994 is the atomic mass of O .
3. Using your average value of $R$ and using its standard deviation as an estimate of uncertainty, calculate the average value of $z$ and its uncertainty. Find the average value of $x$ and its uncertainty in the formula $\mathrm{YBa}_{2} \mathrm{Cu}_{3} \mathrm{O}_{x}$. If you are really daring, use Equation $\mathrm{B}-1$ in Appendix B of the textbook for propagation of uncertainty in Equation 5.

## 16. Potentiometric Halide Titration with $\mathbf{A g}^{+}$



Mixtures of halides can be titrated with $\mathrm{AgNO}_{3}$ solution as described in Section 7-4 in the textbook. In this experiment, you will use the apparatus in Figure $7-5$ of the textbook to monitor the activity of $\mathrm{Ag}^{+}$as the titration proceeds. The theory of the potentiometric measurement is described in Section 15-2 of the textbook.

Each student is given a vial containing $0.22-0.44 \mathrm{~g}$ of KCl plus $0.50-$ 1.00 g of KI (both weighed accurately). The object is to determine the quantity of each salt in the mixture. A 0.4 M bisulfate buffer $(\mathrm{pH} 2)$ should be available in the lab. It is prepared by titrating $1 \mathrm{M} \mathrm{H}_{2} \mathrm{SO}_{4}$ with 1 M NaOH to a pH near 2.0.

## Reagents

Unknowns: Each student receives a vial containing $0.22-0.44 \mathrm{~g}$ of KCl plus $0.50-1.00 \mathrm{~g}$ of KI (weighed accurately). The object is to determine the quantity of each salt in the mixture.

Buffer (pH 2): ( $6 \mathrm{~mL} /$ student) Titrate $1 \mathrm{M} \mathrm{H}_{2} \mathrm{SO}_{4}$ with 1 M NaOH to a pH near 2.0.
Silver nitrate: $1.2 \mathrm{~g} \mathrm{AgNO}_{3} /$ student.

## Procedure

1. Pour your unknown carefully into a 50 - or $100-\mathrm{mL}$ beaker. Dissolve the solid in $\sim 20 \mathrm{~mL}$ of water and pour the solution into a $100-\mathrm{mL}$ volumetric flask. Rinse the sample vial and beaker five times with small portions of $\mathrm{H}_{2} \mathrm{O}$ and transfer the washings to the flask. Dilute to the mark and mix well.
2. Dry 1.2 g of $\mathrm{AgNO}_{3}$ (FM 169.87) at $105^{\circ} \mathrm{C}$ for 1 h and cool in a dessicator for 30 min with minimal exposure to light. Some discoloration is normal (and tolerable in this experiment) but should be minimized. Accurately weigh 1.2 g and dissolve it in a $100-\mathrm{mL}$ volumetric flask.
3. Set up the apparatus in Figure $7-5$ of the textbook. The silver electrode is simply a $3-\mathrm{cm}$ length of silver wire soldered to copper wire. (Fancier electrodes can be prepared by housing the connection in a glass tube sealed with epoxy at the lower end. Only the silver should protrude from the epoxy.) The copper wire is fitted with a jack that goes to the reference
socket of a pH meter. The reference electrode for this titration is a glass pH electrode connected to its usual socket on the meter. If a combination pH electrode is employed, the reference jack of the combination electrode is not used. The silver electrode should be taped to the inside of the $100-\mathrm{mL}$ beaker so that the $\mathrm{Ag} / \mathrm{Cu}$ junction remains dry for the entire titration. The stirring bar should not hit either electrode.
4. Pipet 25.00 mL of unknown into the beaker, add 3 mL of pH 2 buffer, and begin magnetic stirring. Record the initial level of $\mathrm{AgNO}_{3}$ in a $50-\mathrm{mL}$ buret and add $\sim 1 \mathrm{~mL}$ of titrant to the beaker. Turn the pH meter to the millivolt scale and record the volume and voltage. It is convenient (but is not essential) to set the initial reading to +800 mV by adjusting the meter.
5. Titrate the solution with $\sim 1-\mathrm{mL}$ aliquots until 50 mL of titrant have been added or until you can see two abrupt voltage changes. You need not allow more than $15-30 \mathrm{~s}$ for each point. Record the volume and voltage at each point. Make a graph of millivolts versus milliliters to find the approximate positions ( $\pm 1 \mathrm{~mL}$ ) of the two end points.
6. Turn the pH meter to standby, remove the beaker, rinse the electrodes well with distilled water, and blot them dry with a tissue. (Silver halide adhering to the glass electrode can be removed by soaking in concentrated sodium thiosulfate solution. This thorough cleaning is not necessary between steps 6 and 7 in this experiment. The silver halides in the titration beaker can be saved and converted back to pure $\mathrm{AgNO}_{3} .{ }^{28}$ ) Clean the beaker and set up the titration apparatus again. The beaker need not be dry.
7. Perform an accurate titration using 1-drop aliquots near the end points (and 1-mL aliquots elsewhere). You need not allow more than 30 s per point for equilibration.
8. Prepare a graph of millivolts versus milliliters and locate the end points as in Figure 7-4 of the textbook. The $I^{-}$end point is taken as the intersection of the two dashed lines in the inset of Figure 7-4. The $\mathrm{Cl}^{-}$end point is the inflection point (the steepest point) at the second break. Calculate milligrams of KI and milligrams of KCl in your solid unknown.

## Analyzing Cl- in Streams, Lakes, or Salt Water

A variation of the preceding procedure could make a class project in environmental analysis. For example, you could study changes in streams as a function of the season or recent rainfall.

[^12]You could study stratification (layering) of water in lakes. The measurement responds to all ions that precipitate with $\mathrm{Ag}^{+}$, of which $\mathrm{Cl}^{-}$is, by far, the dominant ion in natural waters.

You can use the electrodes in Figure 7-5 of the textbook, or you can construct the rugged combination electrode shown in Figure 1.29 The indicator electrode in Figure 1 is a bare silver wire in contact with analyte solution. The inner (reference) chamber of the combination electrode contains a copper wire dipped into $\mathrm{CuSO}_{4}$ solution. The inner electrode maintains a


Figure 1. Combination electrode constructed from 8-mm-outerdiameter glass tubing. Strip the insulation off the ends of a twowire copper cable. One bare Cu wire extends into the glass tube. A silver wire soldered to the other Cu wire is left outside the glass tube. The assembly is held together at the top with heatshrink tubing. When ready for use, insert a cotton thread into the bottom of the tube and fit a $14 / 20$ serum cap moistened with 0.1 M $\mathrm{CuSO}_{4}$ over the end so that part of the thread is inside and part is outside. After adding 0.1 M $\mathrm{CuSO}_{4}$ to the inside of the tube, the electrode is ready for use.
constant potential because the concentration of $\mathrm{Cu}^{2+}$ in the solution is constant. The solution makes electrical contact at the septum, where a piece of thread leaves enough space for solution to slowly drain from the electrode into the external sample solution.

## Procedure

1. Collect water from streams or lakes or from the ocean. To minimize bacterial growth, plastic jugs should be filled to the top and tightly sealed. Refrigeration is recommended.
2. G. Lisensky and K. Reynolds, J. Chem. Ed. 1991, 68, 334; R. Ramette, Chemical Equilibrium (Reading, MA: Addison-Wesley, 1981), p. 649.
3. Prepare $4 \mathrm{mM} \mathrm{AgNO}_{3}$ solution with an accurately known concentration, as in step 2 at the beginning of this experiment. One student can prepare enough reagent for five people by using 0.68 g of $\mathrm{AgNO}_{3}$ in a 1-L volumetric flask.
4. Measure with a graduated cylinder 100 mL of a natural water sample and pour it into a 250 mL beaker. Position the combination electrode from Figure 1 or the pair of electrodes from Figure 7-5 of the textbook in the beaker so that a stirring bar will not hit the electrode.
5. Carry out a rough titration by adding $1.5-\mathrm{mL}$ increments of titrant to the unknown and reading the voltage after 30 s to the nearest millivolt. Prepare a graph of voltage versus volume of titrant to locate the end point, which will not be as abrupt as those in Figure 7-4 of the textbook. If necessary, adjust the volume of unknown in future steps so that the end point comes at $20-40 \mathrm{~mL}$. If you need less unknown, make up the difference with distilled water.
6. Carry out a more careful titration with fresh unknown. Add three-quarters of the titrant volume required to reach the equivalence point all at once. Then add $\sim 0.4-\mathrm{mL}$ increments ( 8 drops from a $50-\mathrm{mL}$ buret) of titrant until you are 5 mL past the equivalence point. Allow 30 s (or longer, if necessary) for the voltage to stabilize after each addition. The end point is the steepest part of the curve, which can be estimated by the method shown in Figure 1 of Experiment 7.
7. Calculate the molarity and parts per million $(\mu \mathrm{g} / \mathrm{mL})$ of $\mathrm{Cl}^{-}$in the unknown. Use data from several students with the same sample to find the mean and standard deviation of $\mathrm{ppm} \mathrm{Cl}^{-}$.

## 17. Electrogravimetric Analysis of Copper



Most copper-containing compounds can be electrolyzed in acidic solution, with quantitative deposition of Cu at the cathode. Section 17-2 of the textbook discusses this technique.

Students may analyze a preparation of their own (such as copper acetylsalicylate ${ }^{30}$ ) or be given unknowns prepared from $\mathrm{CuSO}_{4} \cdot 5 \mathrm{H}_{2} \mathrm{O}$ or metallic Cu . In the latter case, dissolve the metal in $8 \mathrm{M} \mathrm{HNO}_{3}$, boil to remove $\mathrm{HNO}_{2}$, neutralize with ammonia, and barely acidify the solution with dilute $\mathrm{H}_{2} \mathrm{SO}_{4}$ (using litmus paper to test for acidity). Samples must be free of chloride and nitrous acid. ${ }^{31}$ Copper oxide unknowns (soluble in acid) are available from Thorn Smith. ${ }^{2}$

The apparatus in Figure 17-6 of the textbook uses any 6-12 V direct-current power supply. A tall-form $150-\mathrm{mL}$ beaker is the reaction vessel.

## Procedure

1. Handle the Pt gauze cathode with a tissue, touching only the thick stem, not the wire gauze. Immerse the electrode in hot $8 \mathrm{M} \mathrm{HNO}_{3}$ to remove previous deposits, rinse with water and alcohol, dry at $105^{\circ} \mathrm{C}$ for 5 min , cool for 5 min , and weigh accurately. If the electrode contains any grease, it can be heated to red heat over a burner after the treatment above. ${ }^{32}$
2. The sample should contain $0.2-0.3 \mathrm{~g}$ of Cu in 100 mL . Add 3 mL of $98 \mathrm{wt} \% \mathrm{H}_{2} \mathrm{SO}_{4}$ and 2 mL of freshly boiled $8 \mathrm{M} \mathrm{HNO}_{3}$. Position the cathode so that the top 5 mm are above the liquid level after magnetic stirring is begun. Adjust the current to 2 A , which should require $3-4 \mathrm{~V}$. When the blue color of $\mathrm{Cu}(\mathrm{II})$ has disappeared, add some distilled water so that new Pt surface is exposed to the solution. If no further deposition of Cu occurs on the fresh surface in 15 min at a current of 0.5 A , the electrolysis is complete. If deposition is observed, continue electrolysis and test the reaction for completeness again.

[^13]3. Without turning off the power, lower the beaker while washing the electrode with a squirt bottle. Then the current can be turned off. (If current is disconnected before removing the cathode from the liquid and rinsing off the acid, some Cu could redissolve.) Wash the cathode gently with water and alcohol, dry at $105^{\circ} \mathrm{C}$ for 3 min , cool in a desiccator for 5 min , and weigh.
4. Report the mass of Cu in the unknown.

## 18. Polarographic Measurement of an Equilibrium Constant ${ }^{33}$



In this experiment, you will find the overall formation constant $\left(\beta_{p}\right)$ and stoichiometry for the reaction of oxalate with $\mathrm{Pb}^{2+}$ :

$$
\mathrm{Pb}^{2+}+p \mathrm{C}_{2} \mathrm{O}_{4}^{2-} \rightleftharpoons \mathrm{Pb}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{p}^{2-2 p} \quad \beta p=\frac{\left[\mathrm{Pb}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{p}^{2-2 p}\right]}{\left[\mathrm{Pb}^{2+}\right]\left[\mathrm{C}_{2} \mathrm{O}_{4}^{2-}\right]^{p}}
$$

where $p$ is a stoichiometry coefficient. We will do this by measuring the polarographic half-wave potential for solutions containing $\mathrm{Pb}^{2+}$ and various amounts of oxalate. Polarography is described in Section 17-5 of the textbook. The change of half-wave potential, $\Delta E_{1 / 2}\left[=E_{1 / 2}(\right.$ observed $)-E_{1 / 2}\left(\right.$ for $\mathrm{Pb}^{2+}$ without oxalate $\left.)\right]$ is expected to obey the equation

$$
\begin{equation*}
\Delta E_{1 / 2}=-\frac{R T}{n F} \ln \beta_{\mathrm{p}}-\frac{p R T}{n F} \ln \left[\mathrm{C}_{2} \mathrm{O}_{4}^{2-}\right] \tag{1}
\end{equation*}
$$

where $R$ is the gas constant, $F$ is the Faraday constant, and $T$ is temperature in kelvins. You should measure the lab temperature at the time of the experiment or use a thermostatically controlled cell.

An electrode reaction is considered to be reversible when it is fast enough to maintain equilibrium at the electrode surface. The shape of a reversible polarographic wave is given by

$$
\begin{equation*}
E=E_{1 / 2}-\frac{R T}{n F} \ln \left(\frac{I}{I_{\mathrm{d}}-I}\right) \tag{2}
\end{equation*}
$$

where $I$ is current and $I_{\mathrm{d}}$ is diffusion current (the current at the plateau of the wave).

## Procedure

1. Pipet 1.00 mL of $0.020 \mathrm{M} \mathrm{Pb}\left(\mathrm{NO}_{3}\right)_{2}$ into each of five $50-\mathrm{mL}$ volumetric flasks labeled $\mathrm{A}-\mathrm{E}$ and add 1 drop of $1 \mathrm{wt} \%$ Triton $\mathrm{X}-100$ to each. Then add the following solutions and dilute to the mark with water. The $\mathrm{KNO}_{3}$ may be delivered carefully with a graduated cylinder. The oxalate should be pipetted.

A: Add nothing else. Dilute to the mark with $1.20 \mathrm{M} \mathrm{KNO}_{3}$.

[^14]B: Add 5.00 mL of $1.00 \mathrm{M} \mathrm{K}_{2} \mathrm{C}_{2} \mathrm{O}_{4}$, and 37.5 mL of $1.20 \mathrm{M} \mathrm{KNO}_{3}$.
C: Add 10.00 mL of $1.00 \mathrm{M} \mathrm{K}_{2} \mathrm{C}_{2} \mathrm{O}$, and 25.0 mL of $1.20 \mathrm{M} \mathrm{KNO}_{3}$.
D: Add 15.00 mL of $1.00 \mathrm{M} \mathrm{K}_{2} \mathrm{C}_{2} \mathrm{O}_{4}$ and 12.5 mL of $1.20 \mathrm{M} \mathrm{KNO}_{3}$.
E: Add 20.00 mL of $1.00 \mathrm{M} \mathrm{K}_{2} \mathrm{C}_{2} \mathrm{O}_{4}$.
2. Transfer each solution to a polarographic cell, deoxygenate with bubbling $\mathrm{N}_{2}$ for 10 min , and record the polarogram from -0.20 to -0.95 V (versus S.C.E.). Measure the residual current, using the same settings and a solution containing just $1.20 \mathrm{M} \mathrm{KNO}_{3}$ (plus 1 drop of $1 \mathrm{wt} \%$ Triton X-100). Record each polarogram on a scale sufficiently expanded to allow accurate measurements.
3. For each polarogram, make a graph of $E$ versus $\ln \left[I /\left(I_{d}-I\right)\right]$, using 6-8 points for each graph. Be sure to subtract the residual current at each potential. According to Equation 2, $E=E_{1 / 2}$ when $\left.\ln \left[I /\left(I_{\mathrm{d}}-I\right)\right]\right]=0$. Use this condition to locate $E_{1 / 2}$ on each graph.
4. Make a graph of $\Delta E_{1 / 2}$ versus $\ln \left[\mathrm{C}_{2} \mathrm{O}_{4}^{2-}\right]$. From the slope, use Equation 1 to find $p$, the stoichiometry coefficient. Then use the intercept to find the value of $\beta_{p}$. Use the method of least squares to find the standard deviations of the slope and intercept. From the standard deviations, find the uncertainties in $p$ and $\beta_{p}$ and express each with the correct number of significant figures.

## 19. Coulometric Titration of Cyclohexene with Bromine ${ }^{34}$



Coulometry is described in Section 17-3 of the textbook. In this experiment, cyclohexene will be titrated with $\mathrm{Br}_{2}$ generated by electrolytic oxidation of $\mathrm{Br}^{-}$:

$$
\begin{equation*}
2 \mathrm{Br}^{-} \rightarrow \mathrm{Br}_{2}+2 \mathrm{e}^{-} \tag{1}
\end{equation*}
$$

Cyclohexene trans-1,2-Dibromocyclohexane
The initial solution contains an unknown quantity of cyclohexene and a large amount of $\mathrm{Br}^{-}$. When Reaction 1 has generated just enough $\mathrm{Br}_{2}$ to react with all the cyclohexene, the moles of electrons liberated in Reaction 1 are equal to twice the moles of $\mathrm{Br}_{2}$ and therefore twice the moles of cyclohexene.

The reaction is carried out at a constant current with the apparatus in Figure 1. $\mathrm{Br}_{2}$ generated at the Pt anode at the left immediately reacts with cyclohexene. When cyclohexene is consumed, the concentration of $\mathrm{Br}_{2}$ suddenly rises, signaling the end of the reaction.

The equation relating moles of electrons to the electric current and the time is
Relation between electrons, current, and time:

$$
\begin{equation*}
\text { Moles of } \mathrm{e}^{-}=\frac{I \cdot t}{F} \tag{3}
\end{equation*}
$$

where $I$ is the current in amperes ( $=$ coulombs $/ \mathrm{s}=\mathrm{C} / \mathrm{s}$ ), $t$ is the time in seconds, and $F$ is the Faraday constant (96 $485 \mathrm{C} / \mathrm{mol}$ ).

The rise in $\mathrm{Br}_{2}$ concentration is detected by measuring the current between the two detector electrodes at the right in Figure 1. A voltage of 0.25 V applied between these two electrodes is not enough to electrolyze any solute, so only a tiny current of $<1 \mu \mathrm{~A}$ flows through the microammeter. At the equivalence point, cyclohexene is consumed, $\left[\mathrm{Br}_{2}\right]$ suddenly increases, and detector current flows by virtue of the reactions:

$$
\begin{array}{ll}
\text { Detector anode: } & 2 \mathrm{Br}^{-} \rightarrow \mathrm{Br}_{2}+2 \mathrm{e}^{-} \\
\text {Detector cathode: } & \mathrm{Br}_{2}+2 \mathrm{e}^{-} \rightarrow 2 \mathrm{Br}^{-}
\end{array}
$$

[^15]

Figure 1. Apparatus for coulometric titration of cyclohexene with $\mathrm{Br}_{2}$.

In our procedure, enough $\mathrm{Br}_{2}$ is first generated in the absence of cyclohexene to give a detector current of $20.0 \mu \mathrm{~A}$. When cyclohexene is added, the current decreases to a tiny value because $\mathrm{Br}_{2}$ is consumed. $\mathrm{Br}_{2}$ is then generated by the coulometric circuit, and the end point is taken when the detector again reaches $20.0 \mu \mathrm{~A}$. Because the reaction is begun with $\mathrm{Br}_{2}$ present, impurities that can react with $\mathrm{Br}_{2}$ before analyte is added are eliminated.

The electrolysis current (not to be confused with the detector current) for the $\mathrm{Br}_{2}$-generating electrodes can be controlled by a hand-operated switch. As the detector current approaches $20.0 \mu \mathrm{~A}$, you close the switch for shorter and shorter intervals. This practice is analogous to adding titrant dropwise from a buret near the end of a titration. The switch in the coulometer circuit serves as a "stopcock" for addition of $\mathrm{Br}_{2}$ to the reaction.

## EXAMPLE Coulometric Titration

A $2.000-\mathrm{mL}$ volume containing 0.6113 mg of cyclohexene $/ \mathrm{mL}$ is to be titrated with a constant current of 4.825 mA . How much time will required for complete titration?

Solution The quantity of cyclohexene is

$$
\frac{(2.000 \mathrm{~mL})(0.6113 \mathrm{mg} / \mathrm{mL})}{(82.146 \mathrm{mg} / \mathrm{mmol})}=0.01488 \mathrm{mmol}
$$

In Reactions 1 and 2, each mole of cyclohexene requires $1 \mathrm{~mol}^{\text {of }} \mathrm{Br}_{2}$, which requires 2 mol of electrons. For 0.01488 mmol of cyclohexene to react, 0.02976 mmol of electrons must flow. From Equation 3,

Moles of $\mathrm{e}^{-}=\frac{I \cdot t}{F} \Rightarrow t=\frac{\left(\text { moles of } \mathrm{e}^{-}\right) F}{I}=\frac{\left(0.02976 \times 10^{-3} \mathrm{~mol}\right)(96485 \mathrm{C} / \mathrm{mol})}{\left(4.825 \times 10^{-3} \mathrm{C} / \mathrm{s}\right)}=595.1 \mathrm{~s}$
It will require just under 10 min to complete the reaction.

For this experiment, you can use a commercial coulometer or the circuits in Figure 2.35 Start timing with a stopwatch when the generator switch is closed.


Figure 2. Circuits for coulometric titrations. (a) Generator circuit. (b) Detector circuit.

[^16]
## Procedure

1. The electrolyte is a $60: 26: 14(\mathrm{vol} / \mathrm{vol} / \mathrm{vol})$ mixture of acetic acid, methanol, and water. The solution contains 0.15 M KBr and 0.1 g of mercuric acetate per 100 mL . (The latter catalyzes the reaction between $\mathrm{Br}_{2}$ and cyclohexene.) The electrodes should be covered with electrolyte. Begin vigorous magnetic stirring (without spattering) and adjust the voltage of the detector circuit to 0.25 V .
2. Generate $\mathrm{Br}_{2}$ with the generator circuit until the detector current is $20.0 \mu \mathrm{~A}$. The generator current should be $\sim 5-10 \mathrm{~mA}$.
3. Pipet $2-5 \mathrm{~mL}$ of unknown (containing $1-5 \mathrm{mg}$ of cyclohexene in methanol) into the flask and set the clock or coulometer to 0 . The detector current should drop to near 0 because the cyclohexene consumes the $\mathrm{Br}_{2}$.
4. Turn the generator circuit on and begin timing. While the reaction is in progress, measure the voltage $(E)$ across the precision resistor $(R=100.0 \pm 0.1 \Omega)$ to find the exact current $(I)$ flowing through the cell $(I=E / R)$. Continue the electrolysis until the detector current rises to $20.0 \mu \mathrm{~A}$. Then stop the coulometer and record the time.
5. Repeat the procedure two more times and find the average molarity (and relative standard deviation) of cyclohexene.
6. When you are finished, be sure all switches are off. Soak the generator electrodes in 8 M $\mathrm{HNO}_{3}$ to dissolve Hg that is deposited during the electrolysis.

## 20. Spectrophotometric Determination of Iron in Vitamin Tablets ${ }^{36}$



In this procedure, iron from a vitamin supplement tablet is dissolved in acid, reduced to $\mathrm{Fe}^{2+}$ with hydroquinone, and complexed with o-phenanthroline to form an intensely colored complex (Color Plate 15 in the textbook).


Quinone
Hydroquinone
FM 110.11


## Reagents

Hydroquinone: ( $20 \mathrm{~mL} /$ student) Freshly prepared solution containing $10 \mathrm{~g} / \mathrm{L}$ in distilled water.
Store in an amber bottle.
Trisodium citrate: ( $20 \mathrm{~mL} /$ student) $25 \mathrm{~g} / \mathrm{L} \mathrm{Na} 2$ citrate $\cdot 2 \mathrm{H}_{2} \mathrm{O}$ (FM 294.10) in distilled water.
o-Phenanthroline: ( $25 \mathrm{~mL} /$ student) Dissolve 2.5 g in 100 mL of ethanol and add 900 mL of distilled water. Store in an amber bottle.
$6 \mathrm{M} \mathrm{HCl}:(25 \mathrm{~mL} /$ student) Dilute 124 mL of $37 \mathrm{wt} \% \mathrm{HCl}$ up to 250 mL with distilled water.
Standard Fe ( $40 \mu \mathrm{~g} \mathrm{Fe} / \mathrm{mL}$ ): ( $35 \mathrm{~mL} /$ student) Dissolve 0.281 g of reagent-grade $\mathrm{Fe}\left(\mathrm{NH}_{4}\right)_{2}\left(\mathrm{SO}_{4}\right)_{2} \cdot 6 \mathrm{H}_{2} \mathrm{O}(\mathrm{FM} 392.14)$ in distilled water in a 1-L volumetric flask containing 1 mL of $98 \mathrm{wt} \% \mathrm{H}_{2} \mathrm{SO}_{4}$.

## Procedure

1. Place one tablet of the iron-containing vitamin in a $125-\mathrm{mL}$ flask or $100-\mathrm{mL}$ beaker and boil gently (in a fume hood) with 25 mL of 6 M HCl for 15 min . Filter the solution directly into a

[^17]$100-\mathrm{mL}$ volumetric flask. Wash the beaker and filter several times with small portions of water to complete a quantitative transfer. Allow the solution to cool, dilute to the mark and mix well. Dilute 5.00 mL of this solution to 100.0 mL in a fresh volumetric flask. If the label indicates that the tablet contains $<15 \mathrm{mg}$ of Fe , use 10.00 mL instead of 5.00 mL .
2. Pipet 10.00 mL of standard Fe solution into a beaker and measure the pH (with pH paper or a glass electrode). Add sodium citrate solution 1 drop at a time until a pH of $\sim 3.5$ is reached. Count the drops needed. (It will require about 30 drops.)
3. Pipet a fresh $10.00-\mathrm{mL}$ aliquot of Fe standard into a $100-\mathrm{mL}$ volumetric flask and add the same number of drops of citrate solution as required in step 2. Add 2.00 mL of hydroquinone solution and 3.00 mL of $o$-phenanthroline solution, dilute to the mark with water, and mix well.
4. Prepare three more solutions from $5.00,2.00$, and 1.00 mL of Fe standard and prepare a blank containing no Fe . Use sodium citrate solution in proportion to the volume of Fe solution. (If 10 mL of Fe requires 30 drops of citrate solution, 5 mL of Fe requires 15 drops of citrate solution.)
5. Determine how many drops of citrate solution are needed to bring 10.00 mL of the iron tablet solution from step 1 to pH 3.5 . This will require about 3.5 or 7 mL of citrate, depending on whether 5 or 10 mL of unknown was diluted in the second part of step 1.
6. Transfer 10.00 mL of solution from step 1 to a $100-\mathrm{mL}$ volumetric flask. Add the required amount of citrate solution determined in step 5 . Then add 2.00 mL of hydroquinone solution and 3.0 mL of o-phenanthroline solution. Dilute to the mark and mix well.
7. Allow the solutions to stand for at least 10 min . Then measure the absorbance of each solution at 510 nm in a $1-\mathrm{cm}$ cell. (The color is stable, so all solutions may be prepared and all the absorbances measured at once.) Use distilled water in the reference cuvet and subtract the absorbance of the blank from the absorbance of the Fe standards.
8. Make a graph of absorbance versus micrograms of Fe in the standards. Find the slope and intercept (and standard deviations) by the method of least squares. Calculate the molarity of $\mathrm{Fe}(o$-phenanthroline $) 3^{2+}$ in each solution and find the average molar absorptivity ( $\varepsilon$ in Beer's law) from the four absorbances. (Remember that all the iron has been converted to the phenanthroline complex.)
9. Using the calibration curve, find the number of milligrams of Fe in the tablet. Use Equation 4-27 in the textbook to find the uncertainty in the number of milligrams of Fe .

## 21. Microscale Spectrophotometric Measurement of Iron in Foods by Standard Addition ${ }^{37}$



This microscale experiment uses the same chemistry as that of Experiment 20 to measure iron in foods such as broccoli, peas, cauliflower, spinach, beans, and nuts. A possible project is to compare processed (canned or frozen) vegetables to fresh vegetables. Instructions are provided for small volumes, but the experiment can be scaled up to fit available equipment. Section 5-3 in the textbook describes the method of standard addition.

## Reagents

2.0 M HCl: $15 \mathrm{~mL} /$ student. Dilute 165 mL of concentrated ( $37 \mathrm{wt} \%$ ) HCl up to 1 L .

Hydroquinone: $4 \mathrm{~mL} /$ student; prepared as in Experiment 20.
Trisodium citrate dehydrate: $4 \mathrm{~g} /$ student.
o-Phenanthroline: $4 \mathrm{~mL} /$ student; prepared as in Experiment 20.
Standard $\mathrm{Fe}(40 \mu \mathrm{~g} \mathrm{Fe} / \mathrm{mL}): 4 \mathrm{~mL} /$ student; prepared as in Experiment 20.
6 M HCl : Dilute 500 mL of $37 \mathrm{wt} \% \mathrm{HCl}$ up to 1 L with distilled water. Store in a bottle and reuse many times for soaking crucibles.

## Procedure

1. Fill a clean porcelain crucible with 6 M HCl in the hood and allow it to stand for 1 h to remove traces of iron from previous use. Rinse well with distilled water and dry. After weighing the empty crucible, add $5-6 \mathrm{~g}$ of finely chopped food sample and weigh again to obtain the mass of food. (Some foods, like frozen peas, should not be chopped because they will lose their normal liquid content.)
2. This step could require 3 h , during which you can be doing other lab work. Carefully heat the crucible with a Bunsen burner in a hood (Experiment 3, Figure 1). Use a low, flame to $d r y$ the sample, being careful to avoid spattering. Increase the flame temperature to char the sample. Keep the crucible lid and tongs nearby. If the sample bursts into flames, use tongs to place the lid on the crucible to smother the flame. After charring, use the hottest possible flame to ignite the black solid, converting it to white ash. The bottom of crucible should be red hot during ignition. Continue ignition until all traces of black disappear.

[^18]3. After cooling the crucible to room temperature, add 10.00 mL of 2.0 M HCl by pipet and swirl gently for 5 min to dissolve the ash. Filter the mixture through a small filter and collect the filtrate in a vial or small flask. You need to recover $>8 \mathrm{~mL}$ for the analysis.
4. Weigh 0.71 g of trisodium citrate dehydrate into each of four $10-\mathrm{mL}$ volumetric flasks. Using a 2-mL volumetric pipet or a $1-\mathrm{mL}$ micropipet, add 2.00 mL of ash solution to each flask. Add 4 mL of distilled water and swirl to dissolve the citrate. The solution will have a pH near 3.6. Using a micropipet, add 0.20 mL of hydroquinone solution and 0.30 mL of phenanthroline solution to each flask.
5. Label the volumetric flasks 0 through 3 . Add no Fe standard to flask 0 . Using a micropipet, add 0.250 mL of Fe standard to flask 1 . Add 0.500 mL of Fe standard to flask 2 and 0.750 mL to flask 3 . The four flasks now contain $0,1,2$, and $3 \mu \mathrm{gFe} / \mathrm{mL}$, in addition to Fe from the food. Dilute each to the mark with distilled water, mix well, and allow 15 min to develop full color.
6. Prepare a blank by mixing 0.71 g of trisodium citrate dehydrate, 2.00 mL of $2.0 \mathrm{M} \mathrm{HCl}, 0.20$ mL of hydroquinone solution, 0.30 mL of phenanthroline solution and diluting to 10 mL . The blank does not require a volumetric flask.
7. Measure the absorbance of each solution at 512 nm in a $1-\mathrm{cm}$ cell with distilled water in the reference cell. Before each measurement, remove all liquid from the cuvet with a Pasteur pipet. Then use $\sim 1 \mathrm{~mL}$ of your next solution (delivered with a clean, dry Pasteur pipet) to wash the cuvet. Remove and discard the washing. Repeat the washing once more with fresh solution and discard the washing. Finally, add your new solution to the cuvet for measuring absorbance.
8. Subtract the absorbance of the blank from each reading and make a graph like that in Figure 5-7 in the textbook to find the Fe content of the unknown solution. Calculate the wt $\%$ of Fe in the food. Use Equation 5-10 in the textbook to estimate the uncertainty in the $\mathrm{wt} \%$ of Fe in the food.

## 22. Spectrophotometric Measurement of an Equilibrium Constant



In this experiment, we use the Scatchard plot described in Section 19-2 of the textbook to find the equilibrium constant for the formation of a complex between iodine and pyridine in cyclohexane: 38


Both $I_{2}$ and $I_{2}$.pyridine absorb visible radiation, but pyridine is colorless. Analysis of the spectral changes associated with variation of pyridine concentration (with a constant total concentration of iodine) will allow us to evaluate $K$ for the reaction. The experiment is best performed with a recording spectrophotometer, but single-wavelength measurements can be used.

## Procedure

All operations should be carried out in a fume hood, including pouring solutions into and out of the spectrophotometer cell. Only a capped cuvette containing the solution whose spectrum is to be measured should be taken from the hood. Do not spill solvent on your hands or breathe the vapors. Used solutions should be discarded in a waste container in the hood, not down the drain.

1. The following stock solutions should be available in the lab:
a. $0.050-0.055 \mathrm{M}$ pyridine in cyclohexane ( 40 mL for each student, concentration known accurately).
b. $0.0120-0.0125 \mathrm{M} \mathrm{I}_{2}$ in cyclohexane ( 10 mL for each student, concentration known accurately).
2. Pipet the following volumes of stock solutions into six $25-\mathrm{mL}$ volumetric flasks labeled A-F, dilute to the mark with cyclohexane, and mix well.
[^19]| Flask | Pyridine stock <br> solution $(\mathrm{mL})$ | $\mathrm{I}_{2}$ stock <br> solution $(\mathrm{mL})$ |
| :---: | :---: | :---: |
| A | 0 | 1.00 |
| B | 1.00 | 1.00 |
| C | 2.00 | 1.00 |
| D | 4.00 | 1.00 |
| E | 5.00 | 1.00 |
| F | 10.00 | 1.00 |

3. Using glass or quartz cells, record a baseline between 350 and 600 nm with solvent in both the sample and the reference cells. Subtract the absorbance of the baseline from all future absorbances. If possible, record all spectra, including the baseline, on one sheet of chart paper. (If a fixed-wavelength instrument is used, first find the positions of the two absorbance maxima in solution E. Then make all measurements at these two wavelengths.)
4. Record the spectrum of each solution A-F or measure the absorbance at each maximum if a fixed-wavelength instrument is used.

## Data Analysis

1. Measure the absorbance at the wavelengths of the two maxima in each spectrum. Be sure to subtract the absorbance of the blank from each.
2. The analysis of this problem follows that of Reaction 19-10 in the textbook, in which $P$ is iodine and X is pyridine. As a first approximation, assume that the concentration of free pyridine equals the total concentration of pyridine in the solution (because [pyridine] >> $\left.\left[I_{2}\right]\right)$. Prepare a graph of $\Delta A /[$ free pyridine $]$ versus $\Delta A$ (a Scatchard plot), using the absorbance at the $I_{2}$ pyridine maximum.
3. From the slope of the graph, find the equilibrium constant by using Equation 19-16. From the intercept, find $\Delta \varepsilon\left(=\varepsilon_{P X}-\varepsilon_{X}\right)$.
4. Now refine the values of $K$ and $\Delta \varepsilon$. Use $\Delta \varepsilon$ to find $\varepsilon_{P X}$. Then use the absorbance at the wavelength of the $\mathrm{I}_{2} \cdot$ pyridine maximum to find the concentration of bound and free pyridine in each solution. Make a new graph of $\Delta A /[$ free pyridine] versus $\Delta A$, using the new values of [free pyridine]. Find a new value of $K$ and $\Delta \varepsilon$. If justified, perform another cycle of refinement.
5. Using the values of free pyridine concentration from your last refinement and the values of absorbance at the $I_{2}$ maximum, prepare another Scatchard plot and see if you get the same value of $K$.
6. Explain why an isosbestic point is observed in this experiment.

## 23. Spectrophotometric Analysis of a Mixture: Caffeine and Benzoic Acid in a Soft Drink ${ }^{39}$

In this experiment we use ultraviolet absorbance (Figure 1) to measure two major species in soft drinks. Caffeine is added as a stimulant and sodium benzoate is a preservative.


All solutions will contain 0.010 M HCl , so the sodium benzoate is protonated to make benzoic acid. Caffeine has no appreciable basicity, so it is neutral at pH 2.


Figure 1. Ultraviolet absorption of benzoic acid, caffeine, and a 1:50 dilution of Mountain Dew soft drink. All solutions contain 0.010 M HCl .

[^20]We restrict ourselves to non-diet soft drinks because the sugar substitute aspartame in diet soda has some ultraviolet absorbance that slightly interferes in the present experiment. We also avoid darkly colored drinks because the colorants have ultraviolet absorbance. Mountain Dew, Mello Yello, and, probably, other lightly colored drinks are suitable for this experiment. There is undoubtedly some ultraviolet absorbance from colorants in these beverages that contributes systematic error to this experiment.

The procedure we describe includes the construction of calibration curves. The experiment could be shortened by recording just one spectrum of caffeine ( $20 \mathrm{mg} / \mathrm{L}$ ) and one of benzoic acid ( $10 \mathrm{mg} / \mathrm{L}$ ) and assuming that Beer's law is obeyed. The experiment could be expanded to use high-performance liquid chromatography (HPLC) and/or capillary electrophoresis to obtain independent measurements of caffeine and benzoic acid (and aspartame in diet drinks). ${ }^{39}$

## Reagents

Stock solutions: An accurately known solution containing $\sim 100 \mathrm{mg}$ benzoic acid/L in water and another containing $\sim 200 \mathrm{mg}$ caffeine $/ \mathrm{L}$ should be available.
0.10 M HCl : Dilute 8.2 mL of $37 \mathrm{wt} \% \mathrm{HCl}$ to 1 L .

## Procedure

1. Calibration standards: Prepare benzoic acid solutions containing 2, 4, 6, 8 and $10 \mathrm{mg} / \mathrm{L}$ in 0.010 M HCl . To prepare a $2 \mathrm{mg} / \mathrm{L}$ solution, mix 2.00 mL of benzoic acid standard plus 10.0 mL of 0.10 M HCl in a $100-\mathrm{mL}$ volumetric flask and dilute to the mark with water. Use 4,6 , 8 and 10 mL of benzoic acid to prepare the other standards. In a similar manner, prepare caffeine standards containing $4,8,12,16$ and $20 \mathrm{mg} / \mathrm{L}$ in 0.010 M HCl .
2. Soft drink: Warm $\sim 20 \mathrm{~mL}$ of soft drink in a beaker on a hot plate to expel $\mathrm{CO}_{2}$ and filter the warm liquid through filter paper to remove any particles. After cooling to room temperature, pipet 4.00 mL into a $100-\mathrm{mL}$ volumetric flask. Add 10.0 mL of 0.10 M HCl and dilute to the mark. Prepare a second sample containing 2.00 mL of soft drink instead of 4.00 mL .
3. Verifying Beer's law: Record an ultraviolet baseline from 350 to 210 nm with water in the sample and reference cuvets ( 1.000 cm pathlength). Record the ultraviolet spectrum of each of the 10 standards with water in the reference cuvet. Note the wavelength of peak
absorbance for benzoic acid ( $\lambda^{\prime}$ ) and the wavelength for the peak absorbance of caffeine ( $\lambda^{\prime \prime}$ ). Measure the absorbance of each standard at both wavelengths and subtract the baseline absorbance (if your instrument does not do this automatically). Prepare a calibration graph of absorbance versus concentration (M) for each compound at each of the two wavelengths. Each graph should go through 0 . The least-squares slope of the graph is the molar absorptivity at that wavelength.
4. Unknowns: Measure the ultraviolet absorption spectrum of the $2: 100$ and $4: 100$ dilutions of the soft drink. With the absorbance at the wavelengths $\lambda^{\prime}$ and $\lambda^{\prime \prime}$, use Equation 19-6 in the textbook to find the concentrations of benzoic acid and caffeine in the original soft drink. Report results from both dilute solutions.
5. Synthetic unknown: If your instructor chooses, measure the spectrum of a synthetic, unknown mixture of benzoic acid and caffeine prepared by the instructor. Use Equation 19-6 in the textbook to find the concentration of each component in the synthetic unknown.

## 24. $\mathbf{M n}^{\mathbf{2 +}}$ Standardization by EDTA Titration



Experiments 24-26 illustrate a sequence in which students (1) prepare and standardize a $\mathrm{Mn}^{2+}$ solution by EDTA titration and then (2) use this standard in the analysis of Mn in steel by two different instrumental techniques. ${ }^{40}$

## Reagents

$\mathrm{MnSO}_{4} \cdot \mathrm{H}_{2} \mathrm{O}: \quad(1 \mathrm{~g} /$ student $)$ This material is not a primary standard.
EDTA: $\mathrm{Na}_{2} \mathrm{H}_{2} \mathrm{EDTA} \cdot 2 \mathrm{H}_{2} \mathrm{O}, 1 \mathrm{~g} /$ student.
$0.50 \mathrm{M} \mathrm{NH}_{3} / 1.1 \mathrm{M} \mathrm{NH}_{4}^{+} \operatorname{buffer}\left(\mathrm{pH} 9.7\right.$ ): Mix 6.69 g of $\mathrm{NH}_{4} \mathrm{Cl}$ (FM 53.49) plus 16.86 g of $28 \%$ aqueous $\mathrm{NH}_{3}$ (FM 17.03) with enough water to give a total volume of 250 mL .
Hydroxylamine hydrochloride: $\left(\mathrm{NH}_{3} \mathrm{OH}^{+} \mathrm{Cl}^{-}\right.$, FM 69.49$) 1 \mathrm{~g} /$ student. (CAUTION: Do not breathe dust from $\mathrm{NH}_{3} \mathrm{OH}^{+} \mathrm{Cl}^{-}$; avoid contact with skin and eyes.)
Calmagite indicator: Dissolve 0.05 g in $100 \mathrm{~mL} \mathrm{H}_{2} \mathrm{O}$.

## Procedure

1. Standard 0.005 M EDTA: Dry $\mathrm{Na}_{2} \mathrm{H}_{2}$ EDTA $\cdot 2 \mathrm{H}_{2} \mathrm{O}$ (FM 372.25 ) at $80^{\circ} \mathrm{C}$ for 1 h and cool in a desiccator. Accurately weigh out $\sim 0.93 \mathrm{~g}$ and dissolve it with heating in 400 mL of distilled water in a $500-\mathrm{mL}$ volumetric flask. Cool to room temperature, dilute to the mark, and mix well.
2. $\mathrm{Mn}^{2+}$ stock solution: Prepare a solution containing $\sim 1.0 \mathrm{mg} \mathrm{Mn} / \mathrm{mL}(\sim 0.018 \mathrm{M})$ by dissolving $\sim 0.77 \mathrm{~g} \mathrm{MnSO}_{4} \cdot \mathrm{H}_{2} \mathrm{O}$ (FM 169.01) in a clean plastic screw cap bottle with 250 mL water delivered from a graduated cylinder. Masses and volumes need not be accurate because you will standardize this solution.
3. Rinse a clean $50-\mathrm{mL}$ pipet several times with small volumes of $\mathrm{Mn}^{2+}$ stock solution and discard the washings into a chemical waste container. Then pipet 50.00 mL of $\mathrm{Mn}^{2+}$ stock solution into a $250-\mathrm{mL}$ volumetric flask. Add 0.80 g of solid hydroxylamine hydrochloride

[^21]to the flask, and swirl to dissolve the solid. Add $\sim 150 \mathrm{~mL}$ of water and swirl to mix the contents. Dilute to the mark with water, place the cap firmly in place, and invert 20 times to mix the solution. This solution contains $\sim 0.0036 \mathrm{M} \mathrm{Mn}^{2+}$. The reducing agent, hydroxylamine, maintains manganese in the +2 state.
4. Rinse a $50-\mathrm{mL}$ pipet several times with small volumes of the diluted $\mathrm{Mn}^{2+}$ solution from step 3. Pipet 50 mL of the diluted $\mathrm{Mn}^{2+}$ solution into a $250-\mathrm{mL}$ Erlenmeyer flask Add 10 mL of pH 9.7 buffer (by graduated cylinder), and add 3-5 drops of calmagite indicator. The pH of the solution will be near 9.2. Titrate with standard EDTA from a $50-\mathrm{mL}$ buret and note the end point when the color changes from wine red to blue.
5. Repeat step 4 twice more to obtain a total of three replicate titrations. The Erlenmeyer flask must be clean, but it need not be dry for each new titration.
6. From the molarity and volume of standard EDTA required for titration, calculate the molarity and standard deviation of the original $\sim 0.018 \mathrm{M} \mathrm{MnSO}_{4}$ stock solution. Express your answer with an appropriate number of significant digits.

## 25. Measuring Manganese in Steel by Spectrophotometry with Standard Addition



Experiments 24-26 illustrate a sequence in which students (1) prepare and standardize a $\mathrm{Mn}^{2+}$ solution and then (2) use this standard in the analysis of Mn in steel by two different instrumental techniques. ${ }^{41}$ In this experiment, steel is dissolved in acid and its Mn is oxidized to the violet colored permanganate ion, whose absorbance is measured with a spectrophotometer:

| $2 \mathrm{Mn}^{2+}$ |  |
| :---: | :---: |
| (colorless) | Periodate <br> (colorless) |
| $5 \mathrm{IO}_{4}^{-}$ |  |$+3 \mathrm{H}_{2} \mathrm{O} \rightarrow 2 \mathrm{MnO}+5 \mathrm{IO}_{3}^{-}+6 \mathrm{H}^{+}$

Steel is an alloy of iron that typically contains $\sim 0.5 \mathrm{wt} \% \mathrm{Mn}$ plus numerous other elements. When steel is dissolved in hot nitric acid, the iron is converted to Fe (III). Spectrophotometric interference in the measurement of $\mathrm{MnO}_{4}^{-}$by Fe (III) is minimized by adding $\mathrm{H}_{3} \mathrm{PO}_{4}$ to form a nearly colorless complex with $\mathrm{Fe}(\mathrm{III})$. Interference by most other colored impurities is eliminated by subtracting the absorbance of a reagent blank from that of the unknown. Appreciable Cr in the steel will interfere with the present procedure. Carbon from the steel is eliminated by oxidation with peroxydisulfate $\left(\mathrm{S}_{2} \mathrm{O}_{8}^{2-}\right)$ :

$$
\mathrm{C}(s)+2 \mathrm{~S}_{2} \mathrm{O}_{8}^{2-}+2 \mathrm{H}_{2} \mathrm{O} \rightarrow \mathrm{CO}_{2}(g)+4 \mathrm{SO}_{4}^{2-}+4 \mathrm{H}^{+}
$$

## Reagents

3 M Nitric acid: ( $150 \mathrm{~mL} / \mathrm{student)} \mathrm{Dilute} 190 \mathrm{~mL}$ of $70 \mathrm{wt} \% \mathrm{HNO}_{3}$ to 1 L with water. 0.05 M Nitric acid: ( $300 \mathrm{~mL} /$ student) Dilute 3.2 mL of $70 \mathrm{wt} \% \mathrm{HNO}_{3}$ to 1 L with water. Ammonium hydrogen sulfite: ( $0.5 \mathrm{~mL} /$ student) $45 \mathrm{wt} \% \mathrm{NH}_{4} \mathrm{HSO}_{3}$ in water.
Potassium periodate $\left(\mathrm{KIO}_{4}\right): 1.5 \mathrm{~g} /$ student.
Unknowns: Steel, $\sim 2 \mathrm{~g} /$ student. Analyzed samples are available from Thorn Smith. ${ }^{2}$

[^22]
## Procedure

1. Steel can be used as received or, if it appears to be coated with oil or grease, it should be rinsed with acetone and dried at $110^{\circ} \mathrm{C}$ for 5 min , and cooled in a desiccator.
2. Weigh duplicate samples of steel to the nearest 0.1 mg into 250 mL beakers. The mass of steel should be chosen to contain $\sim 2-4 \mathrm{mg}$ of Mn . For example, if the steel contains $0.5 \mathrm{wt} \%$ Mn , a $0.6-\mathrm{g}$ sample will contain 3 mg of Mn . Your instructor should give you guidance on how much steel to use.
3. Dissolve each steel sample separately in 50 mL of $3 \mathrm{M} \mathrm{HNO}_{3}$ by gently boiling in the hood, while covered with a watchglass. If undissolved particles remain, stop boiling after 1 h . Replace the $\mathrm{HNO}_{3}$ as it evaporates.
4. Standard $\mathrm{Mn}^{2+}(\sim 0.1 \mathrm{mg} \mathrm{Mn} / \mathrm{mL})$ : While the steel is dissolving, pipet 10.00 mL of standard $\mathrm{Mn}^{2+}(\sim 1 \mathrm{mg} \mathrm{Mn} / \mathrm{mL})$ from Experiment 24 into a $100-\mathrm{mL}$ volumetric flask, dilute to the mark with water, and mix well. You will use this solution in Experiments 25 and 26. Keep it stoppered, and wrap the stopper with Parafilm or tape to minimize evaporation.
5. Cool the beakers from step 3 for 5 min . Then carefully add $\sim 1.0 \mathrm{~g}$ of $\left(\mathrm{NH}_{4}\right)_{2} \mathrm{~S}_{2} \mathrm{O}_{8}$ or $\mathrm{K}_{2} \mathrm{~S}_{2} \mathrm{O}_{8}$ and boil for 15 min to oxidize carbon to $\mathrm{CO}_{2}$.
6. If traces of pink color $\left(\mathrm{MnO}_{4}^{-}\right)$or brown precipitate $\left(\mathrm{MnO}_{2}\right)$ are observed, add 6 drops of 45 $\mathrm{wt} \% \mathrm{NH}_{4} \mathrm{HSO}_{3}$ and boil for 5 min to reduce all manganese to $\mathrm{Mn}(\mathrm{II})$ :

$$
\begin{gathered}
2 \mathrm{MnO}_{4}^{-}+5 \mathrm{HSO}_{3}^{-}+\mathrm{H}^{+} \rightarrow 2 \mathrm{Mn}^{2+}+5 \mathrm{SO}_{4}^{2-}+3 \mathrm{H}_{2} \mathrm{O} \\
\mathrm{MnO}_{2}(\mathrm{~s})+\mathrm{HSO}_{3}^{-}+\mathrm{H}^{+} \rightarrow \mathrm{Mn}^{2+}+\mathrm{SO}_{4}^{2-}+\mathrm{H}_{2} \mathrm{O}
\end{gathered}
$$

(The purpose of removing colored species at this time is that the solution from step 6 is eventually going to serve as a colorimetric reagent blank.)
7. After cooling the solutions to near room temperature, filter each solution quantitatively through \#41 filter paper into a $250-\mathrm{mL}$ volumetric flask. (If gelatinous precipitate is present, use \#42 filter paper.) To complete a "quantitative" transfer, wash the beaker many times with small volumes of hot $0.05 \mathrm{M} \mathrm{HNO}_{3}$ and pass the washings through the filter to wash liquid from the precipitate into the volumetric flask. Finally, allow the volumetric flasks to cool to room temperature, dilute to the mark with water, and mix well.
8. Transfer $\sim 100 \mathrm{~mL}$ of solution from each $250-\mathrm{mL}$ volumetric flask to clean, dry Erlenmeyer flasks and stopper the flasks tightly. Label these solutions A and B and save them for atomic
absorption analysis in Experiment 26. To help prevent evaporation, it is a good idea to seal around the stoppers with a few layers of Parafilm or tape.
9. Carry out the following spectrophotometric analysis with one of the unknown steel solutions prepared in step 7:
a. Pipet 25.00 mL of liquid from the $250-\mathrm{mL}$ volumetric flask in step 7 into each of three clean, dry $100-\mathrm{mL}$ beakers designated "blank," "unknown," and "standard addition." Add 5 mL of $85 \mathrm{wt} \% \mathrm{H}_{3} \mathrm{PO}_{4}$ (from a graduated cylinder) into each beaker. Then add standard $\mathrm{Mn}^{2+}\left(0.1 \mathrm{mg} / \mathrm{mL}\right.$ from step 4 , delivered by pipet) and solid $\mathrm{KIO}_{4}$ as follows:

| Beaker | Volume of <br> $\mathrm{Mn}^{2+}(\mathrm{mL})$ | Mass of <br> $\mathrm{KIO}_{4}(\mathrm{~g})$ |
| :--- | :---: | :---: |
| Blank | 0 | 0 |
| Unknown | 0 | 0.4 |
| Standard addition | 5.00 | 0.4 |

b. Boil the unknown and standard addition beakers gently for 5 min to oxidize $\mathrm{Mn}^{2+}$ to $\mathrm{MnO}_{4}^{-}$. Continue boiling, if necessary, until the $\mathrm{KIO}_{4}$ dissolves.
c. Quantitatively transfer the contents of each of the three beakers into $50-\mathrm{mL}$ volumetric flasks. Wash each beaker many times with small portions of water and transfer the water to the corresponding volumetric flask. Dilute each flask to the mark with water and mix well.
d. Fill one $1.000-\mathrm{cm}$-pathlength cuvet with unknown solution and another cuvet with blank solution. It is always a good idea to rinse the cuvet a few times with small quantities of the solution to be measured and discard the rinses.
e. Measure the absorbance of the unknown at 525 nm with blank solution in the reference cuvet. For best results, measure the absorbance at several wavelengths to locate the maximum absorbance. Use this wavelength for subsequent measurements.
f. Measure the absorbance of the standard addition with the blank solution in the reference cuvet. The absorbance of the standard addition will be $\sim 0.45$ absorbance units greater than the absorbance of the unknown (based on adding $\sim 0.50 \mathrm{mg}$ of standard $\mathrm{Mn}^{2+}$ to the unknown).
10. Repeat step 9 with the other unknown steel solution from step 7 .

## Data Analysis

1. From the known concentration of the Mn standard in step 4 , calculate the concentration of added Mn in the $50-\mathrm{mL}$ volumetric flask containing the standard addition.
2. All of the $\mathrm{Mn}^{2+}$ is converted to $\mathrm{MnO}_{4}^{-}$in step 9. From the difference between the absorbance of the standard addition and the unknown, calculate the molar absorptivity of $\mathrm{MnO}_{4}^{-}$. Compute the average molar absorptivity from steps 9 and 10.
3. From the absorbance of each unknown and the average molar absorptivity of $\mathrm{MnO}_{4}^{-}$, calculate the concentration of $\mathrm{MnO}_{4}^{-}$in each $50-\mathrm{mL}$ unknown solution.
4. Calculate the weight percent of Mn in each unknown steel sample and the percent relative range of your results:

$$
\% \text { relative range }=\frac{100 \times[\mathrm{wt} \% \text { in steel } 1-\mathrm{wt} \% \text { in steel } 2]}{\text { mean } \mathrm{wt} \%}
$$

## 26. Measuring Manganese in Steel by Atomic Absorption Using a Calibration Curve



This experiment complements the results of the spectrophotometric analysis in Experiment 25.42 In principle, the spectrophotometric analysis and the atomic absorption analysis should give the same value for the weight percent of Mn in the unknown steel. You will use $\mathrm{Mn}^{2+}$ that you standardized in Experiment 24 as the standard for the atomic absorption analysis.

## Reagents

0.05 M Nitric acid: ( $600 \mathrm{~mL} /$ student) Dilute 3.2 mL of $70 \mathrm{wt} \% \mathrm{HNO}_{3}$ to 1 L with water. Unknown steel: Solutions A and B from step 8 of Experiment 25.

Standard manganese: $\sim 0.1 \mathrm{mg} \mathrm{Mn} / \mathrm{mL}$ from step 4 of Experiment 25. This concentration corresponds to $\sim 100 \mu \mathrm{~g} / \mathrm{mL}=\sim 100 \mathrm{ppm}$.

## Calibration Curve

1. Prepare standard solutions containing $\sim 1,2,3,4$ and $5 \mathrm{ppm} \mathrm{Mn}(=\mu \mathrm{g} \mathrm{Mn} / \mathrm{mL})$. Use your standard solution containing $\sim 100 \mathrm{ppm}$ Mn from step 4 of Experiment 25. Pipet 1.00 mL of the standard into a $100-\mathrm{mL}$ volumetric flask and dilute to 100 mL with $0.05 \mathrm{M} \mathrm{HNO}_{3}$ to prepare a 1-ppm standard. Similarly, pipet $2.00,3.00,4.00$, and 5.00 mL into the other flasks and dilute each to 100 mL with $0.05 \mathrm{M} \mathrm{HNO}_{3}$. Calculate the concentration of Mn in $\mu \mathrm{g} / \mathrm{mL}$ in each standard. (The purpose of the $\mathrm{HNO}_{3}$ is to provide $\mathrm{H}^{+}$ions to compete with $\mathrm{Mn}^{2+}$ ions for binding sites on the glass surface. Without excess acid, some fraction of metal ions from a dilute solution can be lost to the glass surface. To avoid adding impurity metal ions, we use a dilute solution of the purest available acid.)
2. Measure the atomic absorption signal from each of the five standards in step 1. Use a Mn hollow cathode lamp and a wavelength of 279.48 nm . Measure each standard three times.

[^23]3. Measure the atomic absorption signal from a blank $\left(0.05 \mathrm{M} \mathrm{HNO}_{3}\right)$. We will use this signal later to estimate the detection limit from Mn. For this purpose, measure a blank seven separate times and compute the mean and standard deviation of the seven measurements.

## Measuring the Unknown

1. Immediately after measuring the points on the calibration curve, measure the atomic absorption signal from unknown steel solutions A and B from step 8 of Experiment 25. Measure the absorption of each solution three times. (If the signals from $A$ and $B$ do not lie in the calibration range, dilute them as necessary so that they do lie in the calibration range. Dilutions must be done accurately with volumetric pipets and volumetric flasks.)

## Data Analysis

1. Make a calibration graph showing the blank plus 5 standards ( 7 blank readings and $3 \times 5=$ 15 standard readings, for a total of $n=22$ points). Compute the least-squares slope and intercept and their standard deviations (Section 4-7 of the textbook) and show the leastsquares line on the graph. Express the equation of the calibration curve in the form $y\left( \pm s_{\mathrm{y}}\right)=$ $\left[m\left( \pm s_{m}\right)\right] x+\left[b\left( \pm \mathrm{s}_{\mathrm{b}}\right)\right]$, where $y$ is the atomic absorbance signal and $x$ is the concentration of Mn in ppm .
2. Use the mean value of the three readings for each unknown to calculate the concentration of Mn solutions A and B.
3. Calculate the uncertainty in Mn concentration in each unknown from Equation 4-27 in the textbook. Because you have measured each unknown three times, the first term in the radical in Equation 4-27 should be $1 / 3$. In Equation 4-27, there are 22 values of $x_{i}$ for the points on the standard curve.
4. From the Mn concentrations (and uncertainties) in solutions A and B, calculate the $\mathrm{wt} \% \mathrm{Mn}$ (and its uncertainty) in the two replicate steel samples.
5. The uncertainty in $\mathrm{wt} \% \mathrm{Mn}$ is the standard deviation. Find the $95 \%$ confidence interval for $\mathrm{wt} \% \mathrm{Mn}$ in each of the two steel samples that you analyzed. For example, suppose that you find the $\mathrm{wt} \%$ of Mn in steel to be 0.43 , with a standard deviation of $0.01_{1}$. (The subscripted digits are not significant but are retained to avoid round-off errors.) The standard deviation
was derived from three replicate measurements of one solution of dissolved steel. The equation for confidence interval is $\mu=\bar{x} \pm t s / \sqrt{n}$, where $\mu$ is the true mean, $\bar{x}$ is the measured mean, $s$ is the standard deviation, $n$ is the number of measurements ( 3 in this case) and $t$ is Student's $t$ for $95 \%$ confidence and $n-1=2$ degrees of freedom. In Table 4-4 of the textbook we find $t=4.303$. Therefore the $95 \%$ confidence interval is $0.43_{3} \pm t s / \sqrt{n}=0.43_{3}$ $\pm(4.303)\left(0.01_{1}\right) / \sqrt{3}=0.43_{3} \pm 0.027$.
6. Use the $t$ test (Equation 4-9 in the textbook) to compare the two atomic absorption results to each other. Are they significantly different at the $95 \%$ confidence level?
7. Use the mean $\mathrm{wt} \% \mathrm{Mn}$ for the two samples and the pooled standard deviation (Equation 4-10 in the textbook) to estimate a $95 \%$ confidence interval around the mean value. Does the mean spectrophotometric value for $\mathrm{wt} \% \mathrm{Mn}$ from Experiment 25 lie within the $95 \%$ confidence interval for the atomic absorption results? (We cannot use the $t$ test to compare Experiments 25 and 26 because we do not have enough samples in Experiment 25 to find a standard deviation. Otherwise, we would use the $t$ test.)
8. Detection limit: The detection limit of an analytical method is the minimum concentration of analyte that can be "reliably" distinguished from 0 . Different statistical criteria for the word "reliably" lead to different definitions of detection limit. If you have measured points on a calibration curve, one common definition of detection limit is

$$
\text { Detection limit }(\mathrm{ppm})=\frac{\bar{y}_{\mathrm{B}}+3 s_{\mathrm{B}}}{m}
$$

where $\bar{y}_{\mathrm{B}}$ is the mean atomic absorbance reading for the blank, $s_{\mathrm{B}}$ is the standard deviation for the blank, and $m$ is the least-squares slope of the calibration curve (absorbance/ppm). In this experiment you measured a blank solution seven times. Use the mean and standard deviation from these seven readings to calculate the detection limit. (If you subtracted the mean value of the blank from each absorbance reading when you constructed the standard curve, then $\bar{y}_{\mathrm{B}}=0$.)

## 27. Properties of an Ion-Exchange Resin ${ }^{43}$



In this experiment, we explore the properties of a cation-exchange resin, which is an organic polymer containing many sulfonic acid groups $\left(-\mathrm{SO}_{3} \mathrm{H}\right)$. When a cation, such as $\mathrm{Cu}^{2+}$, flows into the resin, the cation is tightly bound by sulfonate groups, and one $\mathrm{H}^{+}$is released for each positive charge bound to the resin. The bound cation can be displaced from the resin by a large excess of $\mathrm{H}^{+}$or by an excess of any other cation for which the resin has some affinity.


In the first part of the experiment, known quantities of $\mathrm{NaCl}, \mathrm{Fe}\left(\mathrm{NO}_{3}\right)_{3}$, and NaOH will be passed through the resin in the $\mathrm{H}^{+}$form. The $\mathrm{H}^{+}$released by each cation will be measured by titration with NaOH .

In the second part, we will analyze a sample of impure vanadyl sulfate $\left(\mathrm{VOSO}_{4} \cdot 2 \mathrm{H}_{2} \mathrm{O}\right)$. As supplied commercially, this salt contains $\mathrm{VOSO}_{4}, \mathrm{H}_{2} \mathrm{SO}_{4}$, and $\mathrm{H}_{2} \mathrm{O}$. A solution will be prepared from a known mass of reagent. The $\mathrm{VO}^{2+}$ content can be assayed spectrophotometrically, and the total cation $\left(\mathrm{VO}^{2+}\right.$ and $\left.\mathrm{H}^{+}\right)$content can be assayed by ion exchange. Together, these measurements enable us to establish the quantities of $\mathrm{VOSO}_{4}, \mathrm{H}_{2} \mathrm{SO}_{4}$, and $\mathrm{H}_{2} \mathrm{O}$ in the sample.

## Reagents

0.3 M NaCl : A bottle containing $5-10 \mathrm{~mL}$ per student, with an accurately known concentration.
0.1 $\mathrm{M} \mathrm{Fe}\left(\mathrm{NO}_{3}\right)_{3} \cdot 6 \mathrm{H}_{2} \mathrm{O}$ : A bottle containing $5-10 \mathrm{~mL}$ per student, with an accurately known concentration.
$\mathrm{VOSO}_{4}$ : The commonly available grade (usually designated "purified") is used for this experiment. Students can make their own solutions and measure the absorbance at 750 nm ,

[^24]or a bottle of stock solution ( 25 mL per student) can be supplied. The stock should contain $8 \mathrm{~g} / \mathrm{L}$ (accurately weighed) and be labeled with the absorbance.
0.02 M NaOH : Each student should prepare an accurate $1 / 5$ dilution of standard 0.1 M NaOH .

Phenolphthalein indicator: Dissolve 50 mg of the indicator in 50 mL of ethanol and add $50 \mathrm{~mL} \mathrm{H} \mathrm{H}_{2} \mathrm{O}$.

## Procedure

1. Prepare a chromatography column from a $0.7-\mathrm{cm}$ diameter $\times 15-\mathrm{cm}$ length of glass tubing, fitted at the bottom with a cork having a small hole that serves as the outlet. Place a small ball of glass wool above the cork to retain the resin. Use a small glass rod to plug the outlet and shut off the column. (Alternatively, an inexpensive column such as $0.7 \times 15 \mathrm{~cm}$ EconoColumn from Bio-Rad Laboratories ${ }^{44}$ works well in this experiment.) Fill the column with water, close it off, and test for leaks. Then drain the water until 2 cm remains and close the column again.
2. Make a slurry of 1.1 g of Bio-Rad Dowex $50 \mathrm{~W}-\mathrm{X} 2$ (100/200 mesh) cation-exchange resin in 5 mL of water and pour it into the column (Figure 1). If the resin cannot be poured all at once, allow some to settle, remove the supernatant liquid with a pipet, and pour in the rest of the resin. If the column is stored between laboratory periods, it should be upright, capped, and contain water above the level of the resin. (When the experiment is finished, the resin can be collected, washed with 1 M HCl and water, and reused.)
3. The general procedure for analysis of a sample is as follows:
a. Generate the $\mathrm{H}^{+}$-saturated resin by passing $\sim 10 \mathrm{~mL}$ of 1 M HCl through the column. Apply the liquid sample to the glass wall so as not to disturb the resin.
b. Wash the column with $\sim 15 \mathrm{~mL}$ of water. Use the first few milliliters to wash the glass walls and allow the water to soak into the resin before continuing the washing. (Unlike most other chromatography resins, the one used in this experiment retains water when allowed to run "dry." Ordinarily, you must not let liquid fall below the top of the solid phase in a chromatography column.)
c. Place a clean $125-\mathrm{mL}$ flask under the outlet and pipet the sample onto the column.

[^25]

Figure 1. Pouring a slurry of stationary phase into a chromatography column.
d. After the reagent has soaked in, wash it through with 10 mL of $\mathrm{H}_{2} \mathrm{O}$, collecting all eluate.
e. Add 3 drops of phenolphthalein to the flask and titrate with standard 0.02 M NaOH .
4. Analyze $2.000-\mathrm{mL}$ aliquots of 0.3 M NaCl and $0.1 \mathrm{M} \mathrm{Fe}\left(\mathrm{NO}_{3}\right)_{3}$, following the procedures in step 3. Calculate the theoretical volume of NaOH needed for each titration. If you do not come within $2 \%$ of this volume, repeat the analysis.
5. Pass 10.0 mL of your 0.02 M NaOH through the column as in step 3, and analyze the eluate. Explain what you observe.
6. Analyze 10.00 mL of $\mathrm{VOSO}_{4}$ solution as described in step 3 .
7. Using the molar absorptivity of vanadyl ion $\left(\varepsilon=18.0 \mathrm{M}^{-1} \cdot \mathrm{~cm}^{-1}\right.$ at 750 nm$)$ and the results of step 6, express the composition of the vanadyl sulfate in the form

$$
\left(\mathrm{VOSO}_{4}\right)_{1.00}\left(\mathrm{H}_{2} \mathrm{SO}_{4}\right)_{x}\left(\mathrm{H}_{2} \mathrm{O}\right)_{y} .
$$

## 28. Analysis of Sulfur in Coal by Ion Chromatography ${ }^{45}$



When coal is burned, sulfur in the coal is converted to $\mathrm{SO}_{2}(g)$, which is further oxidized to $\mathrm{H}_{2} \mathrm{SO}_{4}$ in the atmosphere. Rainfall laden with $\mathrm{H}_{2} \mathrm{SO}_{4}$ is harmful to plant life. Measuring the sulfur content of coal is therefore important to efforts to limit man-made sources of acid rain. This experiment measures sulfur in coal by first heating the coal in the presence of air in a flux containing $\mathrm{Na}_{2} \mathrm{CO}_{3}$ and MgO , which converts the sulfur to $\mathrm{Na}_{2} \mathrm{SO}_{4}$. The product is dissolved in water, and sulfate ion is measured by ion chromatography. Although you will be given a sample of coal to analyze, consider how you would obtain a representative sample from an entire trainload of coal being delivered to a utility company.

## Reagents

Coal: $1 \mathrm{~g} /$ student. Coal can be obtained from electric power companies and some heavy industries. Coal is also available as a Standard Reference Material. ${ }^{46}$

Flux: $4 \mathrm{~g} /$ student. $67 \mathrm{wt} \% \mathrm{MgO} / 33 \mathrm{wt} \% \mathrm{Na}_{2} \mathrm{CO} 3$.
$6 \mathrm{M} \mathrm{HCl}: ~ 25 \mathrm{~mL} /$ student.
Phenolphthalein indicator: Dissolve 50 mg of solid indicator in 50 mL of ethanol and add $50 \mathrm{~mL} \mathrm{H}_{2} \mathrm{O}$.

Ammonium sulfate: Solid reagent for preparing standards.

## Procedure

1. Grind the coal to a fine powder with a mortar and pestle. Mix 1 g of coal (accurately weighed) with $\sim 3 \mathrm{~g}$ of flux in a porcelain crucible. Mix thoroughly with a spatula and tap the crucible to pack the powder. Gently cover the mixture with $\sim 1 \mathrm{~g}$ of additional flux. Cover the crucible and place it in a muffle furnace. Then turn on the furnace and set the temperature to $800^{\circ} \mathrm{C}$ and leave the sample in the furnace at $800^{\circ} \mathrm{C}$ overnight. The reaction
2. E. Koubek and A. E. Stewart, J. Chem. Ed. 1992, 69, A146.
3. Standards containing $0.5-5 \mathrm{wt} \% \mathrm{~S}$ are available from NIST Standard Reference Materials Program (SRMINFO@enh.nist.gov).
is over when all black particles have disappeared. A burner can be used in place of the furnace, but the burner should not be left unattended overnight.
4. After cooling to room temperature, place the crucible into a $150-\mathrm{mL}$ beaker and add 100 mL of distilled water. Heat the beaker on a hot plate to just below boiling for 20 min to dissolve as much solid as possible. Pour the liquid through filter paper in a conical funnel directly into a $250-\mathrm{mL}$ volumetric flask. Wash the crucible and beaker three times with $25-\mathrm{mL}$ portions of distilled water and pour the washings through the filter. Add 5 drops of phenolphthalein indicator to the flask and neutralize with 6 M HCl until the pink color disappears. Dilute to 250 mL and mix well.
5. Pipet 25.00 mL of sulfate solution from the $250-\mathrm{mL}$ volumetric flask in step 2 into a $100-\mathrm{mL}$ volumetric flask and dilute to volume to prepare a fourfold dilution for ion chromatography. Inject a sample of this solution into an ion chromatograph ${ }^{47}$ to be sure that the concentration is in a reasonable range for analysis. More or less dilution may be necessary. Prepare the correct dilution for your equipment.
6. Assuming that the coal contains $3 \mathrm{wt} \%$ sulfur, calculate the concentration of $\mathrm{SO}_{4}^{2-}$ in the solution in step 3. Using ammonium sulfate and appropriate volumetric glassware, prepare five standards containing $0.1,0.5,1.0,1.5$, and 2.0 times the calculated concentration of $\mathrm{SO}_{4}^{2-}$ in the unknown.
7. Analyze all solutions by ion chromatography. Prepare a calibration curve from the standards, plotting peak area versus $\mathrm{SO}_{4}^{2-}$ concentration. Use the least-squares fit to find the concentration of $\mathrm{SO}_{4}^{2-}$ in the unknown. Calculate the $\mathrm{wt} \%$ of S in the coal.
8. For example, chromatography can be done with $25-50 \mu \mathrm{~L}$ of sample on a 4 -mm-diameter $\times 250$-mm-long Dionex Ionpac AS5 analytical column and an AG5 guard column using $2.2 \mathrm{mM} \mathrm{Na}_{2} \mathrm{CO}_{3} / 2.8 \mathrm{mM} \mathrm{NaHCO} 3$ eluent at $2.0 \mathrm{~mL} / \mathrm{min}$ with ion suppression. $\mathrm{SO}_{4}^{2-}$ is eluted near 6 min and is detected by its conductivity on a full-scale setting of 30 microsiemens. Many combinations of column and eluent are suitable for this analysis.

## 29. Measuring Carbon Monoxide in Automobile Exhaust by Gas Chromatography ${ }^{48}$



Carbon monoxide is a colorless, odorless, poisonous gas emitted from automobile engines because of incomplete combustion of fuel to $\mathrm{CO}_{2}$. A well-tuned car with a catalytic converter might emit 0.01 vol $\% \mathrm{CO}$, whereas a poorly maintained car could emit as much as $15 \mathrm{vol} \% \mathrm{CO}$ ! In this experiment you will collect samples of auto exhaust and measure the CO content by gas chromatography. A possible class project is to compare different types of cars and different states of maintenance of vehicles. CO emission is greatest within the first few minutes after starting a cold engine. After warm-up, a well-tuned vehicle may emit too little CO to detect with an inexpensive gas chromatograph. CO can be measured as a function of time after start-up.

Chromatography is performed at $50-60^{\circ} \mathrm{C}$ with a $2-\mathrm{m}$-long packed column containing 5 A molecular sieves with He carrier gas and thermal conductivity detection. The column should be flushed periodically by disconnecting it from the detector and flowing He through for 30 h . Flushing after 50-100 injections desorbs $\mathrm{H}_{2} \mathrm{O}$ and $\mathrm{CO}_{2}$ from the sieves.

## Reagents

CO gas standard: Lecture bottle containing $1 \mathrm{vol} \% \mathrm{CO}$ in $\mathrm{N}_{2} .49$

## Reagents

1. Attach with heavy tape a heat-resistant hose to the exhaust pipe of a car. (Caution: Avoid breathing the exhaust.) Use the free end of the hose to collect exhaust in a heavy-walled, $0.5-\mathrm{L}$ plastic zipper-type bag from the grocery. Flush the bag well with exhaust before sealing it tightly. Allow the contents to come to room temperature for analysis.
2. Inject a $1-\mathrm{mL}$ sample of air into the gas chromatograph by using a gas-tight syringe and adjust the temperature and/or flow rate if necessary so that $\mathrm{N}_{2}$ is eluted within 2 min . You should see peaks for $\mathrm{O}_{2}$ and $\mathrm{N}_{2}$.

[^26]3. Inject $1.00-\mathrm{mL}$ of standard $1 \mathrm{vol} \% \mathrm{CO}$ in $\mathrm{N}_{2}$. One way to obtain gas from a lecture bottle is to attach a hose to the tank (in a hood) with a serum stopper on a glass tube at the end of the hose (Figure 1). Place a needle in the serum stopper and slowly bleed gas from the tank to flush the hose. Insert a gas-tight syringe into the serum stopper, remove the vent needle, and slowly withdraw gas into the syringe. Then close the tank to prevent pressure buildup in the tubing. When you inject the standard into the chromatograph, you should see a peak for CO with about three times the retention time of $\mathrm{N}_{2}$. Adjust the detector attenuation so the CO peak is near full scale. Reinject the standard twice and measure the peak area each time.


Figure 1. Collecting a sample of standard gas mixture from a lecture bottle. Remove the vent needle when withdrawing gas into the syringe. Do not open the tank valve so much that the connections pop open. (CAUTION: Handle CO only in a hood.)
4. Inject two $1.00-\mathrm{mL}$ samples of auto exhaust and measure the peak area each time. Compute the $\mathrm{vol} \%$ of CO in the unknown from its average peak area:

$$
\frac{\mathrm{vol} \% \mathrm{CO} \text { in the unknown }}{\text { vol } \% \mathrm{CO} \text { in the standard }}=\frac{\text { peak area of unknown/detector attenuation }}{\text { peak area of standard/detector attenuation }}
$$

## 30. Amino Acid Analysis by Capillary Electrophoresis ${ }^{50}$


(NDA, FM 184.19)

The mixture will then be separated by capillary electrophoresis, and the quantity of each component will be measured relative to that of the internal standard. The goal is to find the relative number of each amino acid in the protein.

## Reagents

Protein: $6 \mathrm{mg} /$ student. Use a pure protein such as lysozyme or cytochrome $c$. The amino acid content should be available in the literature for you to compare with your results. ${ }^{51}$

6 M HCI : Dilute 124 mL of concentrated ( $37 \mathrm{wt} \%$ ) HCl up to 250 mL with distilled water.
$0.05 \mathrm{M} \mathrm{NaOH}:$ Dissolve 0.50 g of NaOH (FM 40.00) in 250 mL of distilled water.
$1.5 \mathrm{M} \mathrm{NH}_{3}$ : Dilute 26 mL of $28 \mathrm{wt} \% \mathrm{NH}_{3}$ up to 250 mL with distilled water.
10 mM KCN : Dissolve 16 mg of KCN (FM 65.12) in 25 mL of distilled water.
50. P. L. Weber and D. R. Buck, J. Chem. Ed. 1994, 71, 609.
51. Abbreviations for amino acids are given in Table 10-1 of the textbook. For hen egg white lysozyme, the amino acid content is

$$
\mathrm{S}_{10} \mathrm{~T}_{7} \mathrm{H}_{1} \mathrm{G}_{12} \mathrm{~A}_{12}\left(\mathrm{E}_{2} \mathrm{Q}_{3}\right) \mathrm{Y}_{3}\left(\mathrm{D}_{8} \mathrm{~N}_{13}\right) \mathrm{V}_{6} \mathrm{M}_{2} \mathrm{I}_{6} \mathrm{~L}_{8} \mathrm{~F}_{3} \mathrm{R}_{11} \mathrm{~K}_{6} \mathrm{C}_{8} \mathrm{~W}_{8} \mathrm{P}_{2}
$$

(R. E. Canfield and A. K. Liu, J. Biol. Chem. 1965, 240, 2000; D. C. Philips, Scientific American, May 1966.) For horse cytochrome $c$, the composition is

$$
\mathrm{S}_{0} \mathrm{~T}_{10} \mathrm{H}_{3} \mathrm{G}_{12} \mathrm{~A}_{6}\left(\mathrm{E}_{9} \mathrm{Q}_{3}\right) \mathrm{Y}_{4}\left(\mathrm{D}_{3} \mathrm{~N}_{5}\right) \mathrm{V}_{3} \mathrm{M}_{2} \mathrm{I}_{6} \mathrm{~L}_{6} \mathrm{~F}_{4} \mathrm{R}_{2} \mathrm{~K}_{19} \mathrm{C}_{2} \mathrm{~W}_{1} \mathrm{P}_{4}
$$

(E. Margoliash and A. Schejter, Adv. Protein Chem. 1966, 21, 114.) Both proteins are available from www.sigmaaldrich.com.

Borate buffer ( pH 9.0 ): To prepare 20 mM buffer, dissolve 0.19 g of sodium tetraborate $\left(\mathrm{Na}_{2} \mathrm{~B}_{4} \mathrm{O}_{7} \cdot 10 \mathrm{H}_{2} \mathrm{O}\right.$, FM 381.37) in 70 mL of distilled water. Using a pH electrode, adjust the pH to 9.0 with 0.3 M HCl (a 1:20 dilution of 6 M HCl with distilled water) and dilute to 100 mL with distilled water.

Run buffer (20 mM borate-50 mM sodium dodecyl sulfate, pH 9.0): Prepare this as you prepared borate buffer but add 1.44 g of $\mathrm{CH}_{3}\left(\mathrm{CH}_{2}\right)_{11} \mathrm{OSO}_{3} \mathrm{Na}$ (FM 288.38) prior to adjusting the pH with HCl .

Amino acids: Prepare 100 mL of standard solution containing all 15 of the amino acids in Figure 1, each at a concentration near 2.5 mM in a solvent of 0.05 M NaOH . Table 10-1 in the textbook gives molecular masses of amino acids.


Figure 1. Electropherogram of standard mixture of NDA-derivatized amino acids plus internal standard, all at equal concentrations, from P. L. Weber and D. R. Buck, J. Chem. Ed. 1994, 71, 609. Abbreviations for amino acids are given in Table 10-1 in the textbook. The internal standard, designated X , is $\alpha$-aminoadipic acid. U is an unidentified peak. Acid hydrolysis converts Q into E and converts N into D , so Q and N are not observed. The analysis of lysine $(\mathrm{K})$ is not reliable because its NDA derivative is unstable. Cysteine (C) and tryptophan (W) are degraded during acid hydrolysis and are not observed. Proline $(\mathrm{P})$ is not a primary amine, so it does not react with NDA to form a detectable product.
$\alpha$ - Aminoadipic acid internal standard: Prepare a 5 mM solution by dissolving 40 mg of $\mathrm{HO}_{2} \mathrm{C}\left(\mathrm{CH}_{2}\right)_{3} \mathrm{CH}\left(\mathrm{NH}_{2}\right) \mathrm{CO}_{2} \mathrm{H}$ (FM 161.16) in 50 mL of distilled water.

Naphthalene-2,3-dicarboxaldehyde (NDA): Prepare a 10 mM solution by dissolving 18 mg of NDA in 10 mL of acetonitrile.

## Hydrolysis of the Protein

1. Fit a rubber septum onto a glass tube $(17 \times 55 \mathrm{~mm})$ that is sealed at one end and evacuate it through a needle. Dissolve 6 mg of protein in 0.5 mL of 6 M HCl in a small vial. Purge the solution with $\mathrm{N}_{2}$ for 1 min to remove $\mathrm{O}_{2}$ and immediately transfer the liquid by syringe into the evacuated tube. Add 0.5 mL of fresh HCl to the vial, purge, and transfer again into the tube. Heat the part of the glass tube containing the liquid at $100-110^{\circ} \mathrm{C}$ in an oil bath for 18-24 h, preferably behind a shield.
2. After cooling, remove the septum and transfer the liquid to a $25-\mathrm{mL}$ round-bottom flask. Evaporate the solution to dryness with gentle heat and suction from a water aspirator. Use a trap like that in Figure 2-17 in the textbook whenever you use an aspirator. Rinse the hydrolysis tube with 1 mL of distilled water, add it to the flask, and evaporate to dryness again. Dissolve the residue in 1.0 mL of 0.05 M NaOH and filter it through a $0.45-\mu \mathrm{m}$ pore size syringe filter. The total concentration of all amino acids in this solution is $\sim 50 \mathrm{mM}$.

## Derivatization

3. Using a micropipet, place $345 \mu \mathrm{~L}$ of 20 mM borate buffer into a small screw-cap vial. Add $10 \mu \mathrm{~L}$ of the standard amino acid solution. Then add $10 \mu \mathrm{~L}$ of $5 \mathrm{mM} \alpha$-aminoadipic acid (the internal standard), $90 \mu \mathrm{~L}$ of 10 mM KCN , and $75 \mu \mathrm{~L}$ of 10 mM naphthalene-2,3-dicarboxaldehyde. The fluorescent yellow-green color of the amino acid-NDA product should appear within minutes. After 25 min , add $25 \mu \mathrm{~L}$ of $1.5 \mathrm{M} \mathrm{NH}_{3}$ to react with excess NDA. Wait 15 min before electrophoresis.
4. Place $345 \mu \mathrm{~L}$ of 20 mM borate buffer ( pH 9.0 ) into a small screw-cap vial. Add $10 \mu \mathrm{~L}$ of the hydrolyzed protein solution in 0.05 M NaOH from step 2 . Then add $10 \mu \mathrm{~L}$ of 5 mM $\alpha$-aminoadipic acid (the internal standard), $60 \mu \mathrm{~L}$ of 10 mM KCN , and $50 \mu \mathrm{~L}$ of 10 mM naphthalene-2,3-dicarboxaldehyde. After 25 min , add $25 \mu \mathrm{~L}$ of $1.5 \mathrm{M} \mathrm{NH}_{3}$ to react with
excess NDA. After 15 min , begin electrophoresis. (Precise timing reduces variations between the standard and the unknown.)

## Electrophoresis and Analysis of Results

5. (Caution: Electrophoresis uses a dangerously high voltage of $20-24 \mathrm{kV}$. Be sure to follow all safety procedures.) Electrophoresis is conducted with a $50-\mu \mathrm{m}$-inner-diameter uncoated silica capillary and spectrophotometric detection at 420 nm . Precondition the column by injecting $30 \mu \mathrm{~L}$ of 0.1 M NaOH and flushing 15 min later with $30 \mu \mathrm{~L}$ each of distilled water and then run buffer. The column should be reconditioned in the same manner after every 3-4 runs.
6. Inject 3 nL of standard amino acid mixture from step 3. The electropherogram should look similar to Figure 1. Measure the area of each peak (or the height, if you do not have a computer for measurement of area). Repeat the injection and measure the areas again.
7. Find the quotient

$$
\frac{\text { area of amino acid peak }}{\text { area of internal standard peak }}
$$

for each amino acid in the standard mixture. (Use peak heights if area is not available.) Prepare a table showing the relative areas for each peak in each injection of standard and find the average quotient for each amino acid from both runs.
8. Inject 3 nL of derivatized, hydrolyzed protein from step 4 and measure the same quotient as measured in step 7. Repeat the injection and find the average quotient from both injections.
9. You know the concentration of internal standard in the protein hydrolysate from the volume and concentration of internal standard used in step 4. Find the concentration of each amino acid in the protein hydrolysate by using Equation 5-11 in the textbook.
10. Find the mole ratio of amino acids in the protein. If there were no experimental error, you could divide all concentrations by the lowest one. Because the lowest concentration has a large relative error, pick an amino acid with two or three times the concentration of the least concentrated amino acid. Define this concentration to be exactly 2 or 3 . Then compute the molarities of other amino acids relative to the chosen amino acid. Your result is a formula such as $\mathrm{S}_{10.6} \mathrm{~T}_{6.6} \mathrm{H}_{0.82} \mathrm{G}_{12.5} \mathrm{~A}_{11.2} \mathrm{E}_{5.3} \mathrm{Y}_{\equiv 3} \mathrm{D}_{19.8} \mathrm{~V}_{6.1} \mathrm{M}_{2.2} \mathrm{I}_{5.7}(\mathrm{~L}+\mathrm{F})_{11.5}$.

## 31. DNA Composition by High-Performance Liquid Chromatography ${ }^{52}$

This experiment illustrates quantitative analysis by high performance liquid chromatography (HPLC). It uses only aqueous eluent, so there is no hazardous waste to dispose.

The genetic material deoxyribonucleic acid, is a polymer made of four nucleotides abbreviated C, T, A, and G:


2'-Deoxycytidine 5'-monophosphate (C)


Thymidine 5'-monophosphate (T)


2'-Deoxyadenosine 5'-monophosphate (A)


2'-Deoxyguanosine 5'-monophosphate (G)

In double-stranded DNA, C is hydrogen bonded to G and A is hydrogen bonded to T . Therefore the concentrations of C and G are equal and the concentrations of A and T are equal. DNA from different organisms has different relative amounts of $(\mathrm{C}+\mathrm{G})$ and $(\mathrm{A}+\mathrm{T})$. When DNA is hydrolyzed by the enzyme nuclease $\mathrm{P}_{1}$, it is cleanly broken into the four nucleotides.

[^27]
## Reagents

Standard nucleotide solution: The standard should contain accurately weighed quantities of the nucleotide monophosphates ${ }^{53}$ at concentrations of $\sim 20 \mathrm{mM}$. The molecular masses of the free acids are $\mathrm{C}-307.2, \mathrm{~T}-322.2$, $\mathrm{A}-331.2, \mathrm{G}-347.2$. Place the required quantities of the solid acids in a $5-\mathrm{mL}$ volumetric flask and add 2 mL of water and 1.6 mL of $0.10 \mathrm{M} \mathrm{NaOH}(2 \mathrm{~mol}$ NaOH per mol of nucleotide). Dissolve the solid, dilute to the mark with water, mix well, and store the standard in a refrigerator. (The volume of the standard changes when it is cooled, but this is not important. Only the relative concentrations of nucleotides in the standard are important in this experiment.)
Hydrolyzed DNA: The volumes of DNA and nuclease $\mathrm{P}_{1}$ solutions should be the minimum required for the number of people doing the experiment. Prepare a solution containing 1 $\mathrm{mg} / \mathrm{mL}$ of calf thymus (or other) DNA. ${ }^{53}$ Dissociate the DNA into single strands by heating at $100^{\circ} \mathrm{C}$ for 10 min and then cooling immediately on ice. Prepare nuclease $\mathrm{P}_{1}{ }^{53}$ at a final concentration of 5 units $/ \mathrm{mL}^{54}$ in 50 mM sodium acetate buffer ( pH 5.3 ) containing 0.6 mM $\mathrm{ZnCl}_{2}$. Mix $20 \mu \mathrm{~L}$ of DNA solution with $20 \mu \mathrm{~L}$ of nuclease solution in a small vial with a conical bottom. Heat the vial at $50^{\circ} \mathrm{C}$ for 1 h and analyze it immediately or store it in the refrigerator.
HPLC Eluent: Prepare 0.010 M potassium phosphate buffer by dissolving $0.010 \mathrm{~mol} \mathrm{~K}_{2} \mathrm{HPO}_{4}$ in 800 mL of water, titrating with $\sim 1 \mathrm{M} \mathrm{HCl}$ to pH 7.2 , and diluting to 1.00 L .

## Chromatography

1. A variety of $\mathrm{C}_{18}$-silica columns should work in this experiment. A $0.46 \times 15 \mathrm{~cm}$ column with $5 \mu \mathrm{~m}$ particles is reasonable. Equilibrate the column with 20 empty column volumes of 0.010 M phosphate buffer ( pH 7.2 ) at a flow rate of $1.2 \mathrm{~mL} / \mathrm{min}$ before beginning chromatography. Establish a flat baseline with an ultraviolet detector at or near 260 nm .
2. Inject $10 \mu \mathrm{~L}$ of the nucleotide standard. You should observe a clean separation of all four peaks ( $\mathrm{C}<\mathrm{T}<\mathrm{G}<\mathrm{A}$ ) with an elution time of 5-10 min. Measure the areas of all four peaks, preferably by computer integration. Alternatively, you can estimate peak area from the

[^28]formula: area of Gaussian peak $=1.064 \times$ peak height $\times w_{1 / 2}$, where $w_{1 / 2}$ is the width at halfheight. Express the areas of C, T, and A relative to the area of G, which we will define as 1.000. Repeat the procedure with a second injection and measure the relative areas. List the relative peak areas in each run and the average of the two runs.
3. Inject $10 \mu \mathrm{~L}$ of hydrolyzed DNA and measure the relative areas of the peaks. Repeat the process a second time. List the relative areas in each run and the average of the two runs.

## Calculations

1. From the average peak areas of the two standard runs, find the response factors for $\mathrm{C}, \mathrm{T}$, and A relative to G . For example, the response factor for C is obtained from the equation

$$
\begin{aligned}
\frac{\text { area of } \mathrm{C}}{\text { concentration of } \mathrm{C}} & =F\left(\frac{\text { area of } \mathrm{G}}{\text { concentration of } \mathrm{G}}\right) \\
\frac{\mathrm{A}_{\mathrm{C}}}{[\mathrm{C}]} & =F\left(\frac{\mathrm{~A}_{\mathrm{G}}}{[\mathrm{G}]}\right)
\end{aligned}
$$

There will be similar equations for T , and A . We are using G as the internal standard.
2. From the average peak areas of the two injections of hydrolyzed DNA, find the relative concentrations $[\mathrm{C}] /[\mathrm{G}],[\mathrm{T}] /[\mathrm{G}]$, and $[\mathrm{A}] /[\mathrm{G}]$ by using the response factors from the standard mixture. What is the theoretical value of $[\mathrm{C}] /[\mathrm{G}]$ ? What is the theoretical relationship between $[\mathrm{T}] /[\mathrm{G}]$ and $[\mathrm{A}] /[\mathrm{G}]$ ?
3. Find the fraction of nucleotides that are $\mathrm{C}+\mathrm{G}$ by evaluating the expression

Fraction of $C+G$ :

$$
\frac{[\mathrm{C}]+[\mathrm{G}]}{[\mathrm{C}]+[\mathrm{G}]+[\mathrm{A}]+[\mathrm{T}]}=\frac{\frac{[\mathrm{C}]}{[\mathrm{G}]}+\frac{[\mathrm{G}]}{[\mathrm{G}]}}{\frac{[\mathrm{C}]}{[\mathrm{G}]}+\frac{[\mathrm{G}]}{[\mathrm{G}]}+\frac{[\mathrm{A}]}{[\mathrm{G}]}+\frac{[\mathrm{T}]}{[\mathrm{G}]}}
$$

For calf thymus DNA, the literature value of the fraction of $\mathrm{C}+\mathrm{G}$ is 0.42 .

## 32. Analysis of Analgesic Tablets by High-Performance Liquid Chromatography ${ }^{55}$



Nonprescription headache medications such as Excedrin or Vanquish contain mixtures of acetaminophen and aspirin for relief and caffeine as a stimulant. This experiment describes conditions for separating and measuring the components by high-performance liquid chromatography (HPLC). Instructions are given for measuring caffeine, but any and all of the components could be measured.


Caffeine


Aspirin (acetylsalicylic acid)


Acetaminophen

## Reagents

HPLC solvent: Organic solvents should be handled in a fume hood. All solvents in this experiment should be HPLC-grade. Mix 110 mL of acetonitrile, 4.0 mL of triethylamine, and 4.0 mL of acetic acid in a 2-L volumetric flask and dilute to the mark with HPLC-grade water. Filter through a $0.45-\mu \mathrm{m}$ filter and store in a tightly capped amber bottle.
Caffeine stock solution ( $100 \mu \mathrm{~g} / \mathrm{mL}$ ): Dissolve 1.000 g of caffeine in 50 mL of HPLC solvent in a $100-\mathrm{mL}$ volumetric flask with gentle heating (in the hood). Cool to room temperature and dilute to the mark with HPLC solvent. Dilute 10.00 mL to 100 mL with HPLC solvent in a volumetric flask to obtain $1000 \mu \mathrm{~g} / \mathrm{mL}$. Dilute once again to obtain $100 \mu \mathrm{~g} / \mathrm{mL}$.
Acetaminophen and aspirin samples: Prepare two solutions, each containing one of the analytes at a concentration of $\sim 50 \mu \mathrm{~g} / \mathrm{mL}$ in HPLC solvent. Filter through $0.22 \mu \mathrm{~m}$ nylon syringe filters and store in capped amber bottles.

[^29]
## Procedure

1. Caffeine quantitative analysis standards: Dilute the $100 \mu \mathrm{~g} / \mathrm{mL}$ stock solution down to 50 , 10 , and $5 \mu \mathrm{~g} / \mathrm{mL}$ with HPLC solvent. Filter $\sim 3 \mathrm{~mL}$ of each solution through a $0.22-\mu \mathrm{m}$ syringe filter into a capped vial. Filter $\sim 3 \mathrm{~mL}$ of the $100 \mu \mathrm{~g} / \mathrm{mL}$ solution into a fourth vial.
2. Sample preparation: Grind the analgesic tablet into a fine powder with a clean mortar and pestle. Dissolve $\sim 0.5 \mathrm{~g}$ (weighed accurately) in 50 mL of HPLC solvent with gentle heating. Cool to room temperature and dilute to volume with HPLC solvent. Dilute 10.00 mL of this solution to 100 mL with HPLC solvent in a volumetric flask. Filter $\sim 3 \mathrm{~mL}$ of the dilute solution through a $0.22-\mu \mathrm{m}$ syringe filter into a capped vial.
3. Chromatography conditions: Use a 2.1 -mm-diameter $\times 10-\mathrm{cm}$-long $\mathrm{C}_{18}$-silica column with $5-\mu \mathrm{m}$ particle size and ultraviolet detection at 254 nm . With a flow rate of $1.5 \mathrm{~mL} / \mathrm{min}$, each run is complete in 4 min .
4. Calibration curve: Inject $10 \mu \mathrm{~L}$ of each of the caffeine standards (5, 10, 50, and 100 $\mu \mathrm{g} / \mathrm{mL}$ ) into the HPLC and measure the peak area. Repeat this process twice more and use the average areas from the three runs to construct a calibration curve of area versus concentration. Compute the least-squares slope and intercept for the line through points.
5. Qualitative analysis: Record a chromatogram of $10 \mu \mathrm{~L}$ of the analgesic tablet solution. Then mix 2 drops of the tablet solution with 2 drops of $50 \mu \mathrm{~g} / \mathrm{mL}$ caffeine solution in a test tube or vial. Inject $10 \mu \mathrm{~L}$ of the mixture into the chromatograph and observe which peak grows. Repeat the process again by adding $50 \mu \mathrm{~g} / \mathrm{mL}$ acetaminophen and $50 \mu \mathrm{~g} / \mathrm{mL}$ aspirin and identify which peaks in the analgesic are acetaminophen and aspirin.
6. Quantitative analysis: Inject $10 \mu \mathrm{~L}$ of the analgesic tablet solution and measure the area of the caffeine peak. Repeat this process twice more and take the average from three injections. Using your calibration graph, determine the concentration of caffeine in the solution and the weight percent of caffeine in the original tablet.

## 33. Anion Content of Drinking Water by Capillary Electrophoresis ${ }^{56}$



Chloride, sulfate, and nitrate are the major anions in fresh water. Fluoride is a minor species added to some drinking water at a level near 1.6 ppm to help prevent tooth decay. In this experiment, you will measure the three major anions by capillary electrophoresis. Possible class projects are to compare water from different sources (homes, lakes, rivers, ocean) and various bottled drinking waters.

Your equipment should be similar to that in Figure 26-19 in the textbook. Convenient capillary dimensions are a diameter of $75 \mu \mathrm{~m}$ and a length of 40 cm from the inlet to the detector (total length $=50 \mathrm{~cm}$ ). Because the anions have little ultraviolet absorbance at wavelengths above 200 nm , we add chromate anion $\left(\mathrm{CrO}_{4}^{2-}\right)$ to the buffer and use indirect ultraviolet detection at 254 nm . The principle of indirect detection is explained in Figure 26-31.

One other significant condition for a successful separation in this experiment is to reduce the electroosmotic flow rate to permit a better separation of the anions based on their different electrophoretic mobilities. At pH 8 , electroosmotic flow is so fast that the anions are swept from the injector to the detector too quickly to be separated well. To reduce electroosmotic flow, we could lower the pH to protonate some $-\mathrm{O}^{-}$groups on the wall. Alternatively, in this experiment we add the cationic surfactant tetradecyl-(trimethyl)ammonium ion, $\mathrm{CH}_{3}\left(\mathrm{CH}_{2}\right)_{13} \stackrel{+}{\mathrm{N}}\left(\mathrm{CH}_{3}\right)_{3}$, which is attracted to $-\mathrm{O}^{-}$groups on the wall and partially neutralizes the negative charge of the wall. This cationic surfactant is abbreviated $\mathrm{OFM}^{+}$, for "osmotic flow modifier."

## Reagents

Run buffer: $4.6 \mathrm{mM} \mathrm{CrO}_{4}^{2-}+2.5 \mathrm{mM} \mathrm{OFM}^{+}$at pH 8 . Dissolve $1.08 \mathrm{~g} \mathrm{Na}_{2} \mathrm{CrO}_{4} \cdot 4 \mathrm{H}_{2} \mathrm{O}(\mathrm{FM}$ 234.02) plus 25.0 mL of 100 mM tetradecyl(trimethyl)ammonium hydroxide ${ }^{57} \mathrm{in} 800 \mathrm{~mL}$ of HPLC-grade $\mathrm{H}_{2} \mathrm{O}$. Place a pH electrode in the solution and add solid boric acid $\left(\mathrm{H}_{3} \mathrm{BO}_{3}\right)$ (with magnetic stirring) to reduce the pH to 8.0 . Dilute to 1.00 L with HPLC-grade $\mathrm{H}_{2} \mathrm{O}$, mix well, filter through a $0.45-\mu \mathrm{m}$ filter, and store in the refrigerator in a tightly capped plastic bottle. Degas prior to use.
56. S. Demay, A. Martin-Girardequ, and M.-F. Gonnord, J. Chem. Ed. 1999, 76, 812.
57. 100 mM tetradecyl(trimethyl)ammonium hydroxide (Catalog number WAT049387) is available from www.waters.com. The surfactant trade name is "Osmotic Flow Modifier," abbreviated $\mathrm{OFM}^{+} \mathrm{OH}^{-}$.

Quantitative standards: Prepare one stock solution containing $1000 \mathrm{ppm} \mathrm{Cl}^{-}, 1000 \mathrm{ppm} \mathrm{NO}_{3}^{-}$, and $1000 \mathrm{ppm} \mathrm{SO}_{4}^{2-}$ by dissolving the following salts in 1.000 L of HPLC-grade $\mathrm{H}_{2} \mathrm{O}: 2.103$ g KCl (FM 74.55), $1.631 \mathrm{~g} \mathrm{KNO}_{3}$ (FM 101.10), and $1.814 \mathrm{~g} \mathrm{~K}_{2} \mathrm{SO}_{4}$ (FM 174.26).
(Concentration refers to the mass of the anion. For example, 1000 ppm sulfate means 1000 $\mu \mathrm{g}$ of $\mathrm{SO}_{4}^{2-}$ per mL of solution, not $1000 \mu \mathrm{~g}$ of $\mathrm{K}_{2} \mathrm{SO}_{4}$.) Dilute the stock solution with HPLC-grade $\mathrm{H}_{2} \mathrm{O}$ to make standards with concentrations of $2,5,10,20,50$, and 100 ppm of the anions. Store the solutions in tightly capped plastic bottles.

Standards for qualitative analysis: Prepare four separate $1.00-\mathrm{L}$ solutions, each containing just one anion at a concentration of $\sim 50 \mathrm{ppm}$. To do this, dissolve $\sim 0.105 \mathrm{~g} \mathrm{KCl}, \sim 0.082 \mathrm{~g} \mathrm{KNO}_{3}$, $\sim 0.091 \mathrm{~g} \mathrm{~K}_{2} \mathrm{SO}_{4}$, or $\sim 0.153 \mathrm{~g} \mathrm{KF}$ (FM 58.10) in 1.00 L .

## Procedure

0. CAUTION: Electrophoresis uses a dangerously high voltage. Be sure to follow all safety procedures for the instrument.
1. When preparing a capillary for its first use, wash through 1 M NaOH for 15 min , followed by 0.1 M NaOH for 15 min , followed by run buffer for 15 min . In this experiment, wash the column with run buffer for 1 min between sample injections.
2. Identify the peaks: Inject a 50 ppm mixture of $\mathrm{Cl}^{-}, \mathrm{NO}_{3}^{-}$, and $\mathrm{SO}_{4}^{2-}$ by applying a pressure of 0.3 bar for 5 s . Then insert the sample end of the capillary back in run buffer and perform a separation for 5 min at 10 kV with the capillary thermostatted near $25^{\circ} \mathrm{C}$. The voltage should be positive at the injector and negative at the detector. The detector should be set at 254 nm . After the run, wash the column with run buffer for 1 min . Mix the 50 ppm anion mixture with an equal volume of $50 \mathrm{ppm} \mathrm{Cl}^{-}$and run an electropherogram of the mixture. The $\mathrm{Cl}^{-}$peak should be twice the size it was in the first run. Repeat the procedure with additions of $\mathrm{NO}_{3}^{-}, \mathrm{SO}_{4}^{2-}$, and $\mathrm{F}^{-}$. This process tells you which peak belongs to each anion and where to look for $\mathrm{F}^{-}$in drinking water.
3. Calibration curves: Inject each of the standard mixtures from lowest concentration to highest concentration ( $2,5,10,20,50$, and 100 ppm ) and measure the area of each peak in each run. Repeat the sequence twice more and use the average peak area at each concentration to construct a calibration curve for each anion. Find the least-squares straight line to fit the graph of area versus concentration for each anion.
4. Unknowns: Make three replicate injections of each unknown water sample and measure the areas of the peaks. Use the average area of each peak and the calibration curves to find the concentrations of the anions in the water. If you analyze any saltwater samples, they should be diluted by a factor of 100 with HPLC-grade water to bring the anion concentrations down to the range of fresh waters.

## 34. Green Chemistry: Liquid Carbon Dioxide Extraction of Lemon Peel Oil ${ }^{58,59}$



In analytical procedures, solvent extraction can provide the initial separation of analyte from bulk sample. In this experiment, we extract a natural product from a renewable feedstock using liquid carbon dioxide as a nontoxic solvent under ambient conditions while generating minimal waste. If you really want to calculate the waste produced in the procedure, you would need to account for waste created in generating the energy required to make Dry Ice (solid $\mathrm{CO}_{2}$ ) used in the experiment, including the amount of Dry Ice lost between the location where it was made and your laboratory. You would also need to account for transportation of Dry Ice from the manufacturer to your laboratory. Even "green" procedures have hidden costs.
"Essential oils" used for flavors and fragrances are volatile organic compounds, including monoterpenes such as limonene, commonly found in plants such as citrus. Essential oils are often isolated by steam distillation in which citrus is boiled in water and the oil co-distills with the water. Liquid condensed from the steam contains both water and oil, which separate from each other. Steam distillation could hydrolyze or decompose some oils. Alternatively, organic


D-Limonene How can we isolate essential oils without using water or organic solvents?

Supercritical fluid extraction uses carbon dioxide at elevated temperature and pressure to achieve a liquid or supercritical fluid state suitable for chemical extractions. In the phase diagram for $\mathrm{CO}_{2}$ in Figure 1, the liquid-vapor boundary line ends at the critical point. At higher temperature and pressure than the critical point, separate liquid and gaseous phases no longer exist. Rather, there is a single supercritical phase whose properties are between those of the liquid and gas.

[^30]

A supercritical fluid might act as a liquid solvent to dissolve solutes, yet maintains viscosity and diffusion properties similar to those of a gas. Supercritical $\mathrm{CO}_{2}$ has advantages for extracting essential oils from flowers, fruit rind, and other products. Supercritical $\mathrm{CO}_{2}$ is nonflammable, relatively nontoxic, and readily available. To perform a supercritical extraction, an instrument is needed to heat and pressurize $\mathrm{CO}_{2}$ above its critical point ( $31^{\circ} \mathrm{C}$ and 74 bar ).

To mimic a true supercritical fluid extraction, we will use liquid $\mathrm{CO}_{2}$, which has properties similar to the supercritical fluid. Dry Ice sublimes at atmospheric pressure and temperatures above $-78^{\circ} \mathrm{C}$. If $\mathrm{CO}_{2}$ is sealed in a vessel during sublimation, the pressure in the vessel increases. After the temperature and pressure have increased sufficiently, liquid $\mathrm{CO}_{2}$ forms. We can exploit the ease of $\mathrm{CO}_{2}$ liquefaction to extract essential oils from citrus rind.

## Reagents and Supplies

Crushed (powdered) Dry Ice: $25 \mathrm{~g} /$ student.
Grated lemon peel (zest): $2.5 \mathrm{~g} /$ student. Grate only the colored part of the lemon peel with the smallest grating surface of a cheese grater. ${ }^{60}$
Methanol: $5 \mathrm{~mL} /$ student.
15-mL polypropylene centrifuge tube: one/student (Corning \#430052 recommended).
Copper wire: $20-\mathrm{cm}$ length of 18-22 gauge wire for each student.

[^31]500-mL plastic graduated cylinder or wide-mouth polycarbonate jar: one per student.
Alternatively, construct a watertight cylinder from a $30-\mathrm{cm}-l o n g$ clear plastic tube with a $25-$ mm diameter and 3-mm wall thickness cemented to a flat plastic base with silicone calk.

Filter paper: one $1.5-\mathrm{cm}$-diameter circle of Whatman \#1 filter paper per student
Thermometer: Several students can share a single thermometer to measure water at $40-50^{\circ} \mathrm{C}$.
Forceps: Several students can share a single pair of forceps capable of reaching into the cylinder to remove the centrifuge tube.

Tweezers: Several students can share a single pair.
Pasteur pipet: One per student.

## Safety Precautions

0. Pressure generated during this experiment creates a risk of flying plastic centrifuge caps and rupture of plastic vessels. The source for this procedure ${ }^{58}$ reports that caps blew off in $4 \%$ of all experiments, so you can EXPECT this to happen in your laboratory. Under no circumstance should vessels other than the recommended ones be used.
1. Do not use any glass in this experiment. Substitution of glass centrifuge tubes or graduated cylinders could result in serious injuries if shattering should occur.
2. Always wear eye protection.
3. Use gloves when handling dry ice. Contact with dry ice can damage your skin.
4. Do not liquefy $\mathrm{CO}_{2}$ more than 5 times in the same centrifuge tube. After repeated liquefaction, the tube may become brittle and rupture.

## Procedure

0. Read safety precautions and the entire procedure before beginning the experiment.
1. Verify that the cap fits tightly on the centrifuge tube. If the cap does not stop turning when you screw it down, try a different cap or different tube. Unscrew the cap and put it aside.
2. Following Figure 2, coil the copper wire into 3 circles on one end and leave the other end straight. The coils should fit into the centrifuge tube and rest above the tapered section of the tube. The straight section of wire should be contained within the tube when the cap is screwed on. Place a small circle of filter paper between the coils so that the filter paper will support the solid to be extracted. Insert the coil with its filter paper into the centrifuge tube.


Figure 2. Extraction procedure. ${ }^{58}$
3. Add $\sim 2.5 \mathrm{~g}$ of grated lemon peel to the tube, but do not pack tightly. The peel should rest on the filter paper. During extraction, liquid $\mathrm{CO}_{2}$ must penetrate the loosely packed peel and reach the bottom tip of the centrifuge tube.
4. Fill the $500-\mathrm{mL}$ plastic cylinder or wide-mouth polycarbonate water bottle one-half to twothirds full of warm tap water at $40-50^{\circ} \mathrm{C}$. Do not heat the cylinder or add hot water at any time later in the experiment, or the cap can blow off the centrifuge tube during the extraction.
5. Wearing gloves and using a scoop or small beaker, fill the centrifuge tube with crushed Dry Ice. Tap the tube on the lab bench and add more Dry Ice to fill the tube. Take the cap that you have already tested for a tight fit and screw it tight. If the seal is not tight, try a different cap or, if necessary, start again with a different tube and cap.
6. Place the centrifuge tube with the tapered end down into the cylinder or plastic jar of warm water. Sublimation of Dry Ice will build high pressure inside the tube and liquid $\mathrm{CO}_{2}$ will appear in about 15 seconds. Even though the cap is tight, gas will escape through the threads.
7. View the boiling $\mathrm{CO}_{2}$ in the centrifuge tube from the side of the cylinder. Do not look into the top of the cylinder. If the cap blows, it will fly straight up and hit you in the face.
8. If liquid $\mathrm{CO}_{2}$ does not appear within a minute, the seal is not tight enough to maintain sufficient pressure in the centrifuge tube. Take the tube out of the cylinder with forceps,
tighten the cap, and place it back in the warm water. If liquid $\mathrm{CO}_{2}$ does not appear after several attempts to tighten the cap, try a different cap. If necessary, begin again with a fresh combination of tube and cap. ${ }^{61}$
9. When the cap is tight, liquid will appear in the tube and gas will slowly escape through the threads. Slowly rotate the cylinder so that the cold centrifuge tube does not freeze to the cylinder wall. Do not remove the centrifuge tube from the cylinder while liquid $\mathrm{CO}_{2}$ is present. The cylinder protects you in case the pressurized centrifuge tube explodes.
10. Liquid $\mathrm{CO}_{2}$ in the centrifuge tube boils vigorously and extracts essential oil from the lemon peel. After a few minutes, $\mathrm{CO}_{2}$ will have escaped from the tube and no liquid will be left. Approximately 0.1 mL of pale yellow oil should be visible at the bottom of the centrifuge tube. If the tube is packed too tightly with lemon peel, liquid $\mathrm{CO}_{2}$ cannot reach the tip of the tube and extracted oil will not collect at the tip.
11. When no liquid $\mathrm{CO}_{2}$ is left in the centrifuge tube, remove the tube from the cylinder with forceps and unscrew the cap slightly to allow the remaining pressure to escape. After all pressure has been released, it is safe to remove the cap. Using tweezers, carefully pull the wire from the tube to remove the lemon peel.
12. Transfer the extracted oil by Pasteur pipet into a gas chromatography autosampler vial and dilute with methanol. Use gas chromatography-mass spectrometry to compare your extract to a commercial sample of lemon oil. We recommend a DB-5 or other $5 \%$ phenyl, nonpolar column with a $10^{\circ} \mathrm{C} / \mathrm{min}$ temperature gradient. Extracted lemon oil will have about six major components.
13. As part of your lab report, identify the major peaks in the chromatogram from their mass spectra. Perform a literature search on supercritical fluid extraction. (a) Find one reference to the use of supercritical fluid extraction in the flavor and fragrance industry. (b) Aside from essential oils, what types of compounds are commonly extracted via supercritical fluid extraction? (c) Identify a vendor of supercritical fluid extraction equipment. ${ }^{62}$

[^32]
[^0]:    4. This section was contributed by Douglas E. Raynie, Department of Chemistry and Biochemistry, South Dakota State University, Brookings SD 57007; douglas.raynie@sdstate.edu.
    5. P. T. Anastas and J. C. Warner, Green Chemistry: Theory and Practice (New York: Oxford University Press, 1998).
[^1]:    6. H. A. Laitinen, Anal. Chem., 1966, 38, 1441.
[^2]:    7. P.T. Anastas, Crit. Rev. Anal. Chem. 1999, 29, 167.
    8. J. Namiesnik, J. Sep. Sci. 2001, 24, 151.
    9. L.H. Keith, L.U. Gron, and J.L. Young, Chem. Rev. 2007, 107, 2695.
[^3]:    10. http://www.epa.gov/epawaste/hazard/wastetypes/pdfs/listing-ref.pdf
    11. http://www.epa.gov/tri/trichemicals/pbt\%20chemicals/pbt_chem_list.htm
[^4]:    13. C. H. Hendrickson and P. R. Robinson, J. Chem. Ed. 1979, 56, 341.
[^5]:    14. R. Q. Thompson and M. Ghadiali, J. Chem. Ed. 1993, 70, 170.
[^6]:    15. D. A. Skoog and D. M. West, Fundamentals of Analytical Chemistry, 3d ed. (New York: Holt, Rinehart and Winston, 1976).
[^7]:    16. Basic reagents should not be stored in glass bottles because they slowly dissolve glass. If ammonia from a glass bottle is used, it may contain silica particles and should be freshly filtered.
[^8]:    18. D. T. Harvey, J. Chem. Ed. 1991, 68, 329.
[^9]:    19. J. Burnett and W. A. Burns, "Using a Spreadsheet to Fit Experimental pH Titration Data to a Theoretical Expression: Estimation of Analyte Concentration and $K_{\mathrm{a}}$,"J. Chem. Ed. 2006, 83, 1190.
[^10]:    22. R. M. Fowler and H. A. Bright, J. Res. National Bureau of Standards 1935, 15, 493.
[^11]:    27. P. Phinyocheep and I. M. Tang, J. Chem. Ed. 1994, 71, A115.
[^12]:    28. E. Thall, J. Chem. Ed. 1981, 58, 561.
[^13]:    30. E. Dudek, J. Chem. Ed. 1977, 54, 329.
    31. J. F. Owen, C. S. Patterson, and G. S. Rice, Anal. Chem. 1983, 55, 990, describe simple procedures for the removal of chloride from $\mathrm{Cu}, \mathrm{Ni}$, and Co samples prior to electrogravimetric analysis.
    32. Some metals, such as $\mathrm{Zn}, \mathrm{Ga}$, and Bi , form alloys with Pt and should not be deposited directly on the Pt surface. The electrode should be coated first with Cu , dried, and then used. Alternatively, Ag can be used in place of Pt for depositing these metals. Platinum anodes are attacked by $\mathrm{Cl}_{2}$ formed by electrolysis of $\mathrm{Cl}^{-}$solutions. To prevent chlorine attack, $1-3 \mathrm{~g}$ of a hydrazinium salt (per 100 mL of solution) can be used as an anodic depolarizer, because hydrazine is more readily oxidized than $\mathrm{Cl}^{-}: \mathrm{N}_{2} \mathrm{H}_{4} \rightarrow \mathrm{~N}_{2}+4 \mathrm{H}^{+}+4 \mathrm{e}^{-}$.
[^14]:    33. W. C. Hoyle and T. M. Thorpe, J. Chem. Ed. 1978, 55, A229.
[^15]:    34. D. H. Evans, J. Chem. Ed. 1968, 45, 88.
[^16]:    35. A constant-current circuit for coulometer generator electrodes is given by J. Swim, E. Earps, L. M. Reed, and D. Paul, J. Chem. Ed. 1996, 73, 679. An operational amplifier circuit for the detector and a circuit for controlled-potential coulometry are given by E. Grimsrud and J. Amend, J. Chem. Ed. 1979, 56, 131.
[^17]:    36. R. C. Atkins, J. Chem. Ed. 1975, 52, 550
[^18]:    37. Idea based on P. E. Adams, J. Chem. Ed. 1995, 72, 649.
[^19]:    38. For literature values of the equilibrium constant for the reaction between $\mathrm{I}_{2}$ and pyridine, see S . S. Barton and R. H. Pottier, J. Chem. Soc. Perkin Trans. II 1984, 731.
[^20]:    39. V. L. McDevitt, A. Rodriquez and K. R. Williams, J. Chem. Ed. 1998, 75, 625.
[^21]:    40. Adapted from San Jose State University Laboratory Manual for a curriculum described by S. P. Perone, J. Pesek, C. Stone, and P. Englert, J. Chem. Ed. 1998, 75, 1444.
[^22]:    41. Adapted from San Jose State University Laboratory Manual for a curriculum described by S. P. Perone, J. Pesek, C. Stone, and P. Englert, J. Chem. Ed. 1998, 75, 1444.
[^23]:    42. Adapted from San Jose State University Laboratory Manual for a curriculum described by S. P. Perone, J. Pesek, C. Stone, and P. Englert, J. Chem. Ed. 1998, 75, 1444.
[^24]:    43. Part of this experiment is taken from M. W. Olson and J. M. Crawford, J. Chem. Ed. 1975, 52, 546.
[^25]:    44. Bio-Rad Laboratories, www.bio-rad.com
[^26]:    48. D. Jaffe and S. Herndon, J. Chem. Ed. 1995, 72, 364.
    49. Available from Scott Specialty Gases, www.scottgas.com
[^27]:    52. S. M. Wietstock, J. Chem. Ed. 1995, 72, 950.
[^28]:    53. www.sigmaaldrich.com
    54. For nuclease $P_{1}$, one unit is defined as the amount that will liberate $1.0 \mu \mathrm{~mol}$ of acid soluble nucleotides from yeast ribonucleic acid per min at pH 5.3 at $37^{\circ} \mathrm{C}$. The commercial preparation has at least $200 \mathrm{units} / \mathrm{mg}$ of nuclease $\mathrm{P}_{1}$.
[^29]:    55. G. K. Ferguson, J. Chem. Ed. 1998, 75, 467.
[^30]:    58 Adapted from L. C. McKenzie, J. E. Thompson, R. Sullivan, and J. E. Hutchison, Green Chem. 2004, 6, 355.
    59 Experiment contributed by Douglas E. Raynie, Department of Chemistry and Biochemistry, South Dakota State University, Brookings SD 57007; douglas.raynie@sdstate.edu.

[^31]:    60 Instead of lemon peel, you may chose to use orange peel. Orange oil will be about $95 \%$ D-limonene, which is sufficiently pure to characterize by infrared spectroscoy and nuclear magnetic resonance.

[^32]:    ${ }^{61}$ In some cases, $\mathrm{CO}_{2}$ might not liquefy or no extract is visible. If the centrifuge tube is rinsed with a small amount of methanol, enough extract to be observed via gas chromatography-mass spectrometry is usually obtained.
    62 Instructors: The University of Oregon Greener Education Materials for Chemists database (http://greenchem.uoregon.edu/Pages/Overview.php?CategoryIDString=\&FullTextSearchKeywords=orange\&C ategoriesToSearch $=\&$ NumberOfMainCategories=7\&AnyAll=Any\&ID=85) contains comments from people who have used this experiment and allows you to add comments from your experience.

